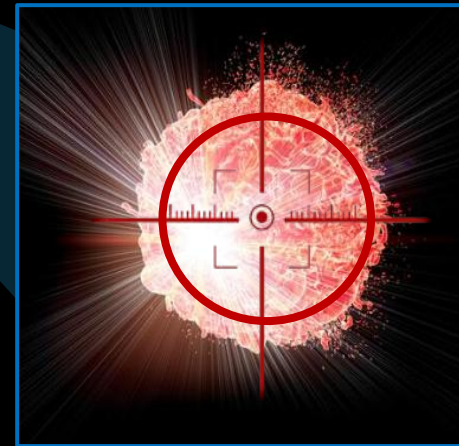
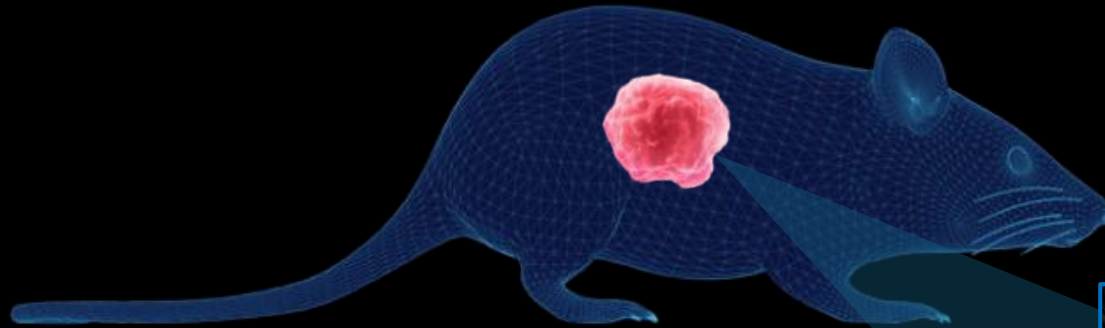




Università degli Studi di Pavia - PhD course in Physics

End Of the Year Seminars - 2025

For a safer Hadrontherapy



Supervisors:
Mario Pietro Carante
Francesca Ballarini

Alice Casali

PhD cycle: XL

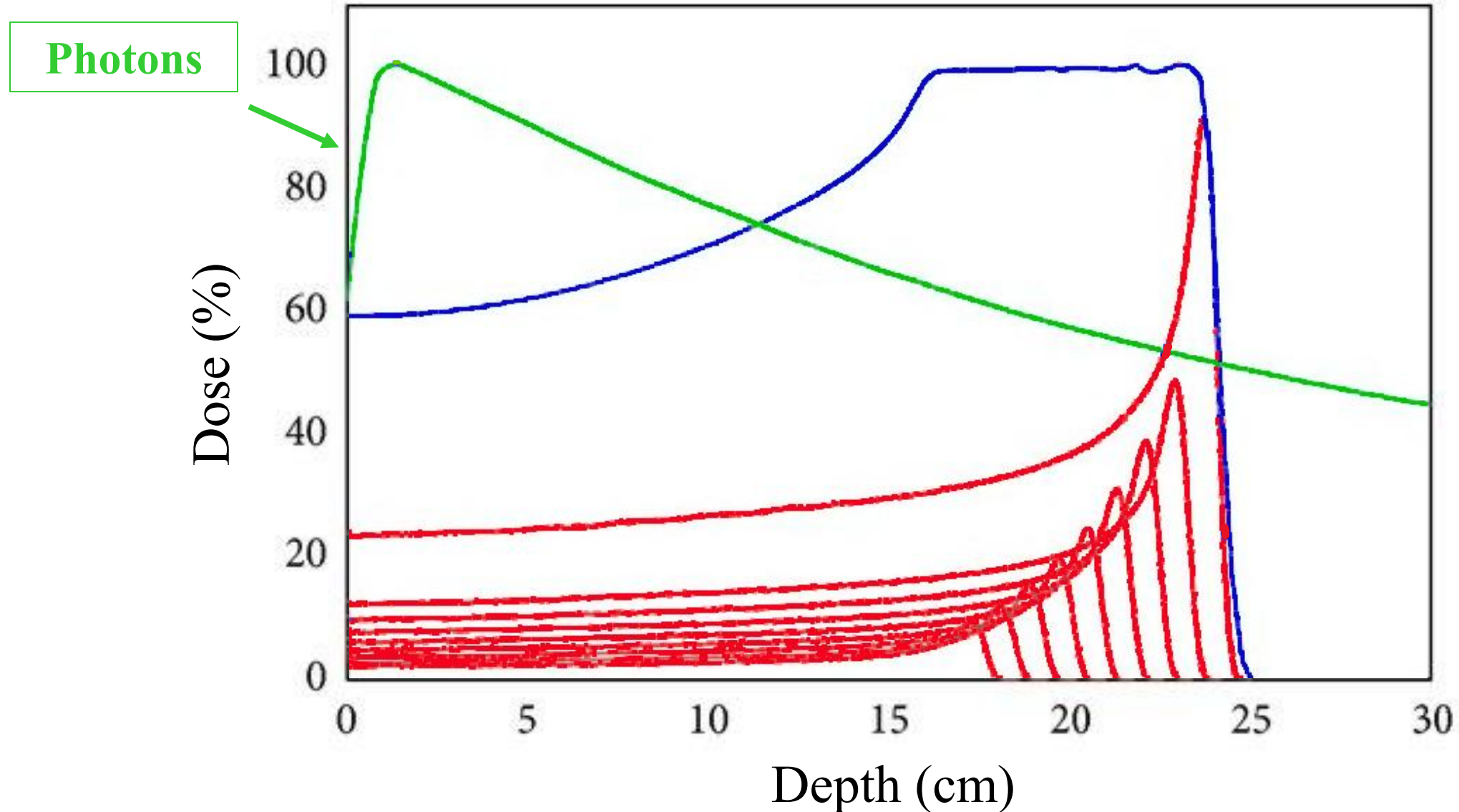
18 Sept 2025

A.A. 2024 - 2025

What is Hadrontherapy?

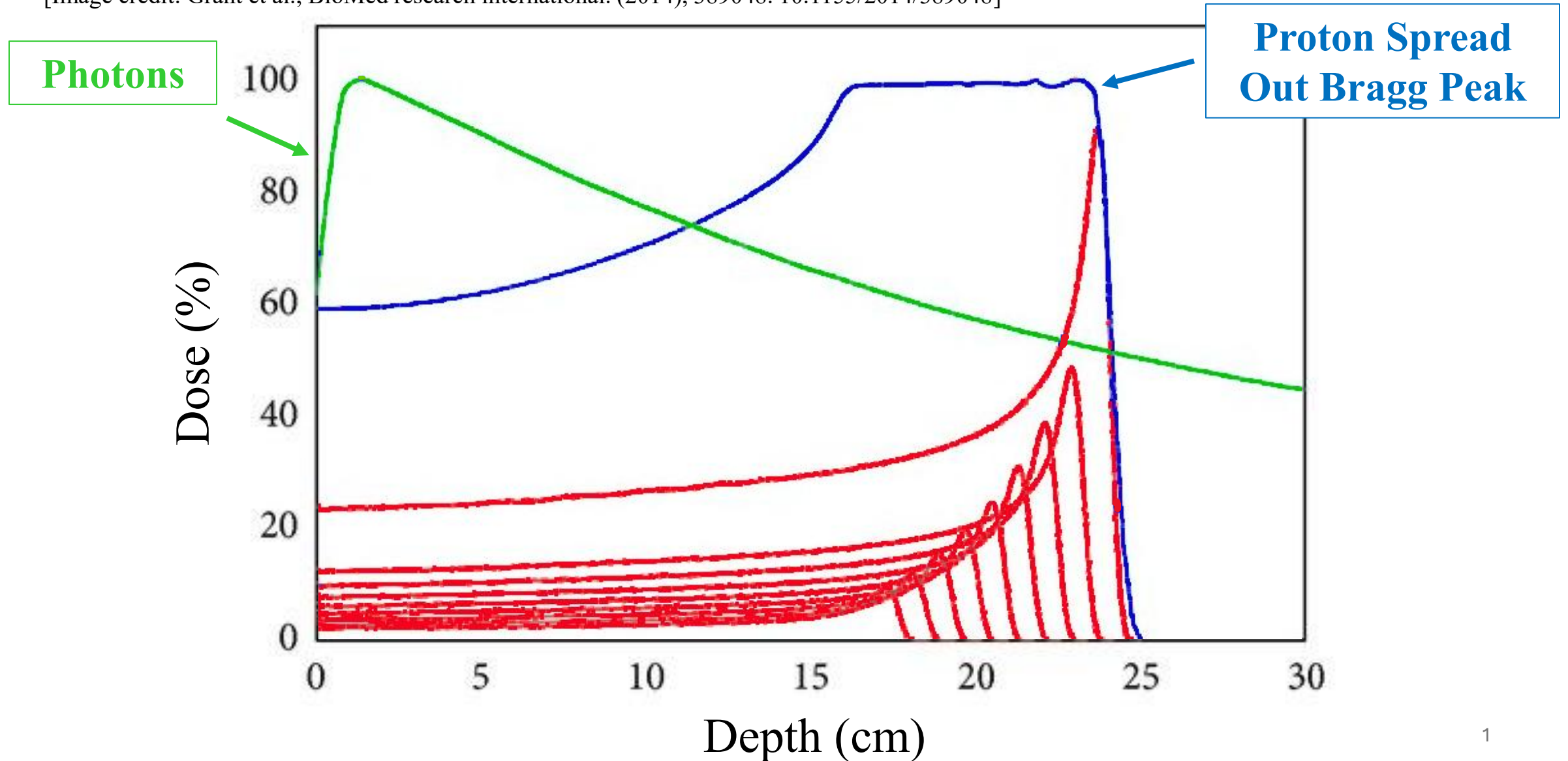
What is Hadrontherapy?

[Image credit: Grant et al., BioMed research international. (2014), 389048. 10.1155/2014/389048]



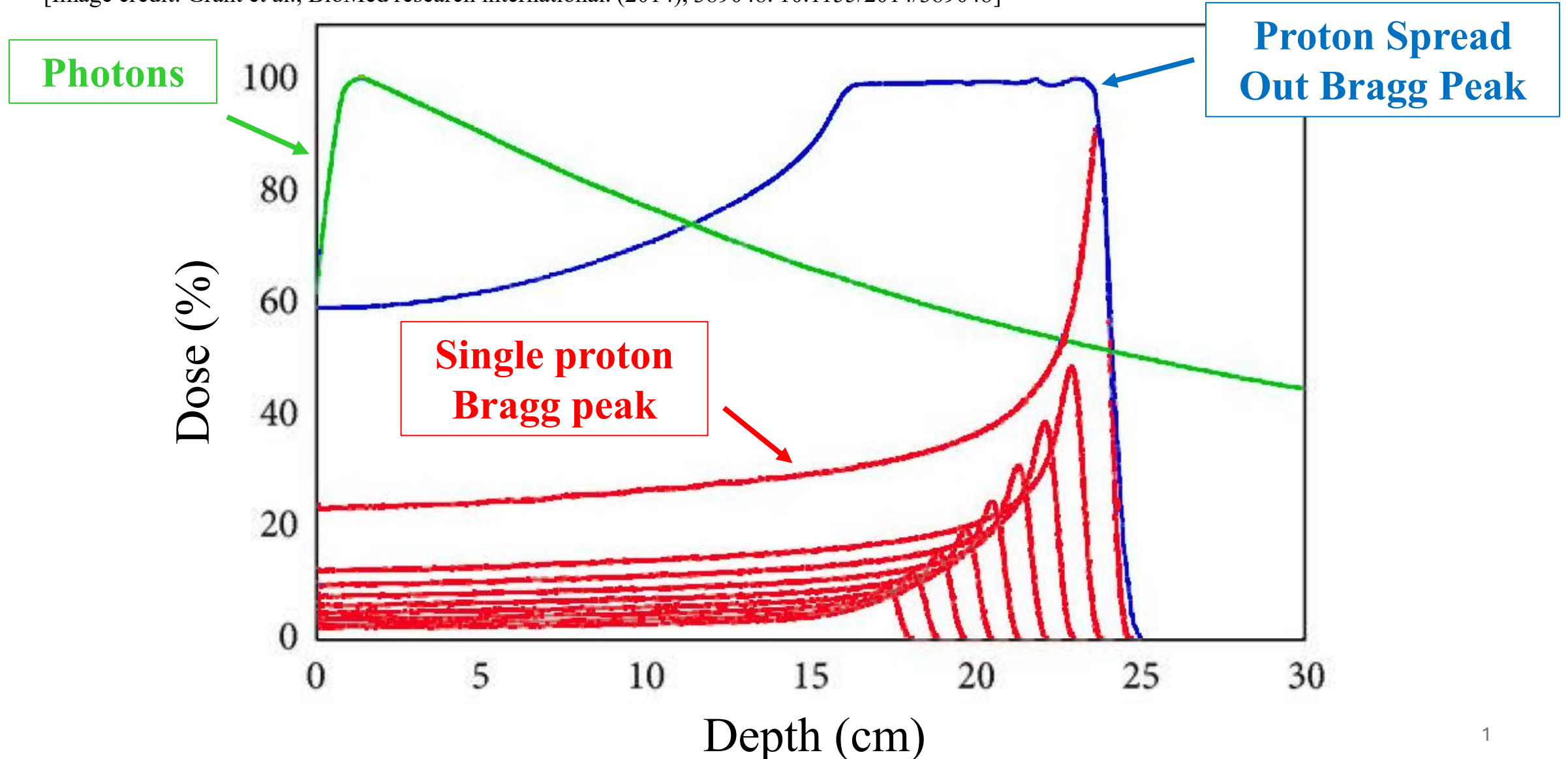
What is Hadrontherapy?

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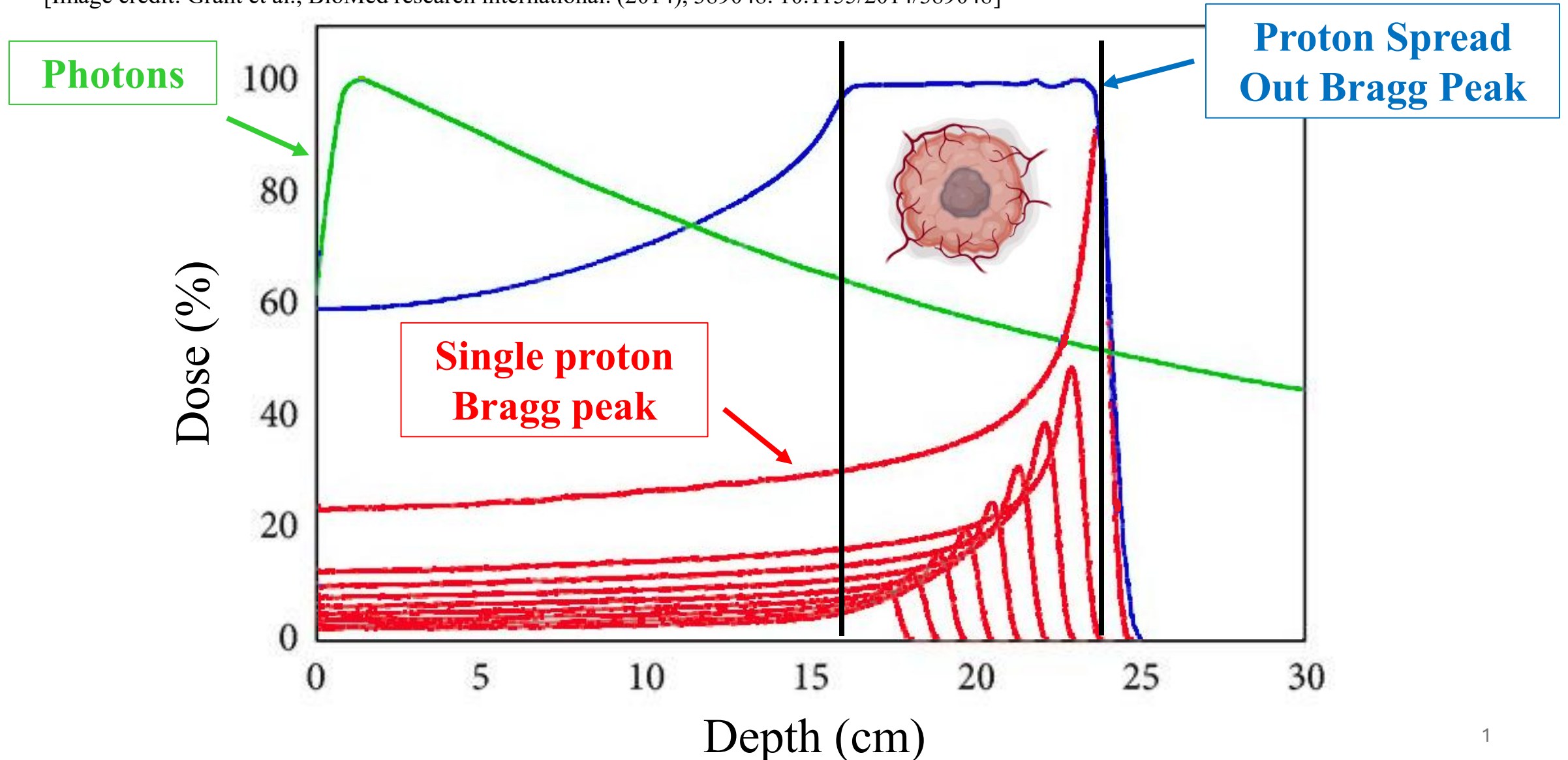
What is Hadrontherapy?

[Image credit: Grant et al., BioMed research international. (2014), 389048. 10.1155/2014/389048]



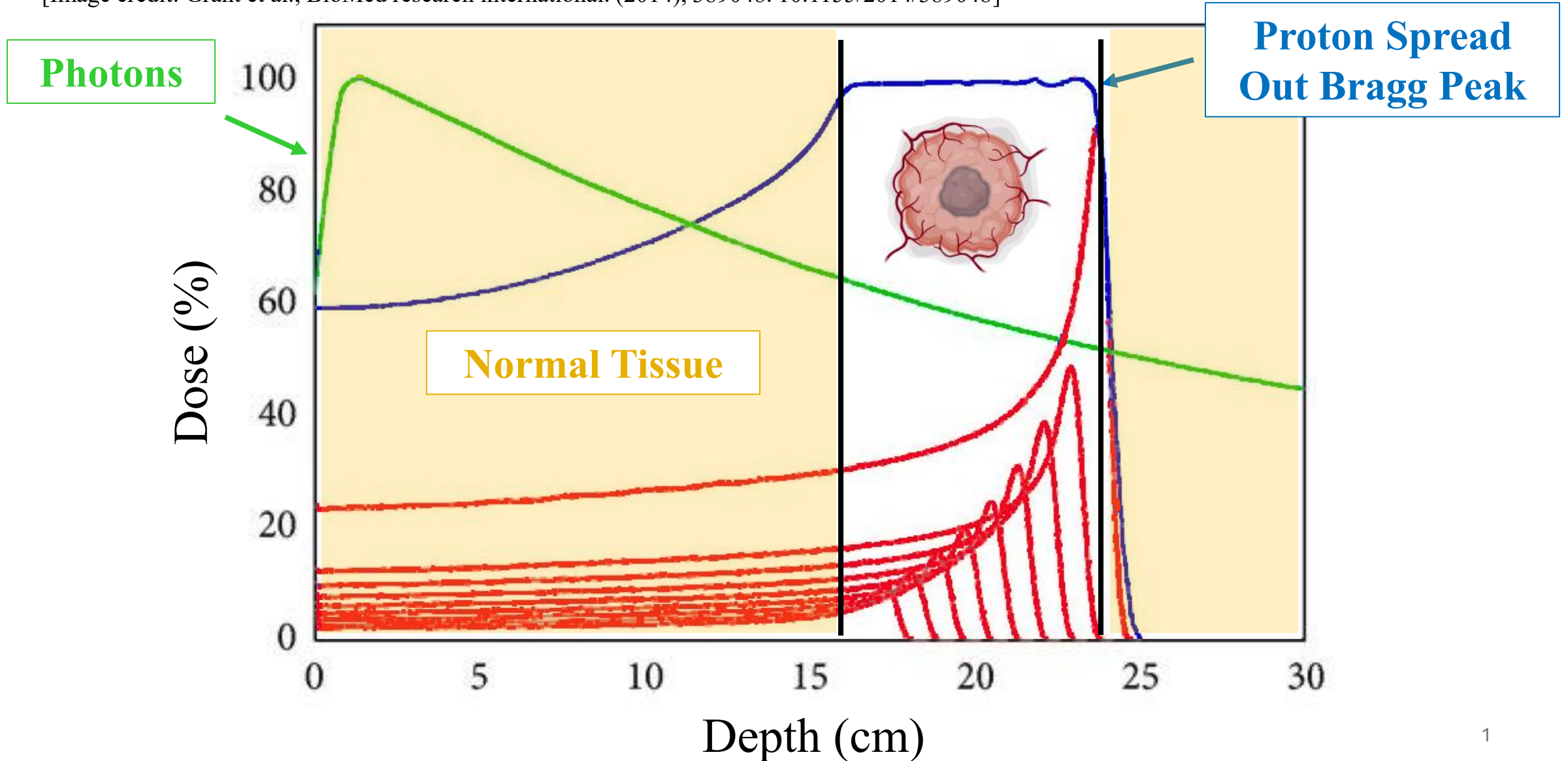
What is Hadrontherapy?

[Image credit: Grant et al., BioMed research international. (2014), 389048. 10.1155/2014/389048]



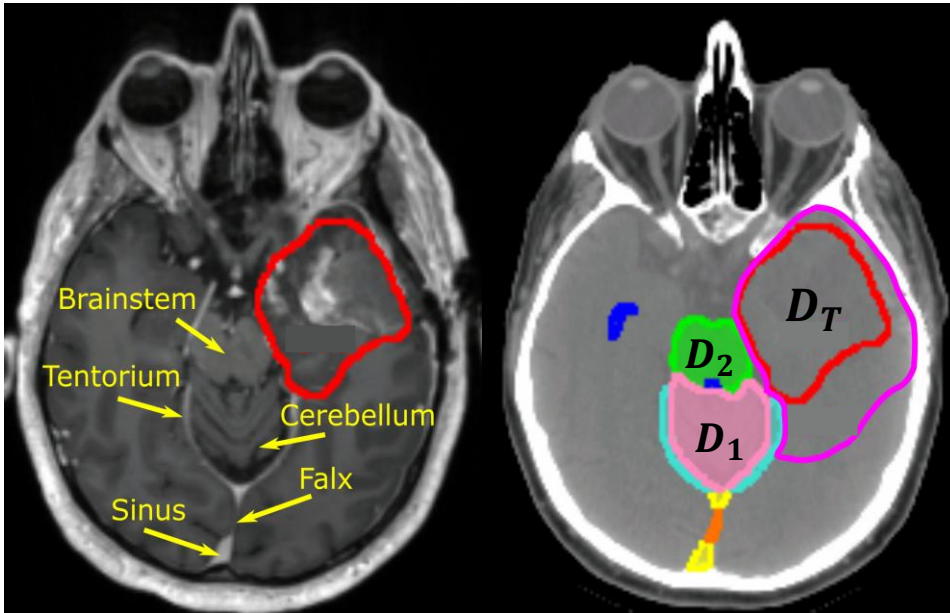
What is Hadrontherapy?

[Image credit: Grant et al., BioMed research international. (2014), 389048. 10.1155/2014/389048]



Treatment Planning

TODAY



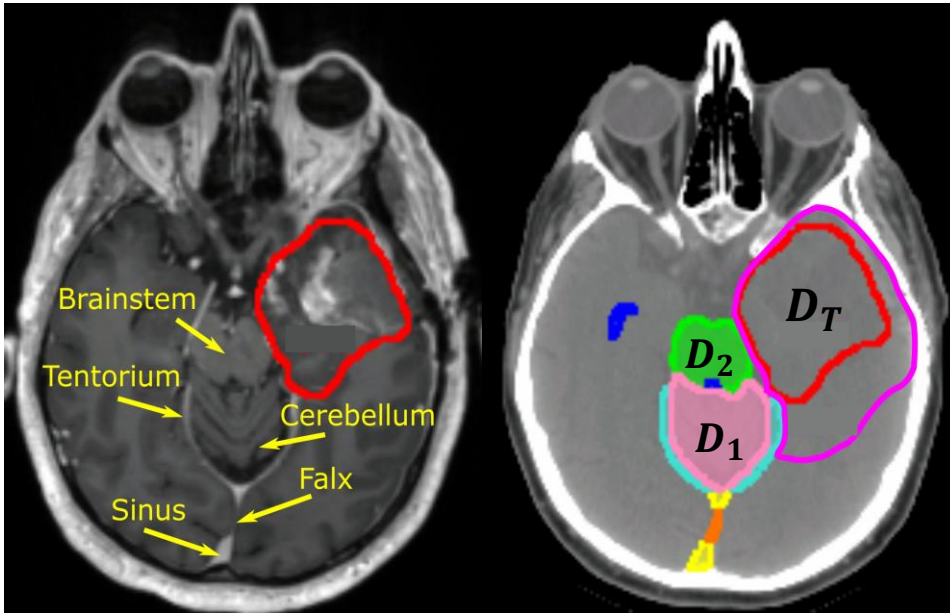
D_T = Tumour dose > 50 Gy

D_1 = OAR 1 < 2 Gy

D_2 = OAR 2 < 3 Gy

Treatment Planning

TODAY



D_T = Tumour dose > 50 Gy

D_1 = OAR 1 < 2 Gy

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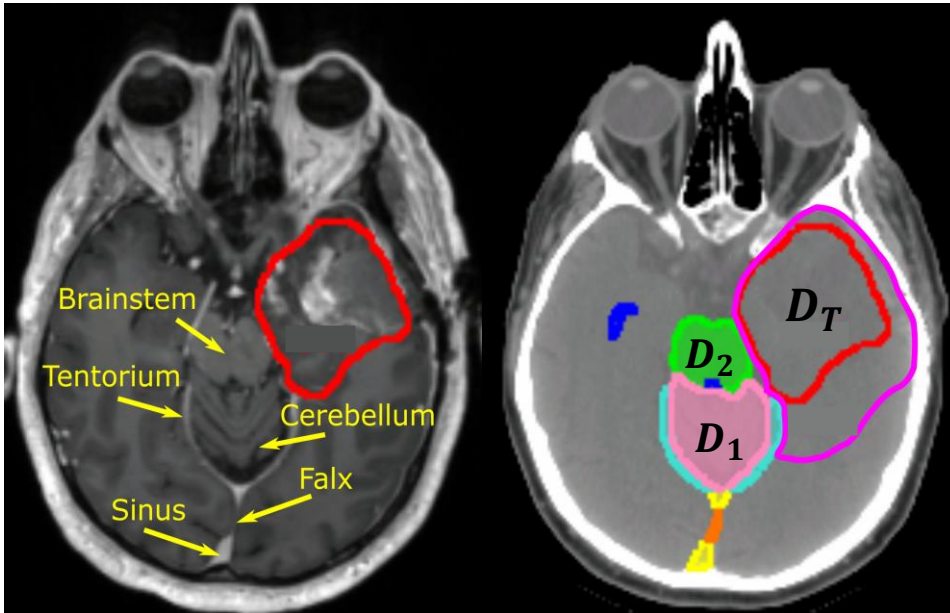


TOMORROW

Directly based on
clinical *outcomes*

Treatment Planning

TODAY



D_T = Tumour dose > 50 Gy

D_1 = OAR 1 < 2 Gy

D_2 = OAR 2 < 3 Gy

[Image credit: The Cancer Imaging Archive]

TOMORROW

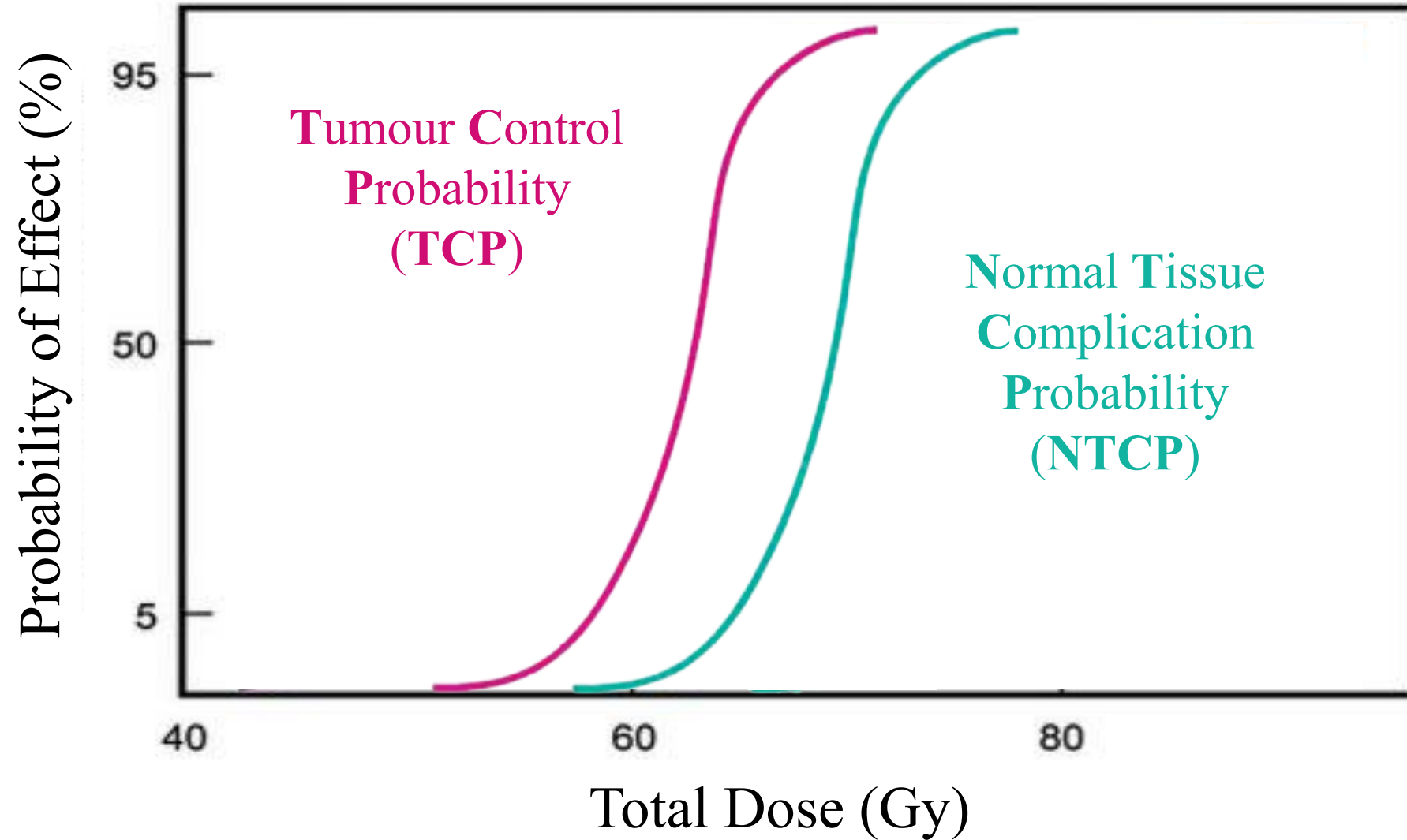
Directly based on
clinical *outcomes*



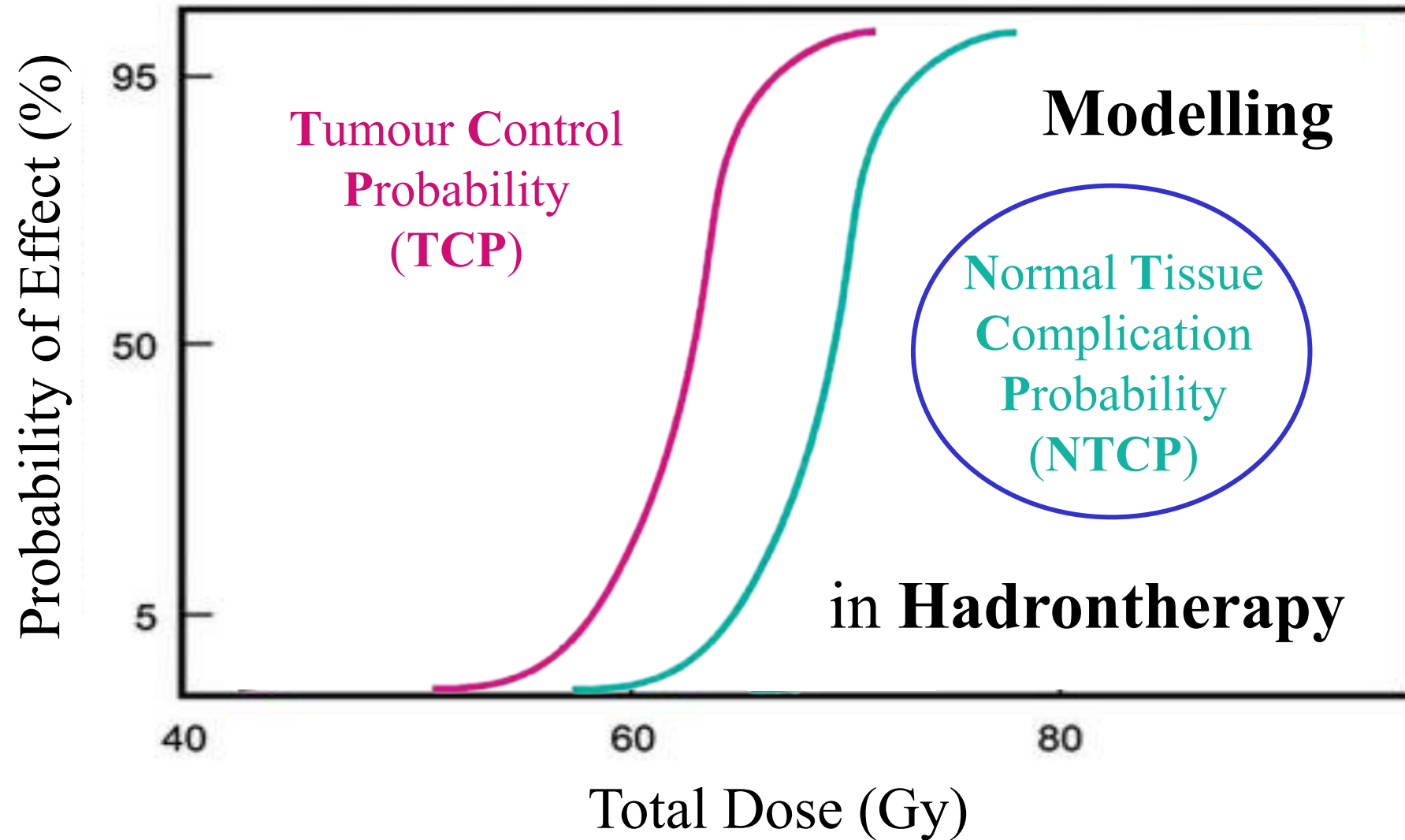
Patient-specific
treatment plans

Quantification of clinical *outcomes*

Quantification of clinical *outcomes*



Quantification of clinical *outcomes*



Existing
NTCP
models



LITERATURE

INNOVATION

Existing NTCP Models

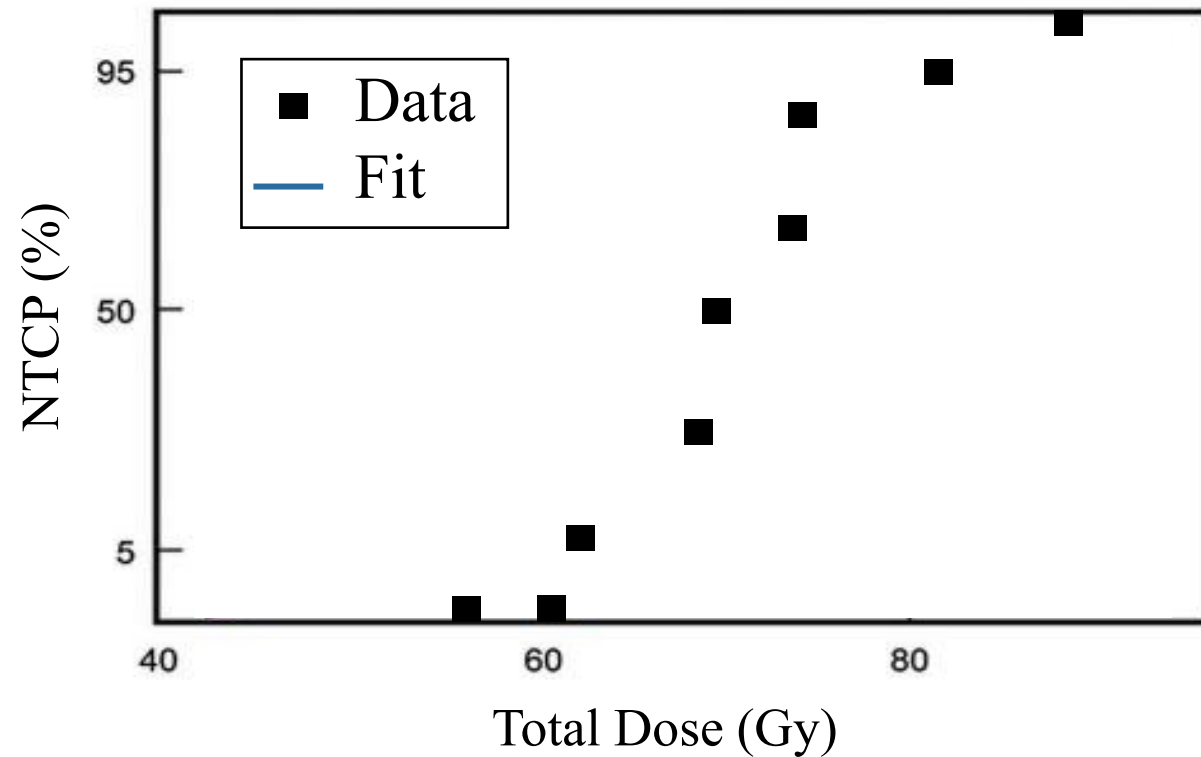
Phenomenological

Mechanistic

Existing NTCP Models

Phenomenological

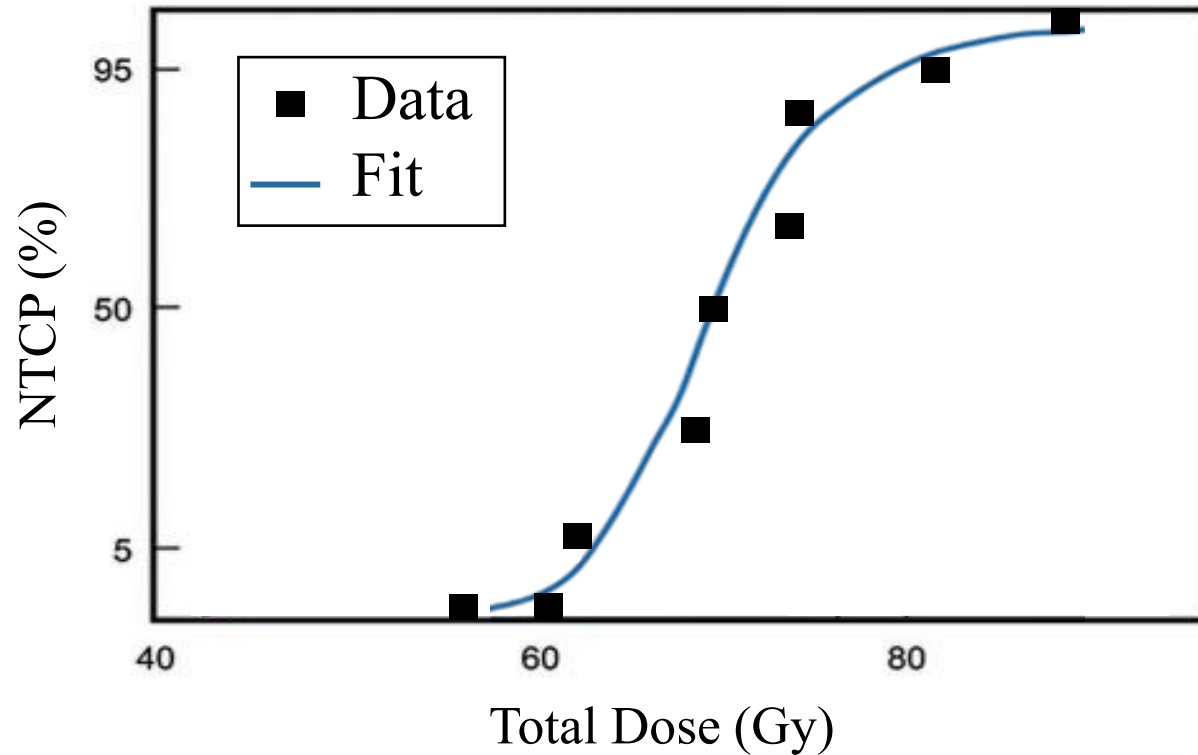
Mechanistic



Existing NTCP Models

Phenomenological

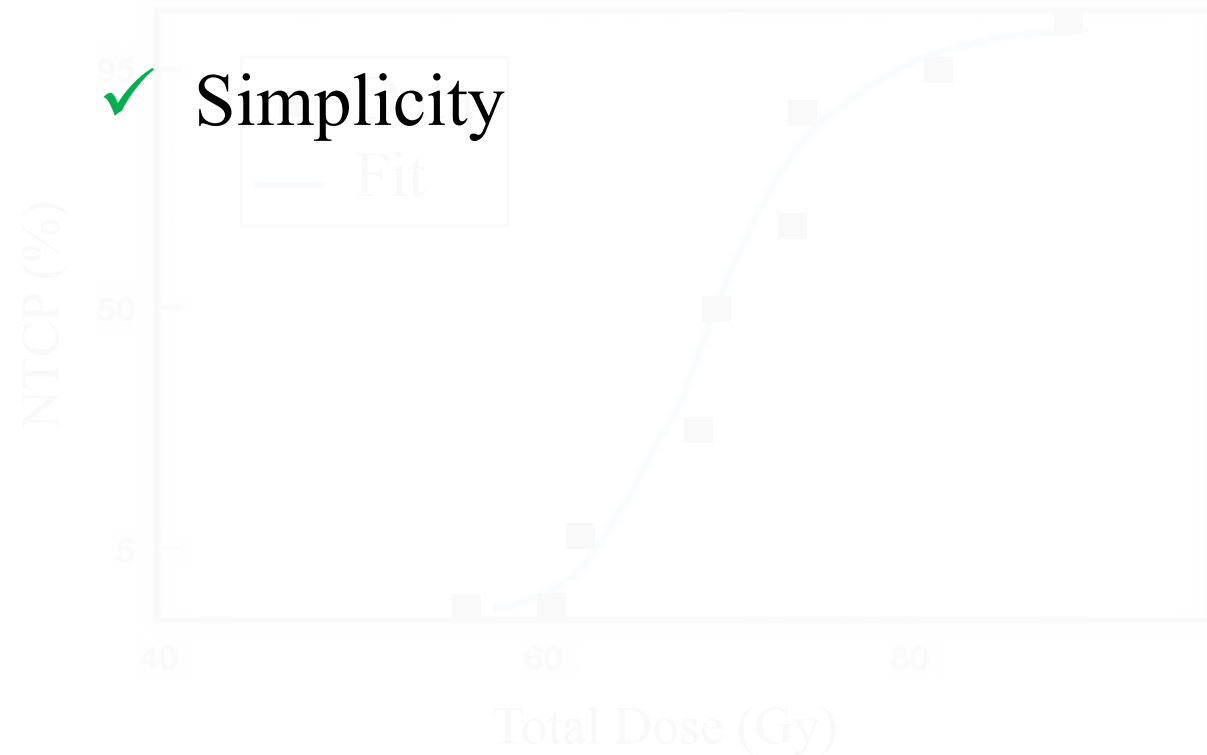
Mechanistic



Existing NTCP Models

Phenomenological

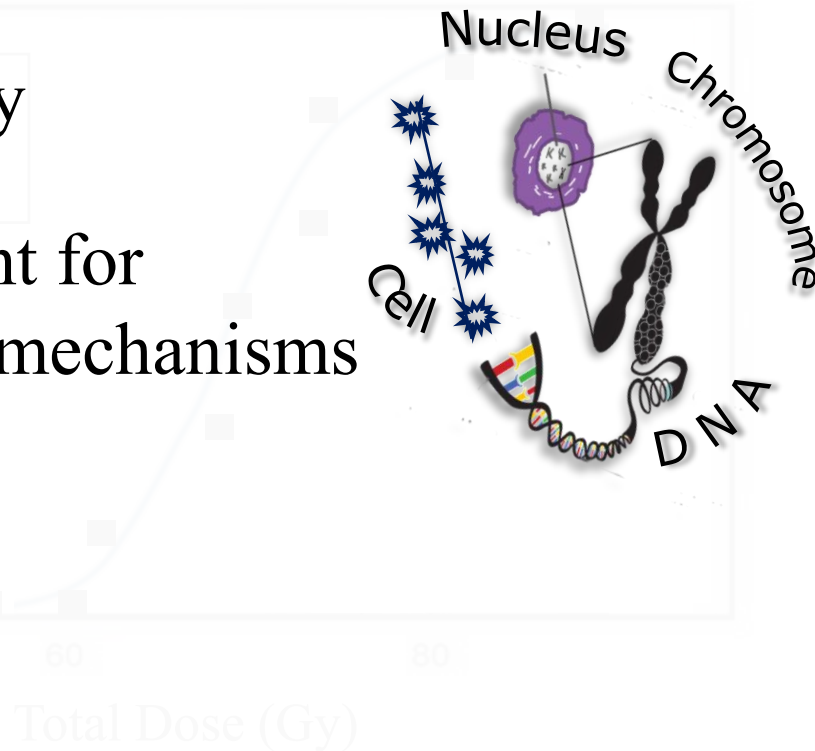
Mechanistic



Existing NTCP Models

Phenomenological

- ✓ Simplicity
- ✓ Not account for biological mechanisms

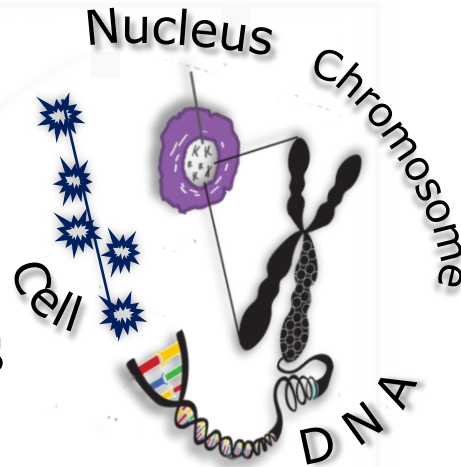


Mechanistic

Existing NTCP Models

Phenomenological

- ✓ Simplicity
- ✓ Not account for biological mechanisms



- ✗ Predictions in situations deviating from the validation dataset

Mechanistic

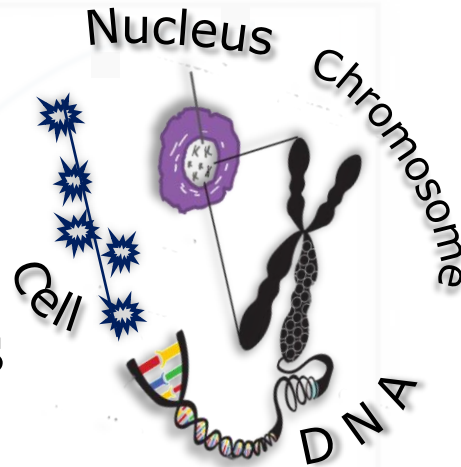
Existing NTCP Models

Phenomenological

✓ Simplicity

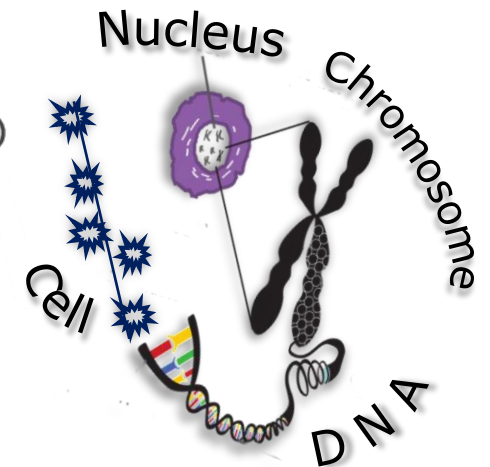
✓ Not account for biological mechanisms

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Mechanistic

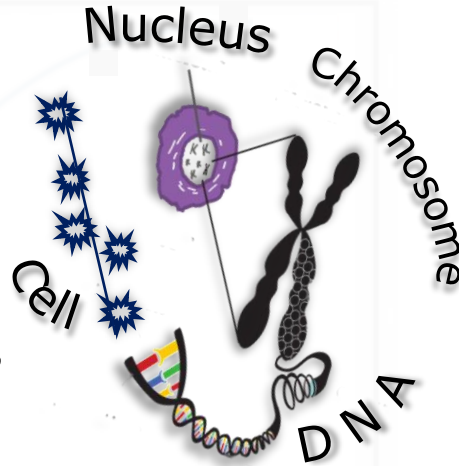
$$\alpha = \frac{e\gamma - \ln(\ln 2)}{D_{50}\left(1 + \frac{2}{\alpha/\beta}\right)} \quad EQD_2 = D_i \frac{1 + \frac{D_i/n}{\alpha/\beta}}{1 + \frac{2}{\alpha/\beta}}$$
$$\beta = \frac{e\gamma - \ln(\ln 2)}{D_{50}\left(\alpha/\beta + 2\right)} \quad NTCP(D_i, v_i) = \left\{1 - \prod_{i=1}^M [1 - P(D_i)^{v_i}]\right\}$$
$$t(D, V) = \frac{D - D(V/V_{ref})}{mD_{50}(V/V_{ref})}$$
$$NTCP(D, V) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^t e^{-\frac{x^2}{2}} dx$$
$$NTCP(D) = 1 - \exp\left[-\frac{\ln 2}{D_{50}} \left(\frac{D}{V_{ref}}\right)^n\right] = D_{50}(1) \left(\frac{V}{V_{ref}}\right)^{-n}$$



Existing NTCP Models

Phenomenological

- ✓ Simplicity
- ✓ Not account for biological mechanisms
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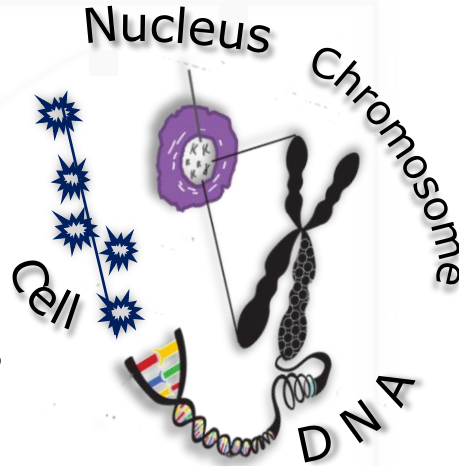
Mechanistic

- ✓ Parameters with physical and biological meanings

Existing NTCP Models

Phenomenological

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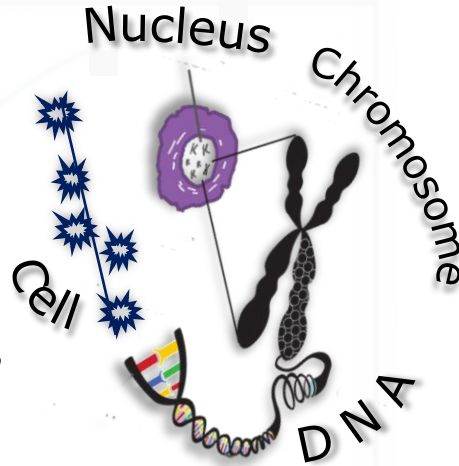
Mechanistic

- ✓ Parameters with physical and biological meanings
- ✓ Predictions

Existing NTCP Models

Phenomenological

- ✓ Simplicity
- ✓ Not account for biological mechanisms
- ✗ Predictions in situations deviating from the validation dataset



Mechanistic

- ✓ Parameters with physical and biological meanings
- ✓ Predictions
- ✗ Optimal parameters?

Lyman – Kutcher - Burman (LKB) model

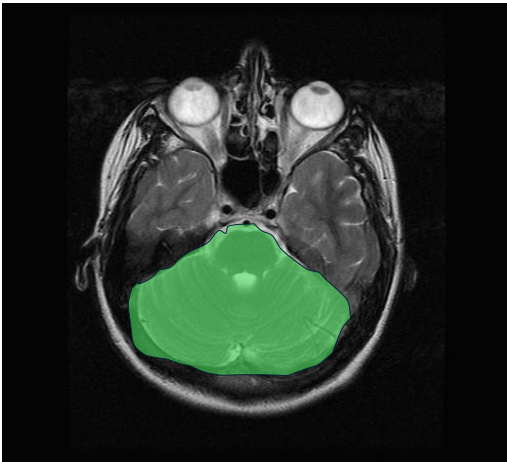
Phenomenological

Lyman – Kutcher - Burman (LKB) model

Phenomenological

Uniform dose distribution

Assumptions:

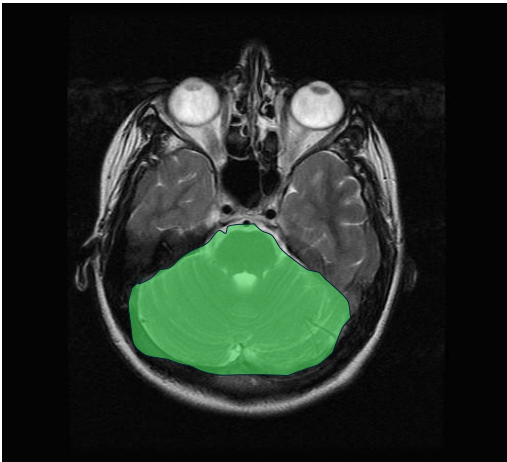


[Image credit: B.V. Prakash et al., Sci Rep 13. (2023), 10.1038/s41598-023-41576-6]

Lyman – Kutcher - Burman (LKB) model

Phenomenological

Uniform dose distribution



[Image credit: B.V. Prakash et al., Sci Rep 13. (2023), 10.1038/s41598-023-41576-6]

Assumptions:

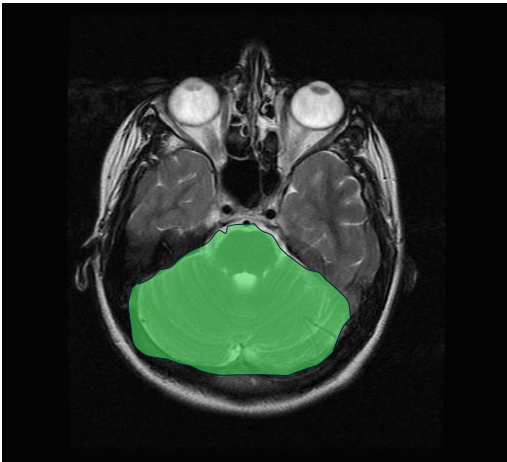


[J. T. Lyman, Radiat. Res., 1985]

Lyman – Kutcher - Burman (LKB) model

Phenomenological

Uniform dose distribution



[Image credit: B.V. Prakash et al., Sci Rep 13. (2023), 10.1038/s41598-023-41576-6]

Assumptions:

Power law
$$D_{50}(V) = \frac{D_{50}(1)}{V^n}$$

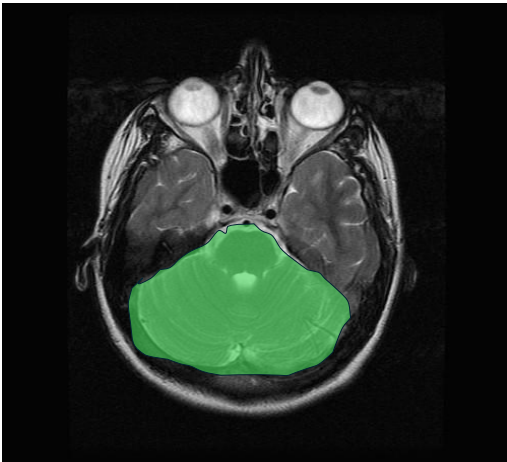


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Lyman – Kutcher - Burman (LKB) model

Phenomenological

Uniform dose distribution



[Image credit: B.V. Prakash et al., Sci Rep 13. (2023), 10.1038/s41598-023-41576-6]

Assumptions:

Power law $D_{50}(V) = \frac{D_{50}(1)}{V^n}$

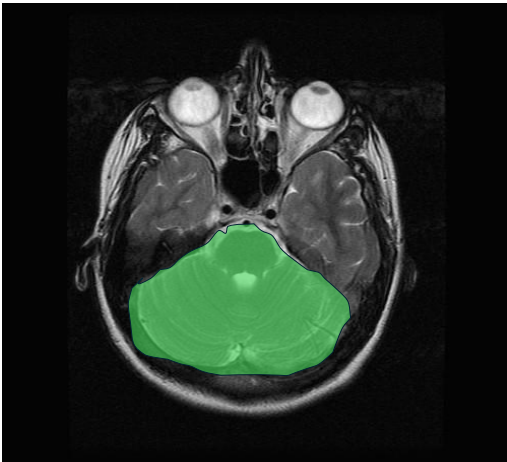


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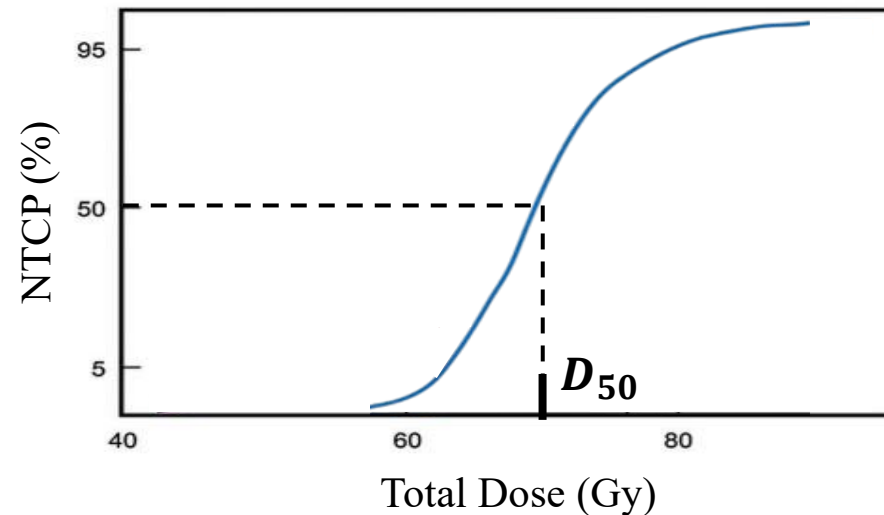


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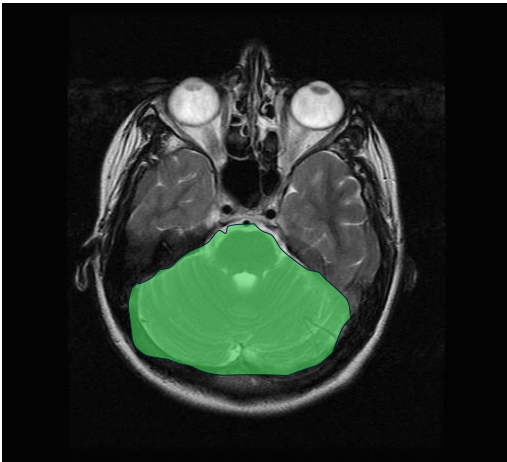


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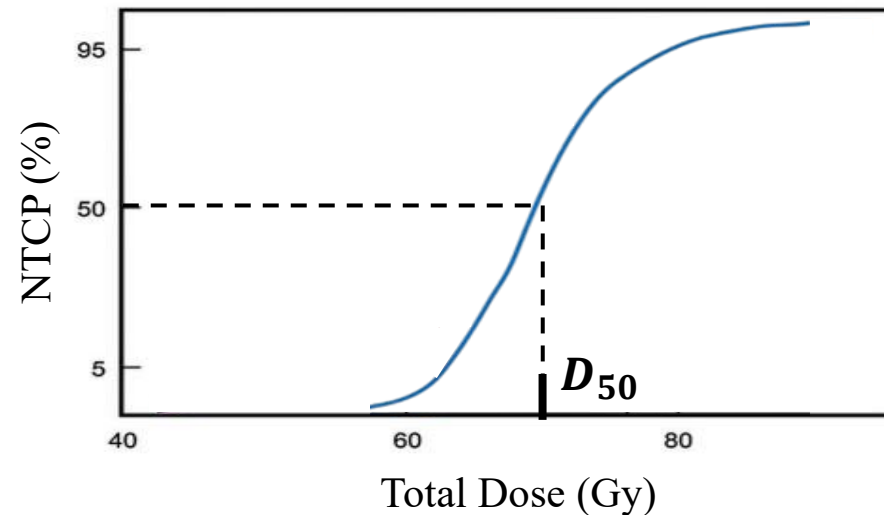
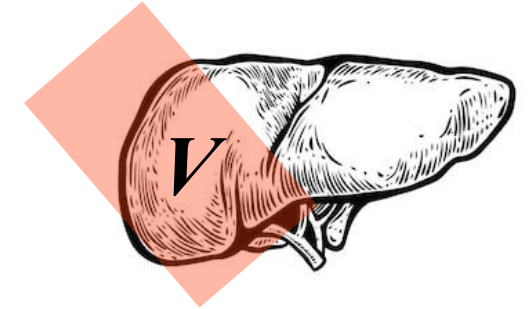


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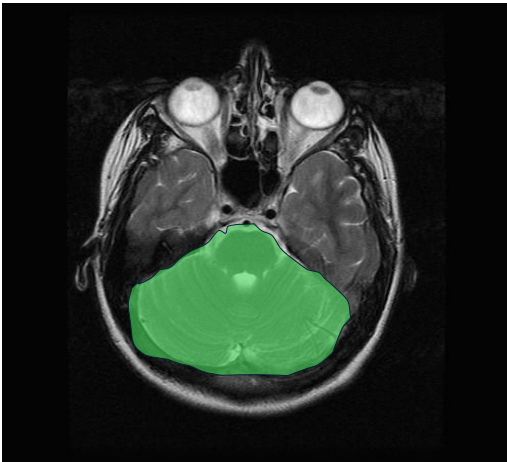


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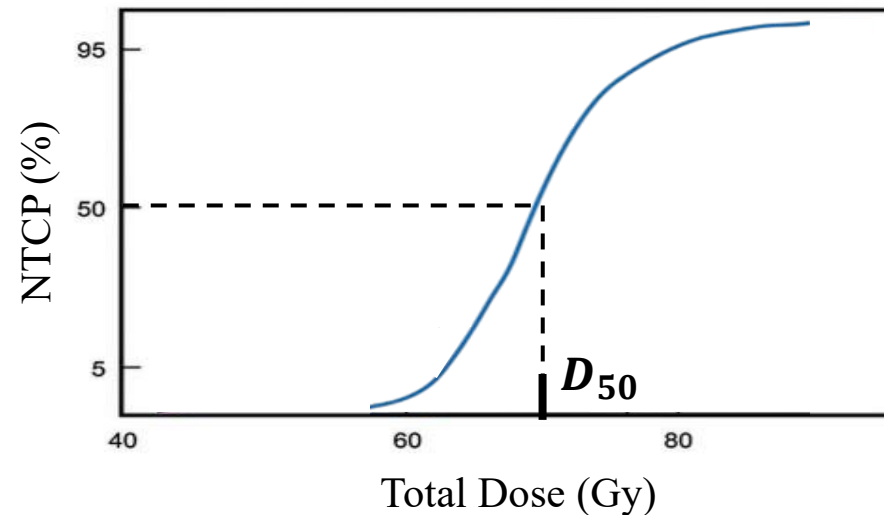
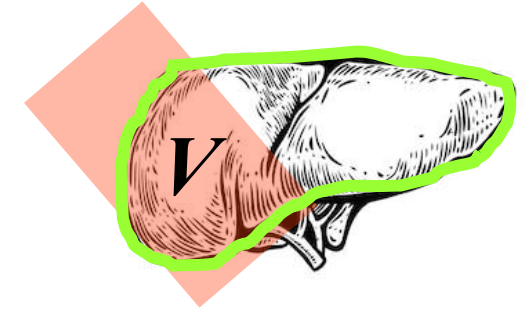


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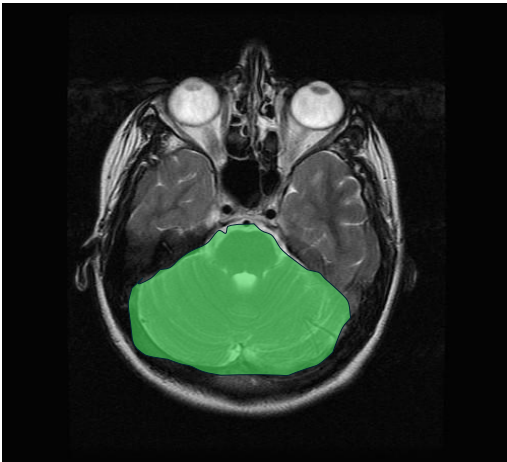


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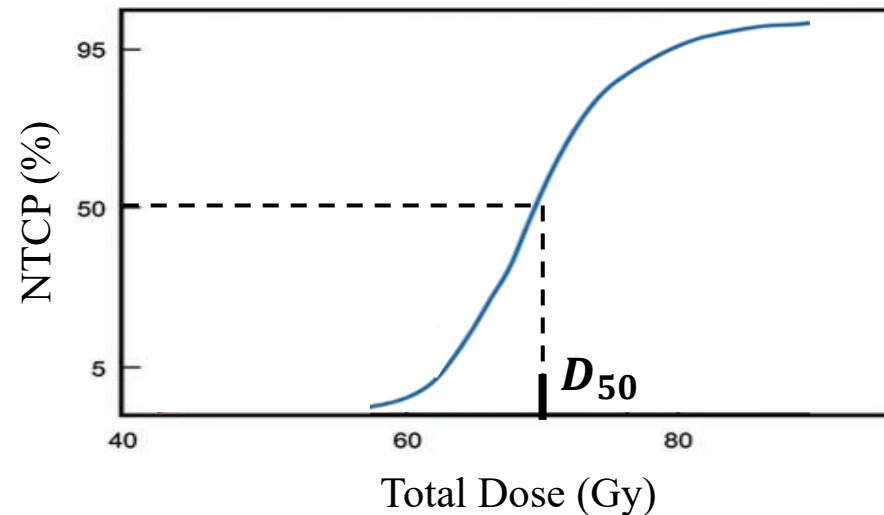
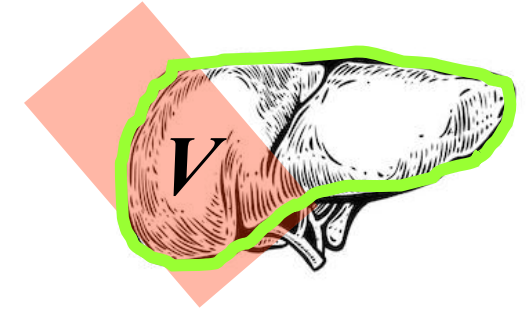


[Image credit: B.V. Prakash et al., Sci Rep 13. (2023), 10.1038/s41598-023-41576-6]



Assumptions:

Power law $D_{50}(V) = \frac{D_{50}(1)}{V^{1/n}}$



[J. T. Lyman, Radiat. Res., 1985]

Lyman – Kutcher - Burman (LKB) model

Phenomenological

$$NTCP(D, V) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^t \exp\left(-\frac{x^2}{2}\right) dx$$

Lyman – Kutcher - Burman (LKB) model

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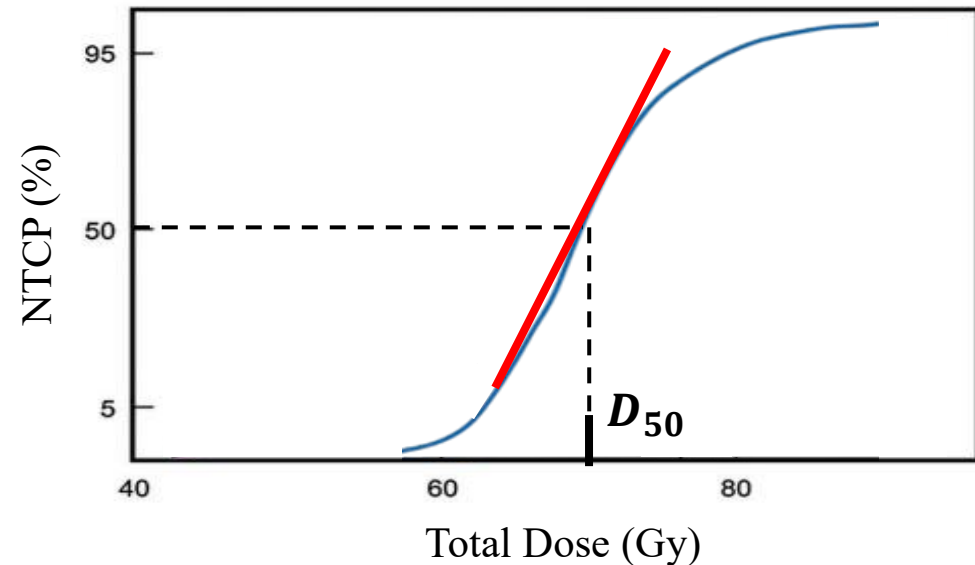
where $t(D, V) = \frac{D - D_{50}(V)}{m D_{50}(V)}$

Lyman – Kutcher - Burman (LKB) model

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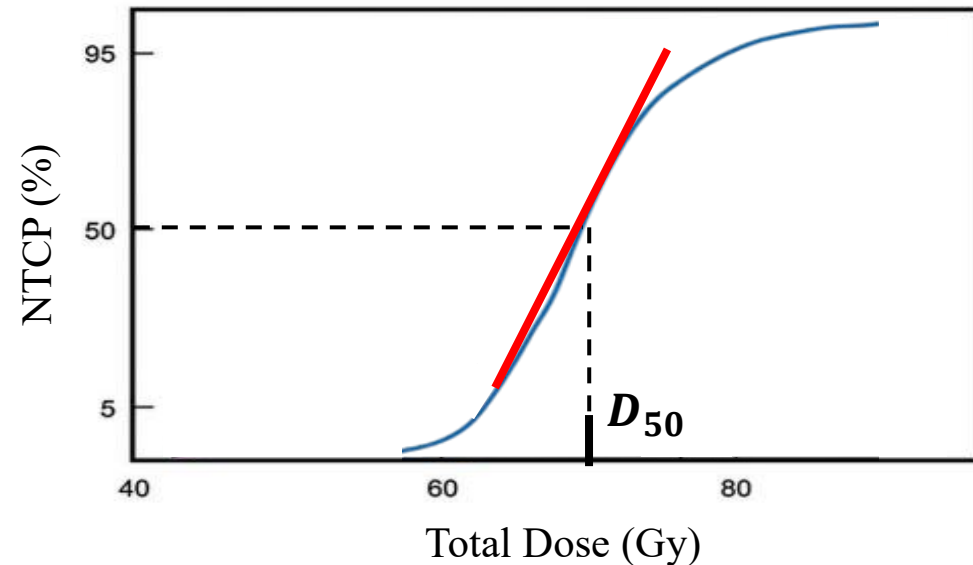


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Lyman – Kutcher - Burman (LKB) model

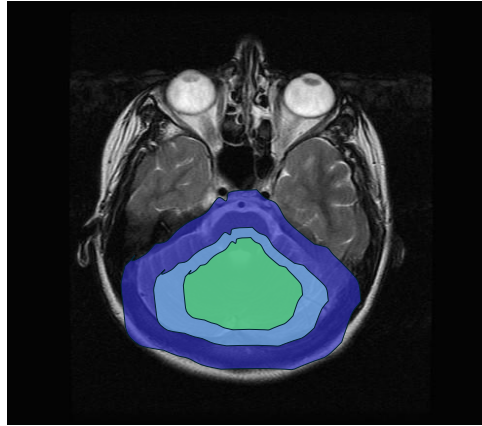
Phenomenological

Lyman – Kutcher - Burman (LKB) model

Phenomenological

NON - uniform dose distribution

Assumption:

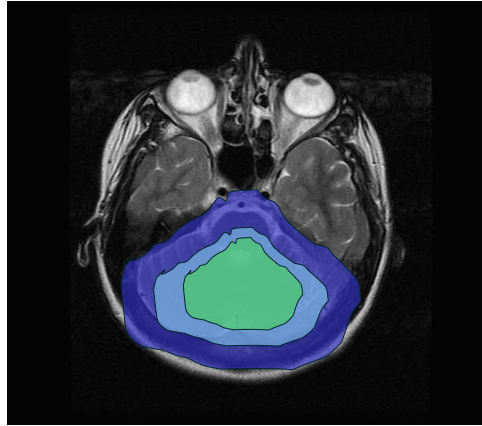


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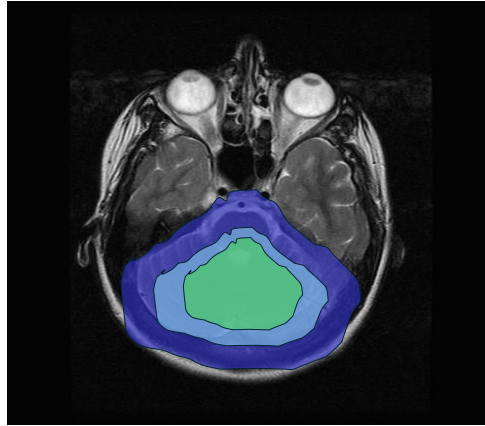
*Lyman
model*

Lyman – Kutcher - Burman (LKB) model

Phenomenological

NON - uniform dose distribution

Assumption:



*Lyman
model*

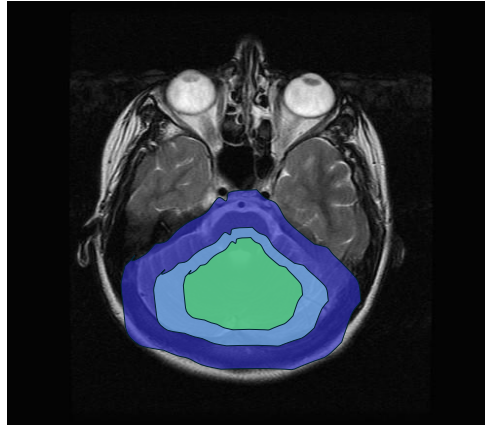
$$t(D_i, v_i) = \frac{EUD - D_{50}(1)}{m D_{50}(1)}$$

Lyman – Kutcher - Burman (LKB) model

Phenomenological

NON - uniform dose distribution

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*Lyman
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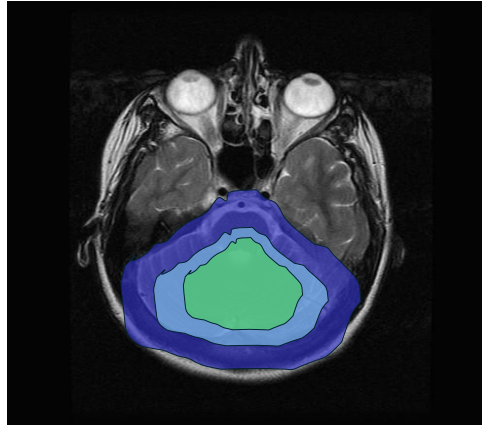
$$EUD = \left(\sum_{i=1}^m v_i D_i^{1/n} \right)^n$$

Lyman – Kutcher - Burman (LKB) model

Phenomenological

NON - uniform dose distribution

Assumption:

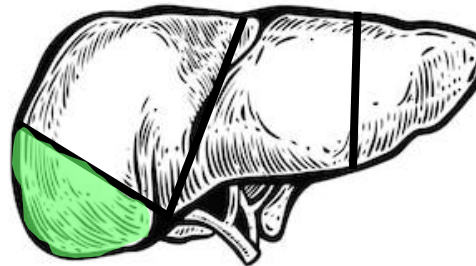


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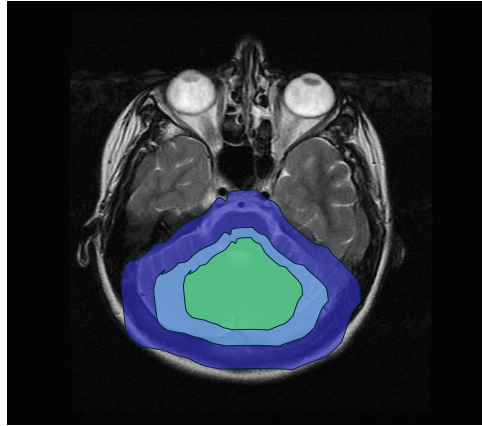


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Phenomenological

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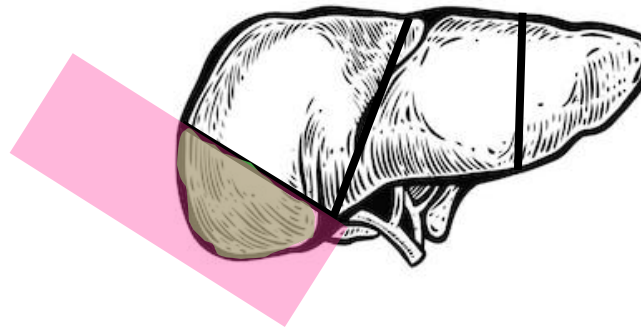


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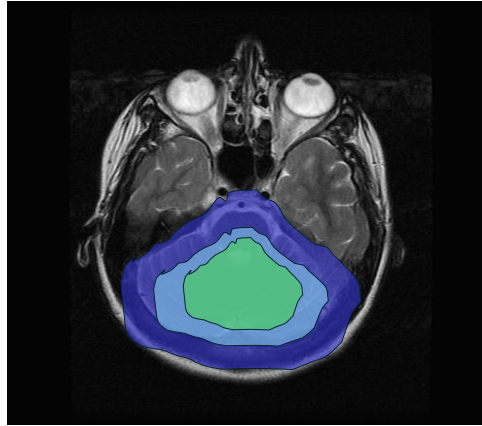


Lyman – Kutcher - Burman (LKB) model

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NON - uniform dose distribution

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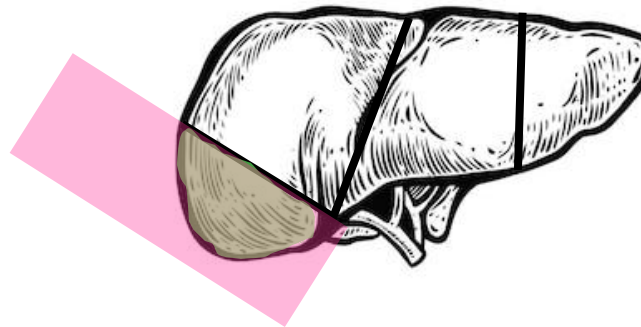


*Lyman
model*

$$t(D_i, v_i) = \frac{\text{EUD} - D_{50}(1)}{m D_{50}(1)}$$



$$\text{EUD} = \left(\sum_{i=1}^m v_i D_i^{1/n} \right)^n$$



Relative Seriality model

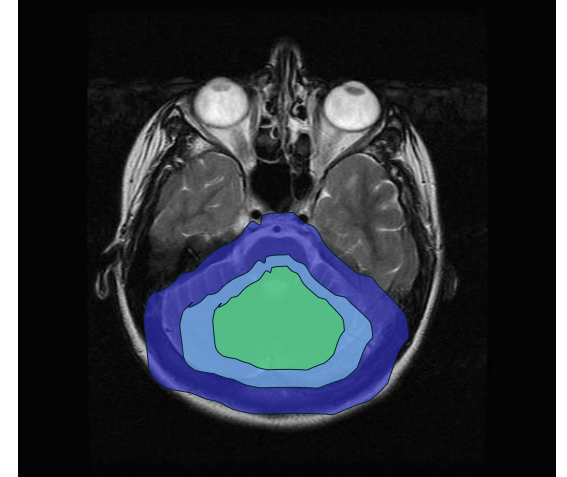
Phenomenological / Mechanistic

Relative Seriality model

Phenomenological / Mechanistic

Assumption:

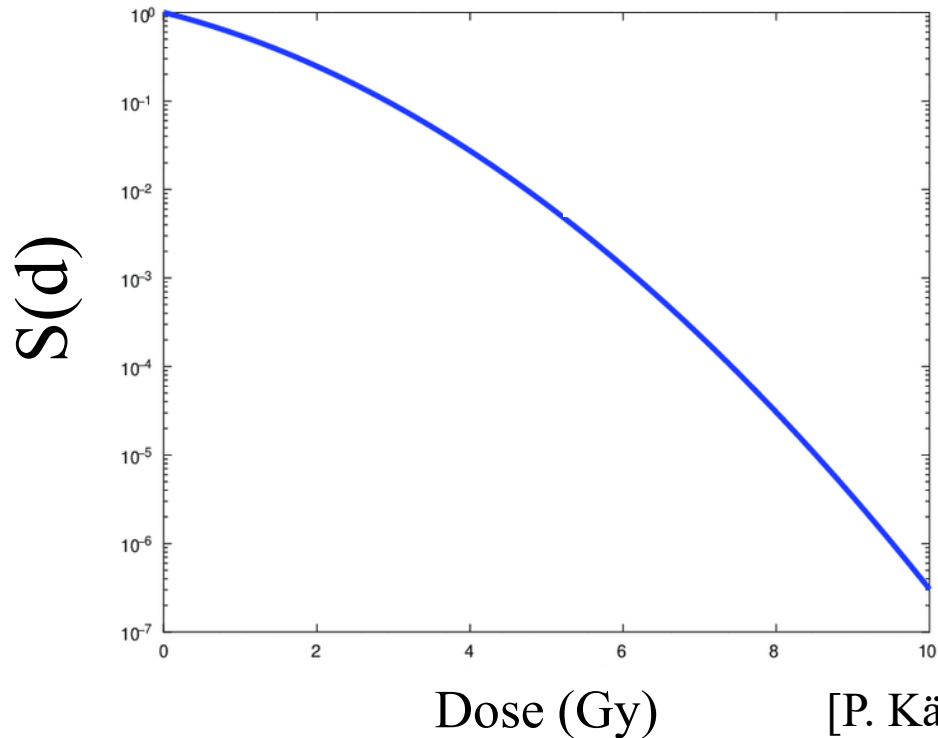
NON - uniform dose distribution



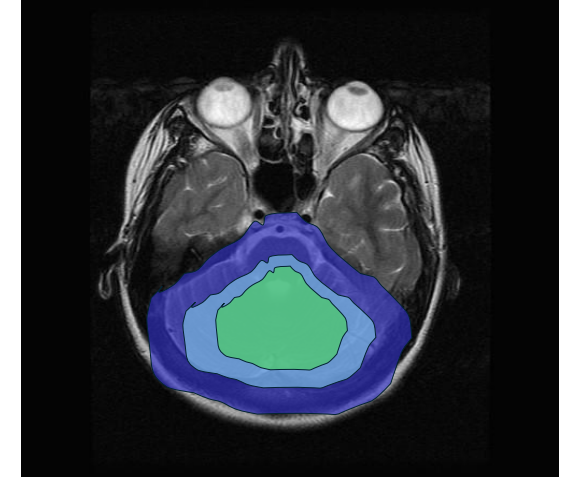
Relative Seriality model

Phenomenological / Mechanistic

Assumption: NON - uniform dose distribution



[P. Källman, Int. J. Radiat. Biol., 1992]



[Image credit: Biorender]

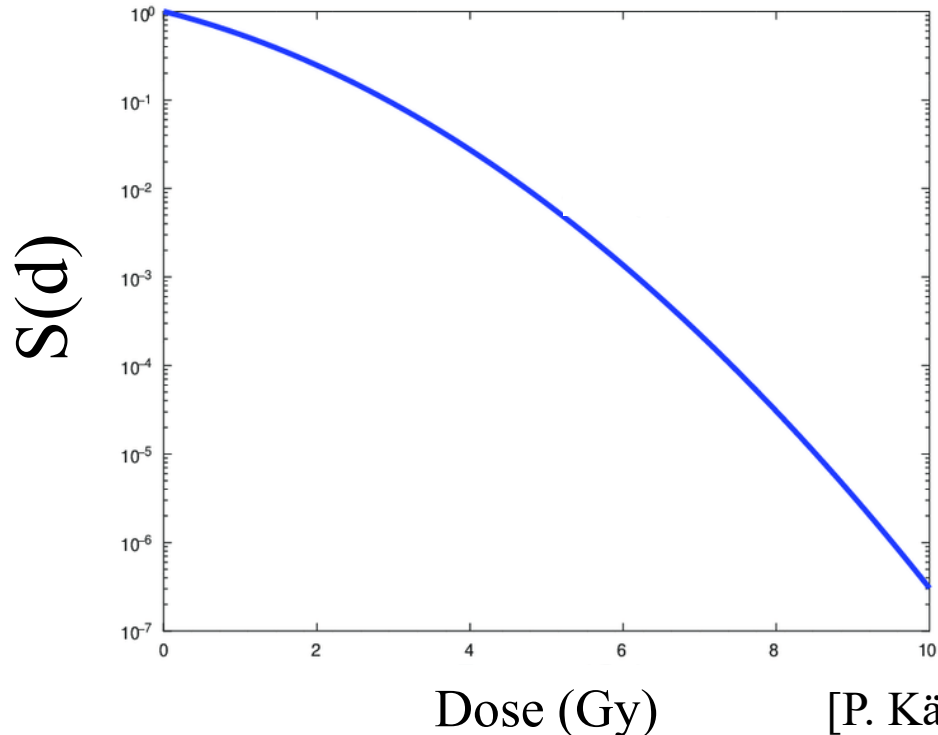
Relative Seriality model

Phenomenological / Mechanistic

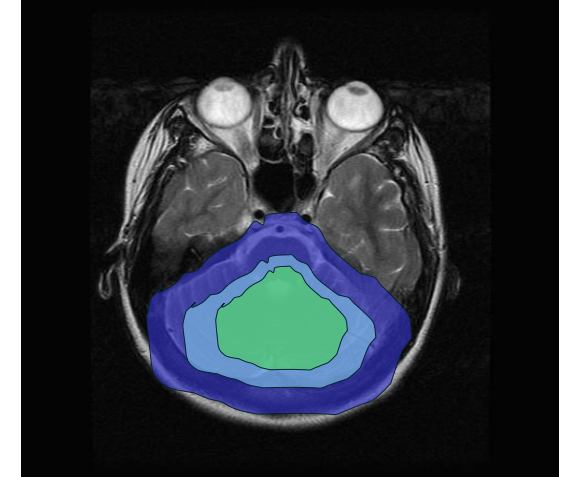
Assumption: NON - uniform dose distribution

Linear – Quadratic (LQ) cell survival model

$$S(d) = e^{-\alpha nd_i - \beta nd_i^2}$$



[P. Källman, Int. J. Radiat. Biol., 1992]



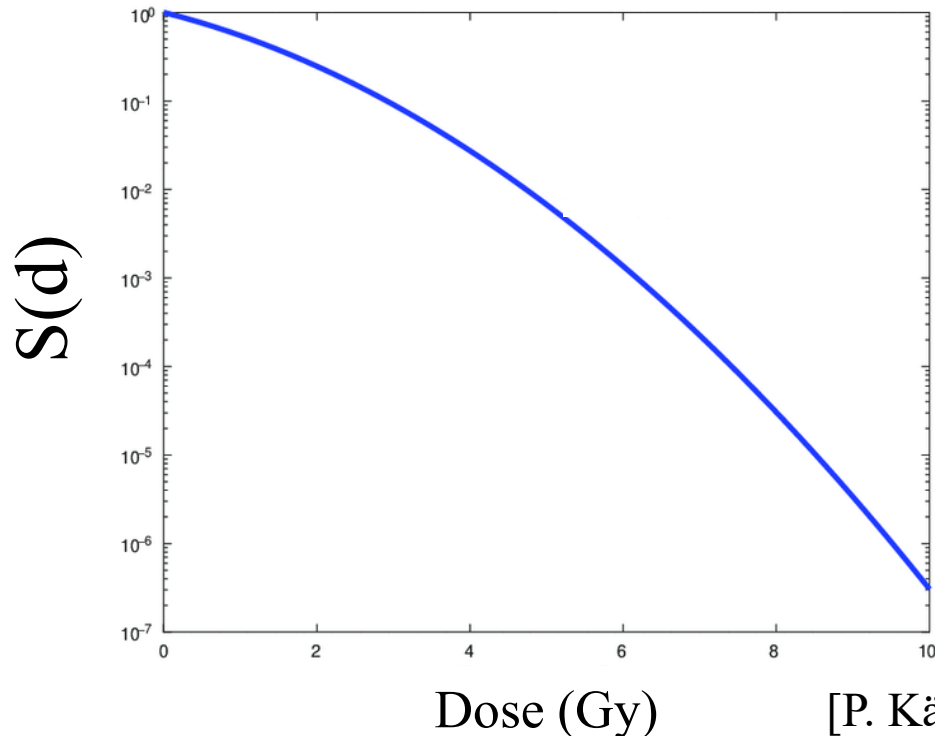
[Image credit: Biorender]

Relative Seriality model

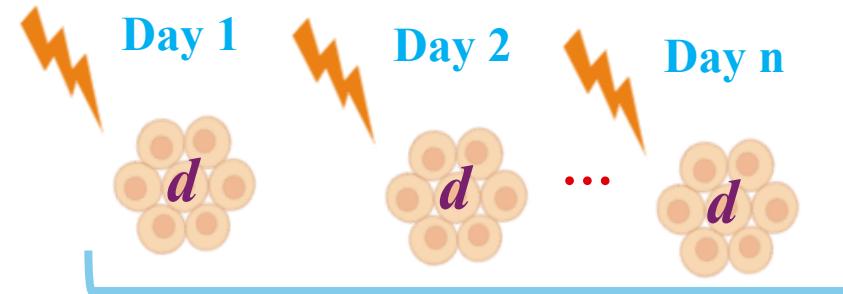
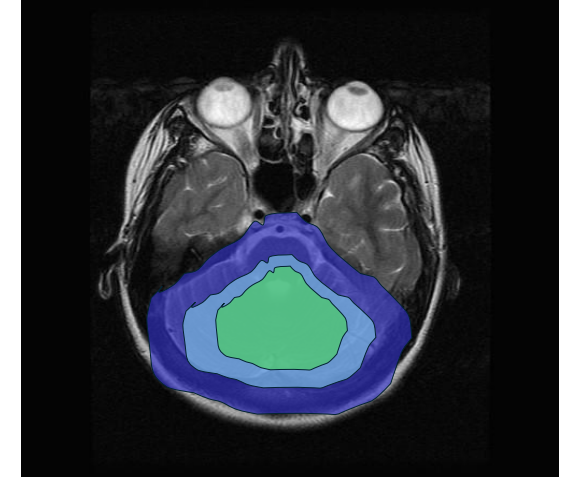
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Linear – Quadratic (LQ) cell survival model



$$S(d) = e^{-\alpha n d_i - \beta n d_i^2}$$

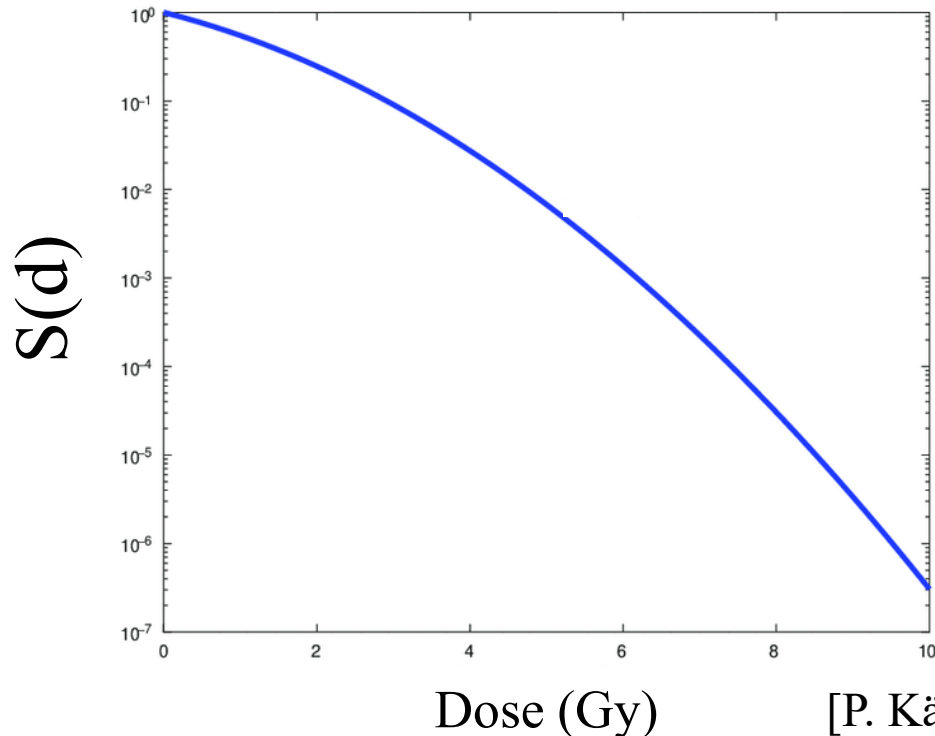


Relative Seriality model

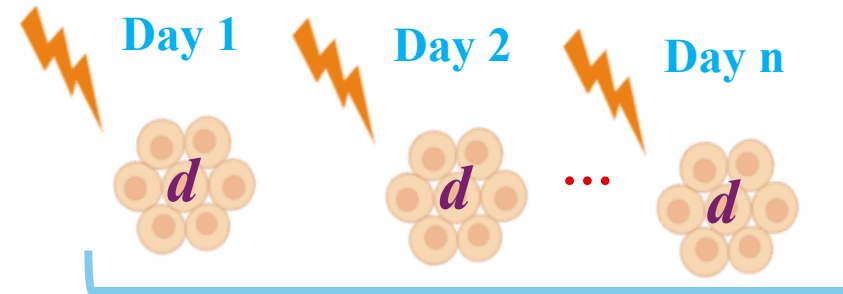
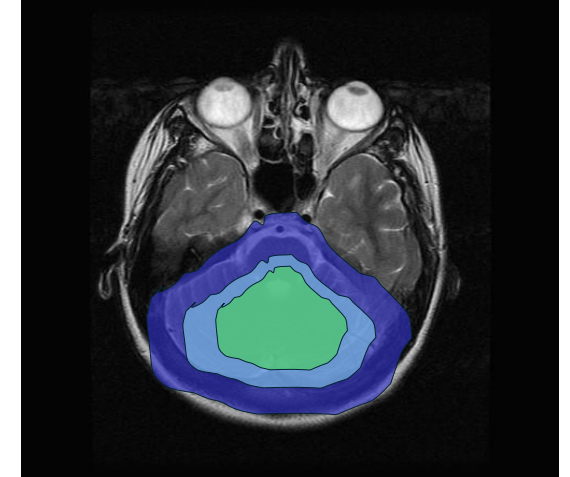
Phenomenological / Mechanistic

Assumption: NON - uniform dose distribution

Linear – Quadratic (LQ) cell survival model



$$S(d) = e^{-\alpha nd_i - \beta nd_i^2}$$

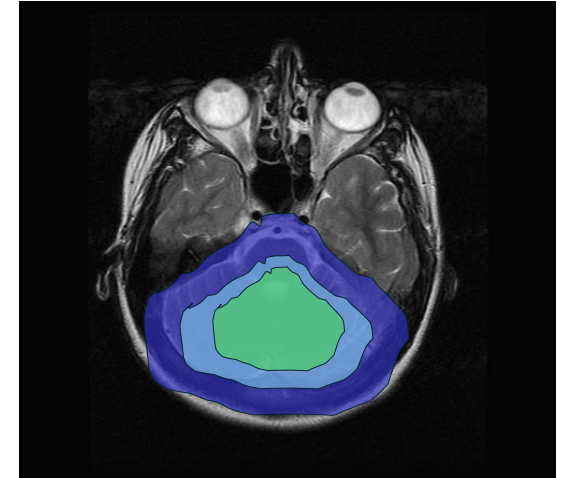


Relative Seriality model

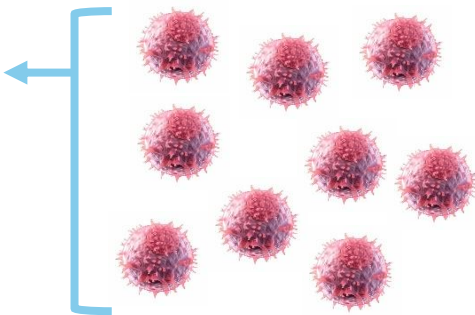
Phenomenological / Mechanistic

Assumption:

NON - uniform dose distribution



1 FSU
=
 $k \text{ cells}$

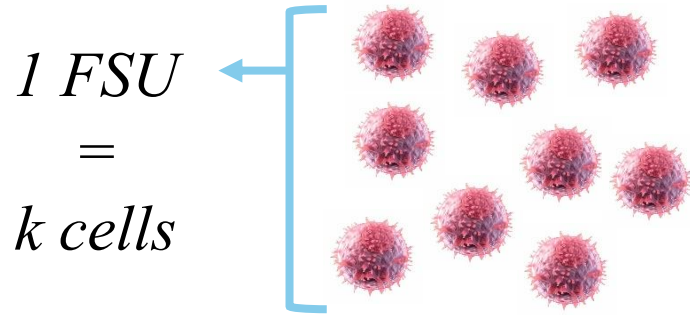
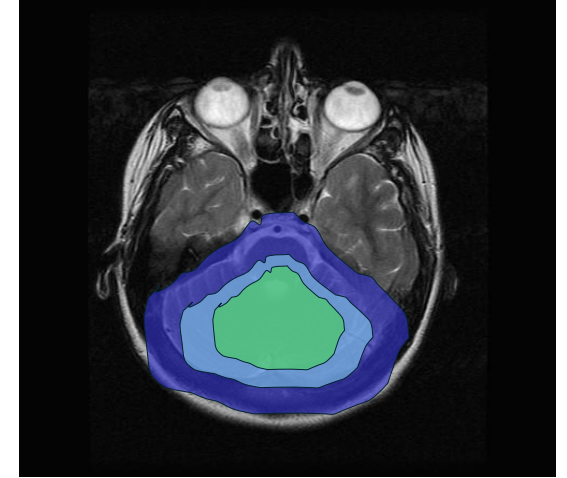
A diagram showing a cluster of approximately ten red, spiky spherical cells, representing tumor cells. A blue bracket is positioned to the left of the cluster, with an arrow pointing from the text '1 FSU = k cells' to the bracket.

Relative Seriality model

Phenomenological / Mechanistic

Assumption:

NON - uniform dose distribution



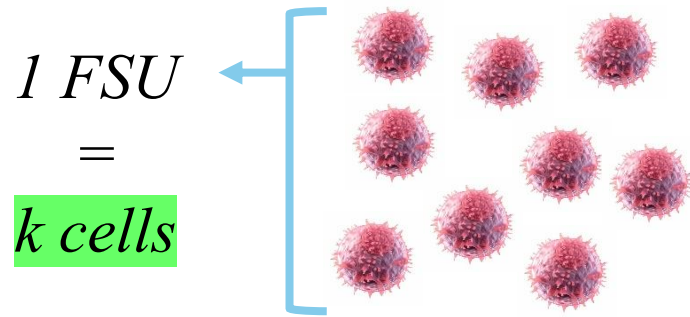
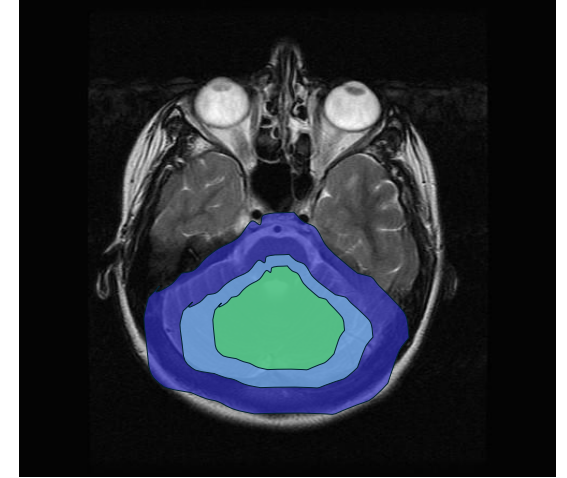
$$P(d_i)_{FSU} = e^{-ke^{-\alpha nd_i - \beta nd_i^2}}$$

Relative Seriality model

Phenomenological / Mechanistic

Assumption:

NON - uniform dose distribution



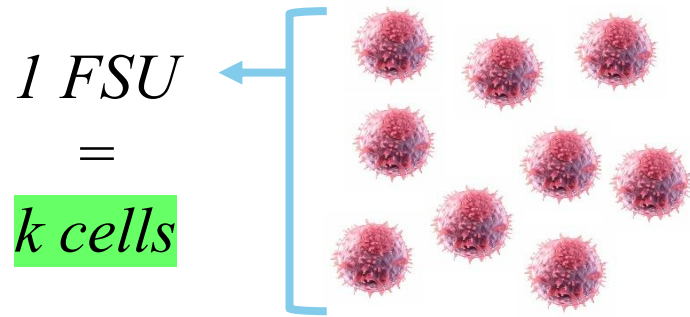
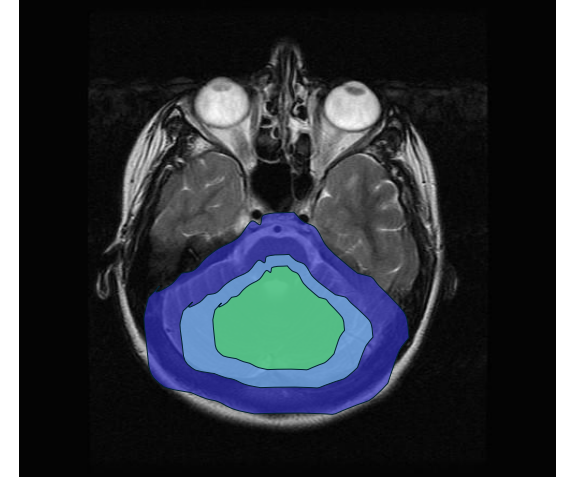
$$P(d_i)_{FSU} = e^{-k} e^{-\alpha n d_i - \beta n d_i^2}$$

Relative Seriality model

Phenomenological / Mechanistic

Assumption:

NON - uniform dose distribution



$$P(d_i)_{FSU} = e^{-k} e^{-\alpha n d_i - \beta n d_i^2}$$

LQ cell
survival model

Relative Seriality model

Phenomenological / Mechanistic

$$(P(d_i)_{FSU})^{\mathbf{s}}$$

Relative Seriality model

Phenomenological / Mechanistic

$$[1 - (P(d_i)_{FSU})^s]$$

Relative Seriality model

Phenomenological / Mechanistic

$$[1 - (P(d_i)_{FSU})^s]^{v_i}$$

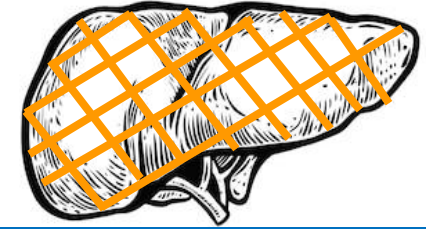
Relative Seriality model

Phenomenological / Mechanistic

$$\begin{aligned} NTCP(d_i, v_i) &= \\ &= \left\{ 1 - \prod_{i=1}^m [1 - (P(d_i)_{FSU})^{\mathbf{s}}]^{v_i} \right\}^{1/s} \end{aligned}$$

Relative Seriality model

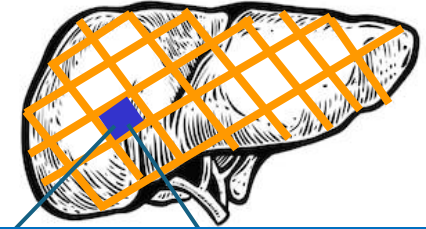
Phenomenological / Mechanistic



$$NTCP(d_i, v_i) = \left\{ 1 - \prod_{i=1}^m \left[1 - \left(e^{-ke^{-\alpha nd_i - \beta nd_i^2}} \right)^s \right]^{v_i} \right\}^{1/s}$$

Relative Seriality model

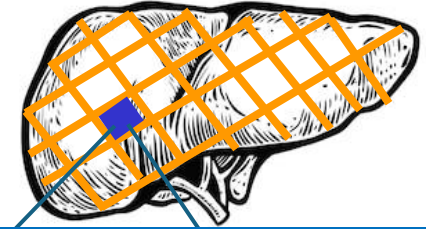
Phenomenological / Mechanistic



$$NTCP(d_i, v_i) = \left\{ 1 - \prod_{i=1}^m \left[1 - \left(e^{-ke^{-\alpha d_i} - \beta n d_i^2} \right)^s \right]^{v_i} \right\}^{1/s}$$

Relative Seriality model

Phenomenological / Mechanistic



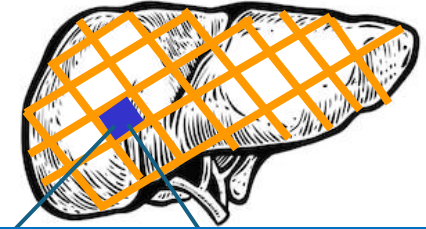
$$NTCP(d_i, v_i) = \left\{ 1 - \prod_{i=1}^m \left[1 - \left(e^{-ke^{-\alpha nd_i} - \beta nd_i^2} \right)^s \right]^{v_i} \right\}^{1/s}$$



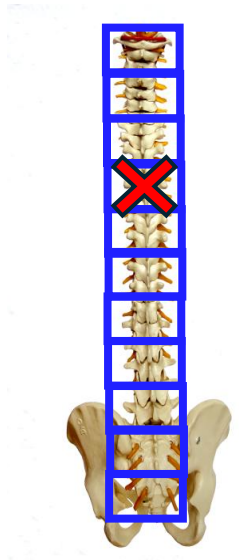
Serial organ

Relative Seriality model

Phenomenological / Mechanistic



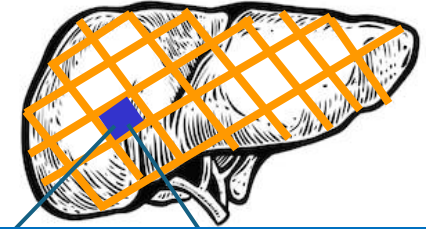
$$NTCP(d_i, v_i) = \left\{ 1 - \prod_{i=1}^m \left[1 - \left(e^{-ke^{-\alpha nd_i} - \beta nd_i^2} \right)^s \right]^{v_i} \right\}^{1/s}$$



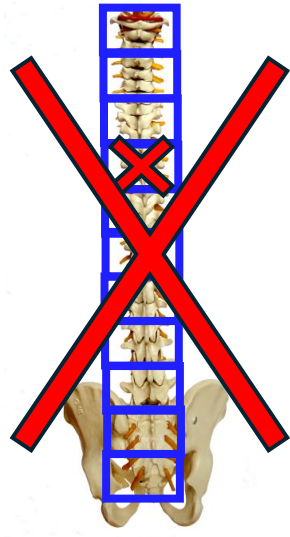
Serial organ

Relative Seriality model

Phenomenological / Mechanistic



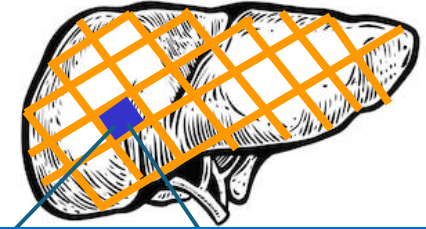
$$NTCP(d_i, v_i) = \left\{ 1 - \prod_{i=1}^m \left[1 - \left(e^{-ke^{-\alpha nd_i - \beta nd_i^2}} \right)^s \right]^{v_i} \right\}^{1/s}$$



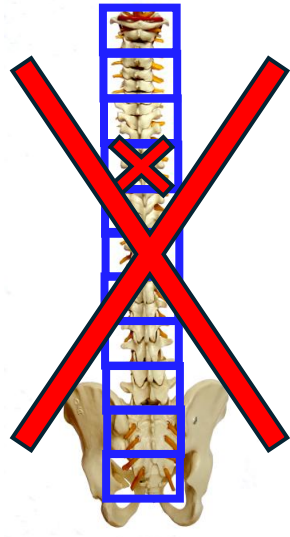
Serial organ

Relative Seriality model

Phenomenological / Mechanistic



$$NTCP(d_i, v_i) = \left\{ 1 - \prod_{i=1}^m \left[1 - \left(e^{-ke^{-\alpha nd_i - \beta nd_i^2}} \right)^s \right]^{v_i} \right\}^{1/s}$$

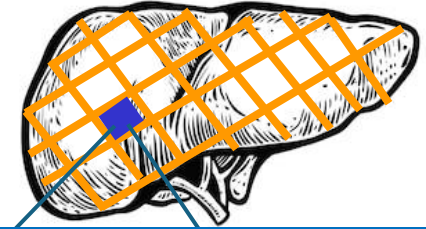


Serial organ

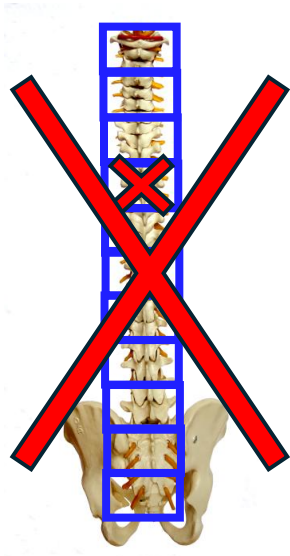
$$S = 1$$

Relative Seriality model

Phenomenological / Mechanistic



$$NTCP(d_i, v_i) = \left\{ 1 - \prod_{i=1}^m \left[1 - \left(e^{-ke^{-\alpha nd_i - \beta nd_i^2}} \right)^s \right]^{v_i} \right\}^{1/s}$$



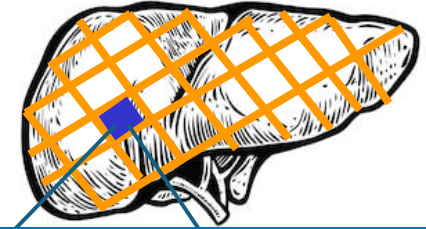
Serial organ

Parallel organ

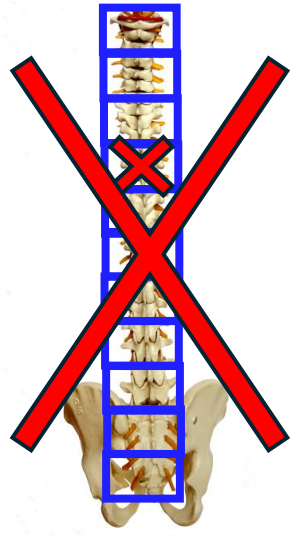
$$S = 1$$

Relative Seriality model

Phenomenological / Mechanistic



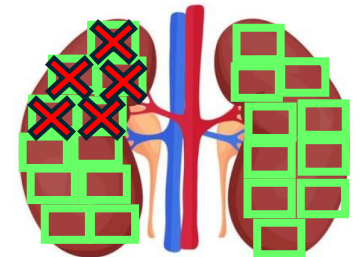
$$NTCP(d_i, v_i) = \left\{ 1 - \prod_{i=1}^m \left[1 - \left(e^{-ke^{-\alpha nd_i - \beta nd_i^2}} \right)^s \right]^{v_i} \right\}^{1/s}$$



Serial organ

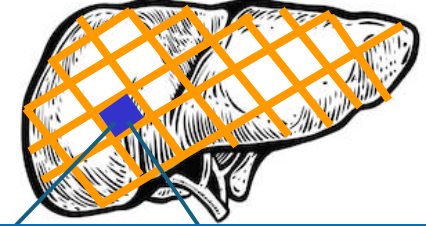
$$S = 1$$

Parallel organ

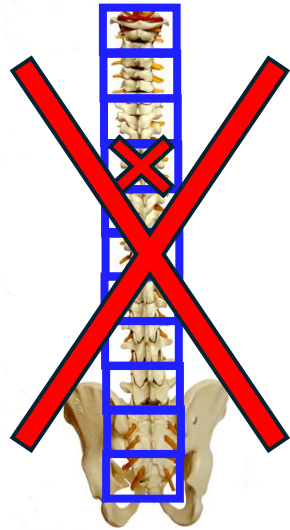


Relative Seriality model

Phenomenological / Mechanistic



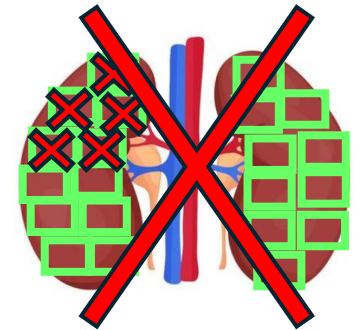
$$NTCP(d_i, v_i) = \left\{ 1 - \prod_{i=1}^m \left[1 - \left(e^{-ke^{-\alpha nd_i - \beta nd_i^2}} \right)^s \right]^{v_i} \right\}^{1/s}$$



Serial organ

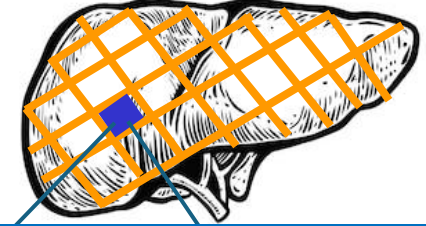
$$S = 1$$

Parallel organ

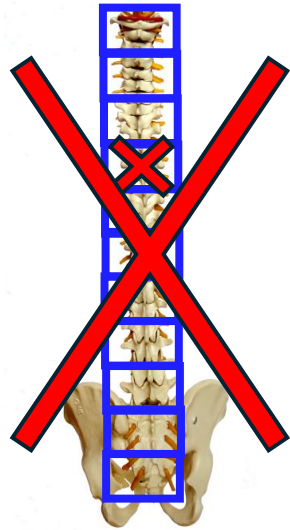


Relative Seriality model

Phenomenological / Mechanistic



$$NTCP(d_i, v_i) = \left\{ 1 - \prod_{i=1}^m \left[1 - \left(e^{-ke^{-\alpha nd_i - \beta nd_i^2}} \right)^s \right]^{v_i} \right\}^{1/s}$$

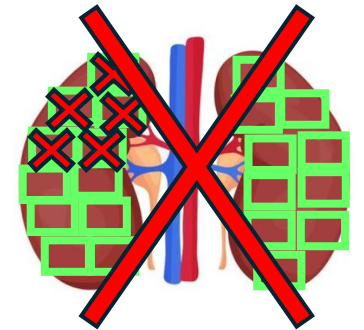


Serial organ

$$S = 1$$

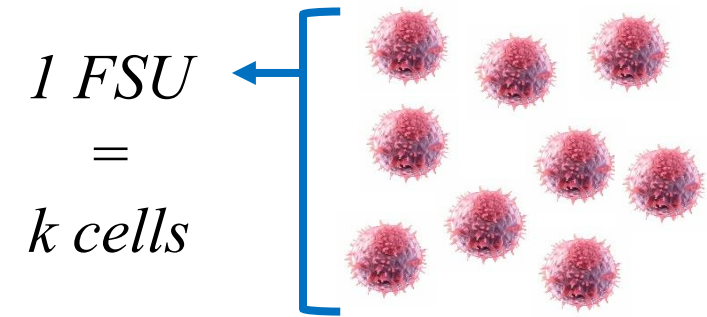
Parallel organ

$$S \rightarrow 0$$



Critical Volume model

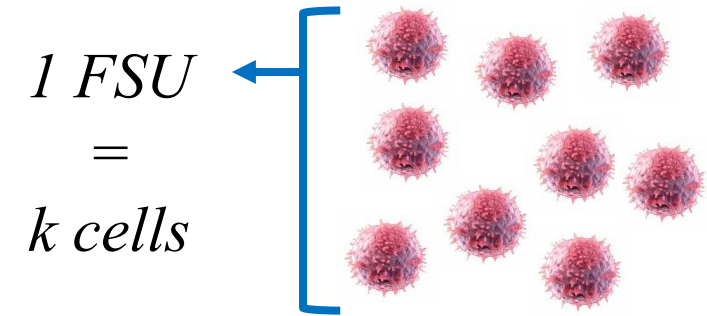
Mechanistic



Critical Volume model

Mechanistic

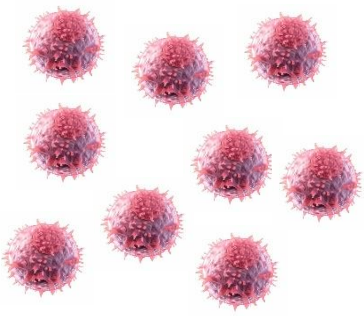
$$P_{FSU} = (1 - e^{-\alpha nd - \beta nd^2})^k$$



Critical Volume model

Mechanistic

$$P_{FSU} = (1 - \overbrace{e^{-\alpha nd - \beta nd^2}}^{\text{LQ cell survival model}})^k$$

$$1 \text{ FSU} = k \text{ cells}$$


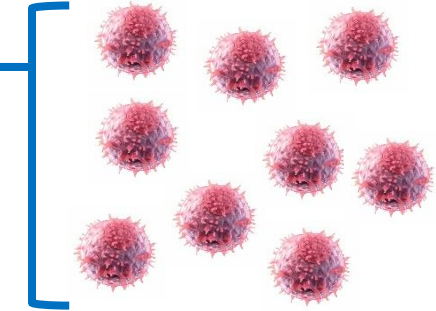
Critical Volume model

Mechanistic

LQ cell
survival model

$$P_{FSU} = (1 - e^{-\alpha nd - \beta nd^2})^k$$

1 FSU
=
k cells



$$NTCP = \sum_{t=M}^N \binom{N}{t} P_{FSU}^t (1 - P_{FSU})^{N-t}$$

Binomial cumulative
probability

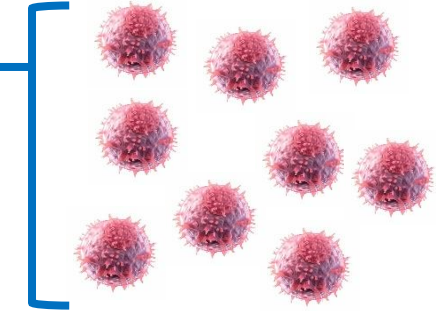
Critical Volume model

Mechanistic

LQ cell
survival model

$$P_{FSU} = (1 - e^{-\alpha nd - \beta nd^2})^k$$

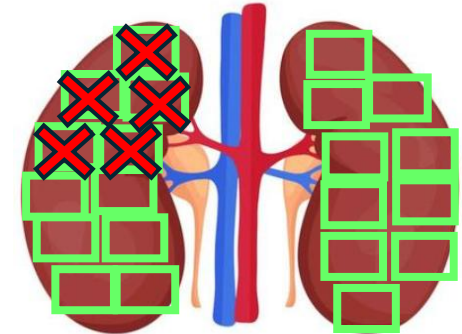
1 FSU
=
k cells



$$NTCP = \sum_{t=M}^N \binom{N}{t} P_{FSU}^t (1 - P_{FSU})^{N-t}$$

Binomial cumulative
probability

Parallel organs



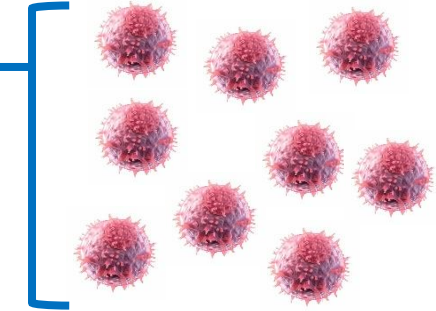
Critical Volume model

Mechanistic

LQ cell
survival model

$$P_{FSU} = (1 - e^{-\alpha nd - \beta nd^2})^k$$

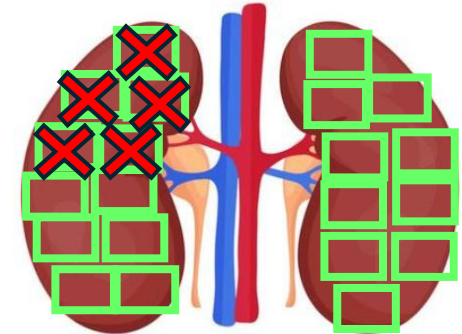
1 FSU
=
k cells



$$NTCP = \sum_{t=M}^N \binom{N}{t} P_{FSU}^t (1 - P_{FSU})^{N-t}$$

Binomial cumulative
probability

Parallel organs

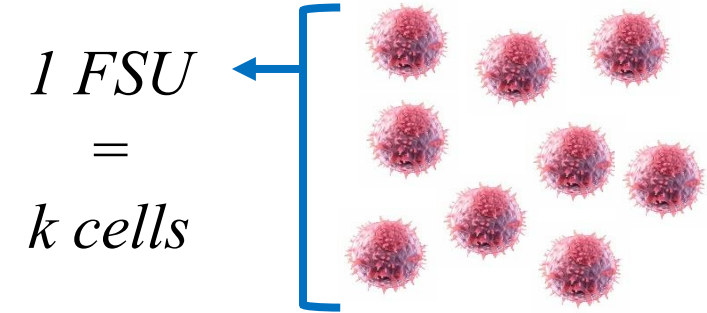


Critical Volume model

Mechanistic

$$P_{FSU} = (1 - e^{-\alpha nd - \beta nd^2})^k$$

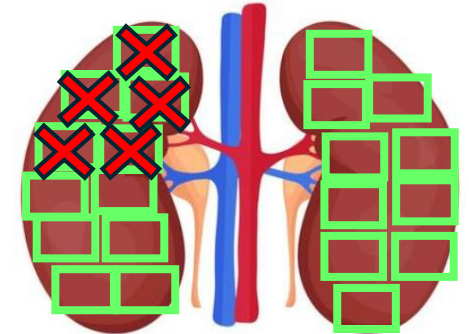
LQ cell survival model



$$NTCP = \sum_{t=M}^N \binom{N}{t} P_{FSU}^t (1 - P_{FSU})^{N-t}$$

Binomial cumulative probability

Parallel organs

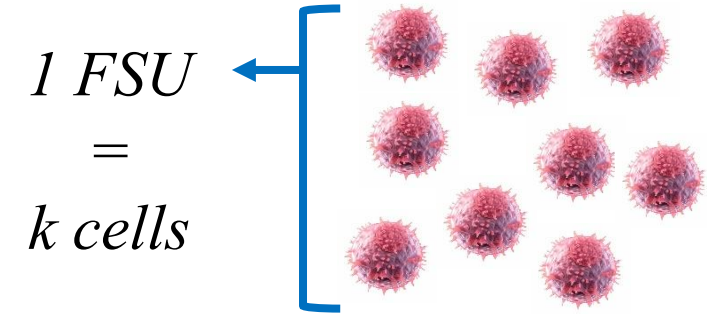


Critical Volume model

Mechanistic

$$P_{FSU} = (1 - e^{-\alpha nd - \beta nd^2})^k$$

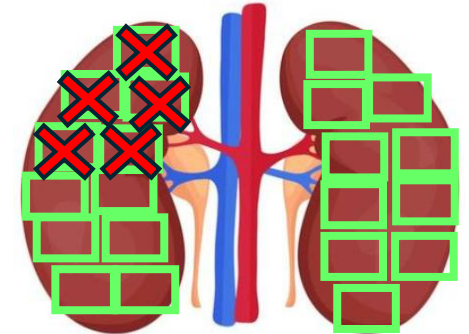
LQ cell
survival model



$$NTCP = \sum_{t=M}^N \binom{N}{t} P_{FSU}^t (1 - P_{FSU})^{N-t}$$

Binomial cumulative
probability

Parallel organs

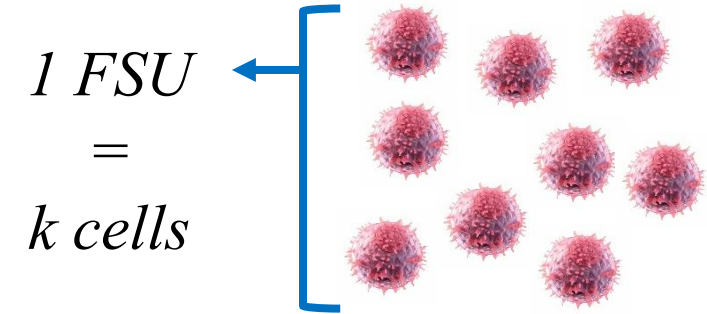


Critical Volume model

Mechanistic

$$P_{FSU} = (1 - e^{-\alpha nd - \beta nd^2})^k$$

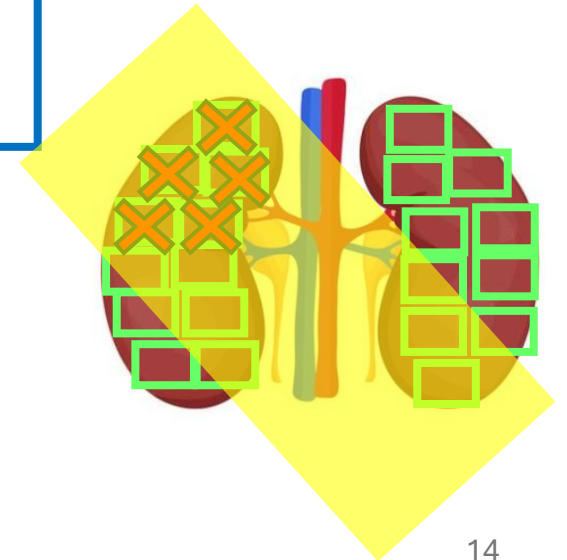
LQ cell
survival model



$$NTCP = \sum_{t=M}^N \binom{N}{t} P_{FSU}^t (1 - P_{FSU})^{N-t}$$

Binomial cumulative
probability

Parallel organs



Critical Element model

Mechanistic

$$NTCP = \sum_{t=M}^N \binom{N}{t} P_{FSU}^t (1 - P_{FSU})^{N-t}$$

Critical Volume Model

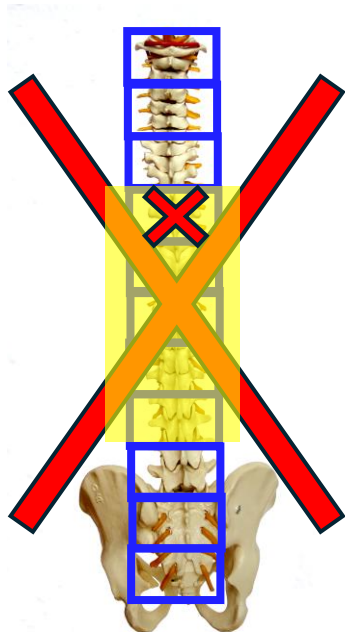
Critical Element model

Mechanistic

$$NTCP = \sum_{t=M}^N \binom{N}{t} P_{FSU}^t (1 - P_{FSU})^{N-t}$$

*Critical Volume
Model*

Serial organs



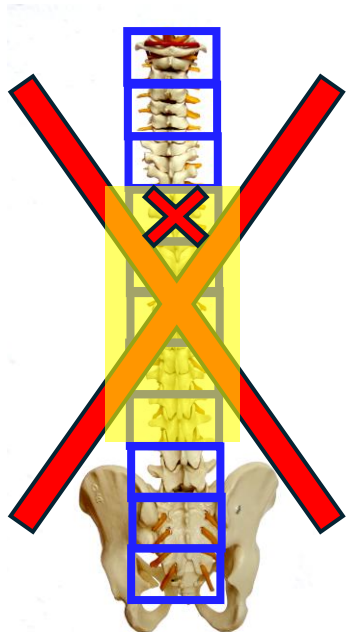
$$M = 1$$

Critical Element model

Mechanistic

$$NTCP = \sum_{t=M}^N \binom{N}{t} P_{FSU}^t (1 - P_{FSU})^{N-t} \quad \text{Critical Volume Model}$$

Serial organs



$$M = 1$$



$$NTCP = 1 - P_0 = 1 - (1 - P_{FSU})^N$$

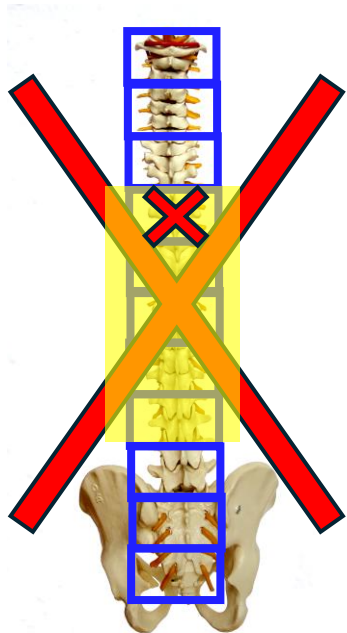
$$P_{FSU} = (1 - e^{-\alpha nd} - \beta nd^2)^k$$

Critical Element model

Mechanistic

$$NTCP = \sum_{t=M}^N \binom{N}{t} P_{FSU}^t (1 - P_{FSU})^{N-t} \quad \text{Critical Volume Model}$$

Serial organs



$$M = 1$$



$$NTCP = 1 - P_0 = 1 - (1 - P_{FSU})^N$$

$$P_{FSU} = (1 - e^{-\alpha nd - \beta nd^2})^k$$

Open Problems

Mechanistic

- ✓ Parameters with physical and biological meanings
- ✓ Predictions
- ✗ Optimal parameters?

Open Problems

How to estimate the model parameters to make predictions?

Mechanistic

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Open Problems

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Open Problems

How to estimate the model parameters to make predictions?



Mechanistic

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- ✓ Predictions

✗ Optimal parameters?



[Image credit: Biorender]

Open Problems

How to estimate the model parameters to make predictions?



cells in 1 FSU
= 100 ???



Mechanistic

- ✓ Parameters with physical and biological meanings
- ✓ Predictions

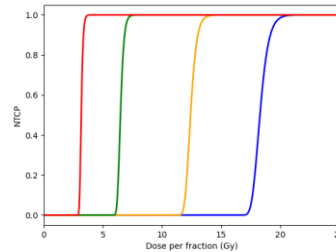
✗ Optimal parameters?

Aim PhD Project

Development of a **novel approach** to estimate
the **parameters** to **predict NTCP** curves
following **Hadrontherapy**

Aim PhD Project

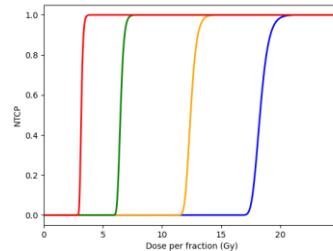
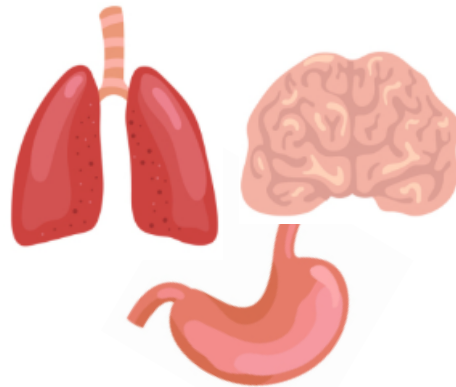
Development of a **novel approach** to estimate the **parameters** to **predict NTCP** curves following **Hadrontherapy**



Aim PhD Project

Development of a **novel approach** to estimate the **parameters** to **predict NTCP** curves following **Hadrontherapy**

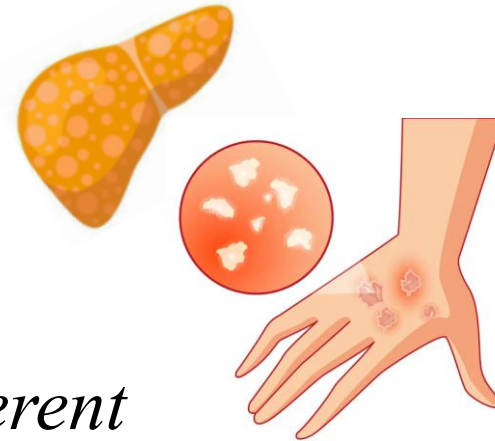
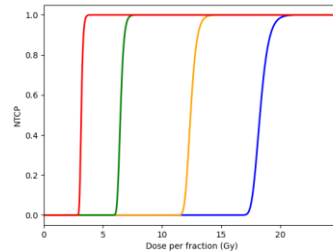
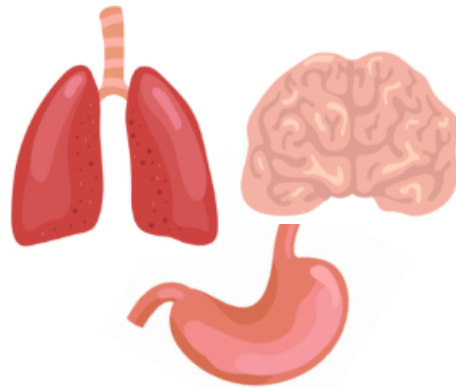
Several organs



Aim PhD Project

Development of a **novel approach** to estimate the **parameters** to **predict NTCP** curves following **Hadrontherapy**

Several organs



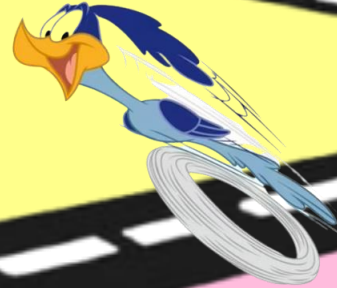
Different endpoints

LITERATURE

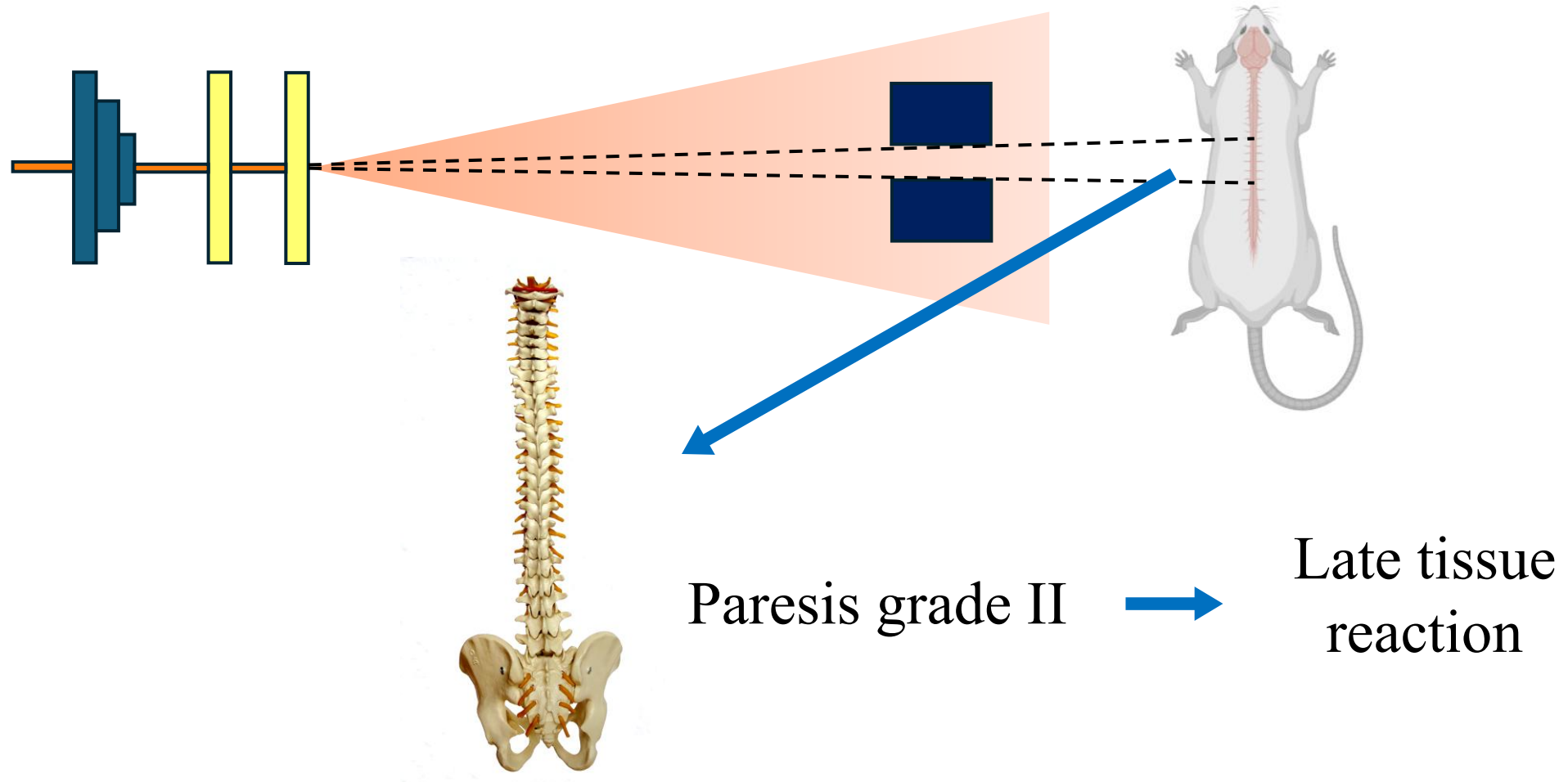
Existing
NTCP
models

Our
approach for
NTCP models

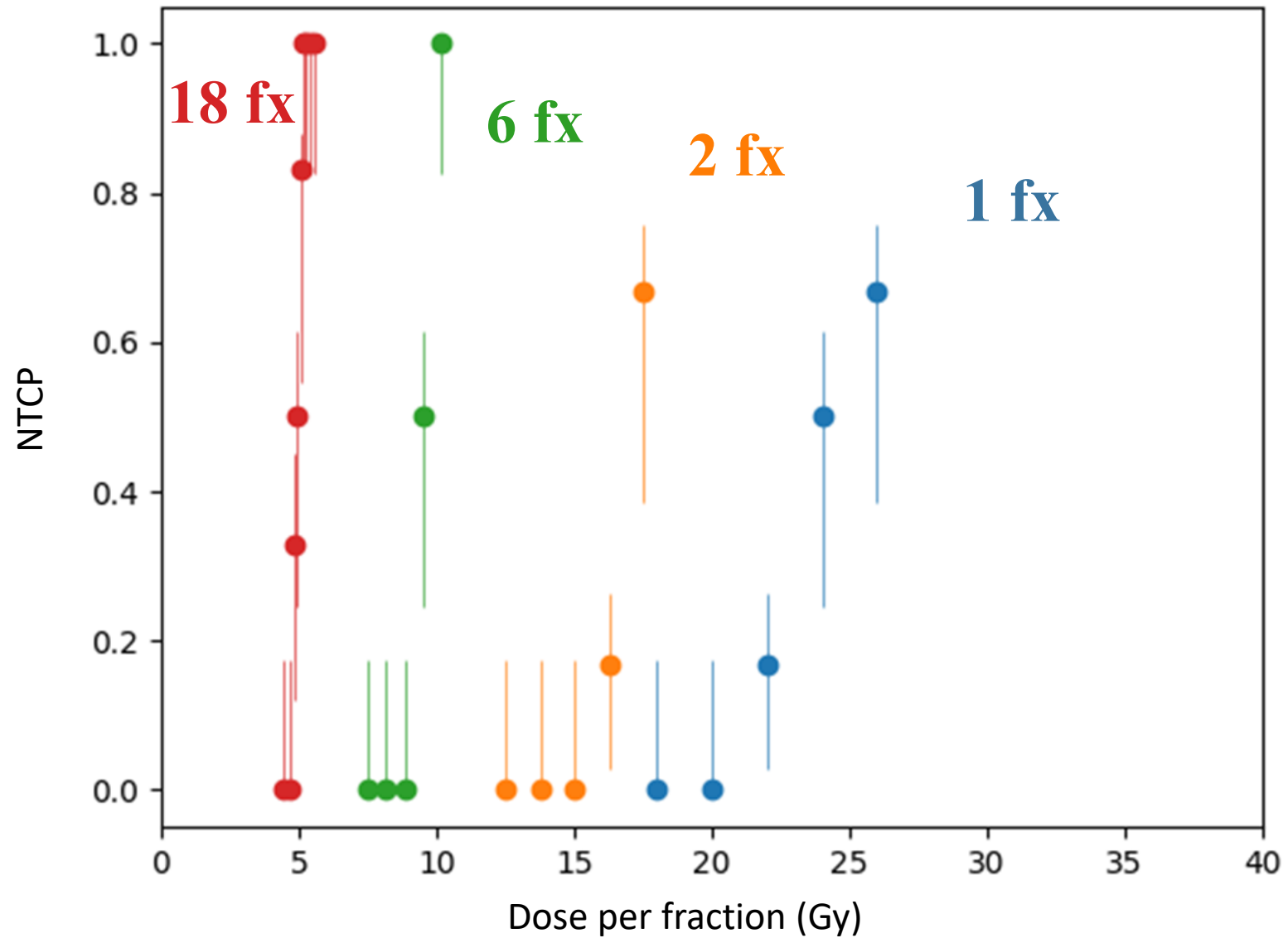
INNOVATION



Experimental Data



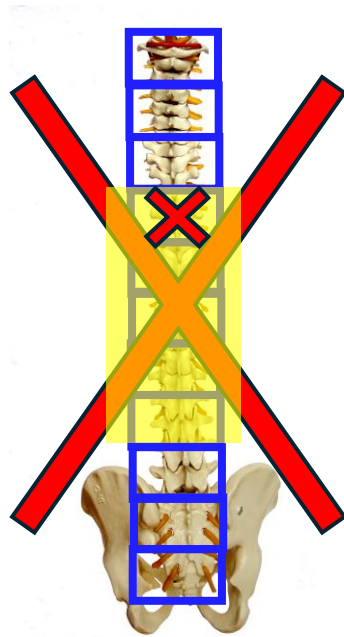
Experimental photon data



Critical Element model

Mechanistic

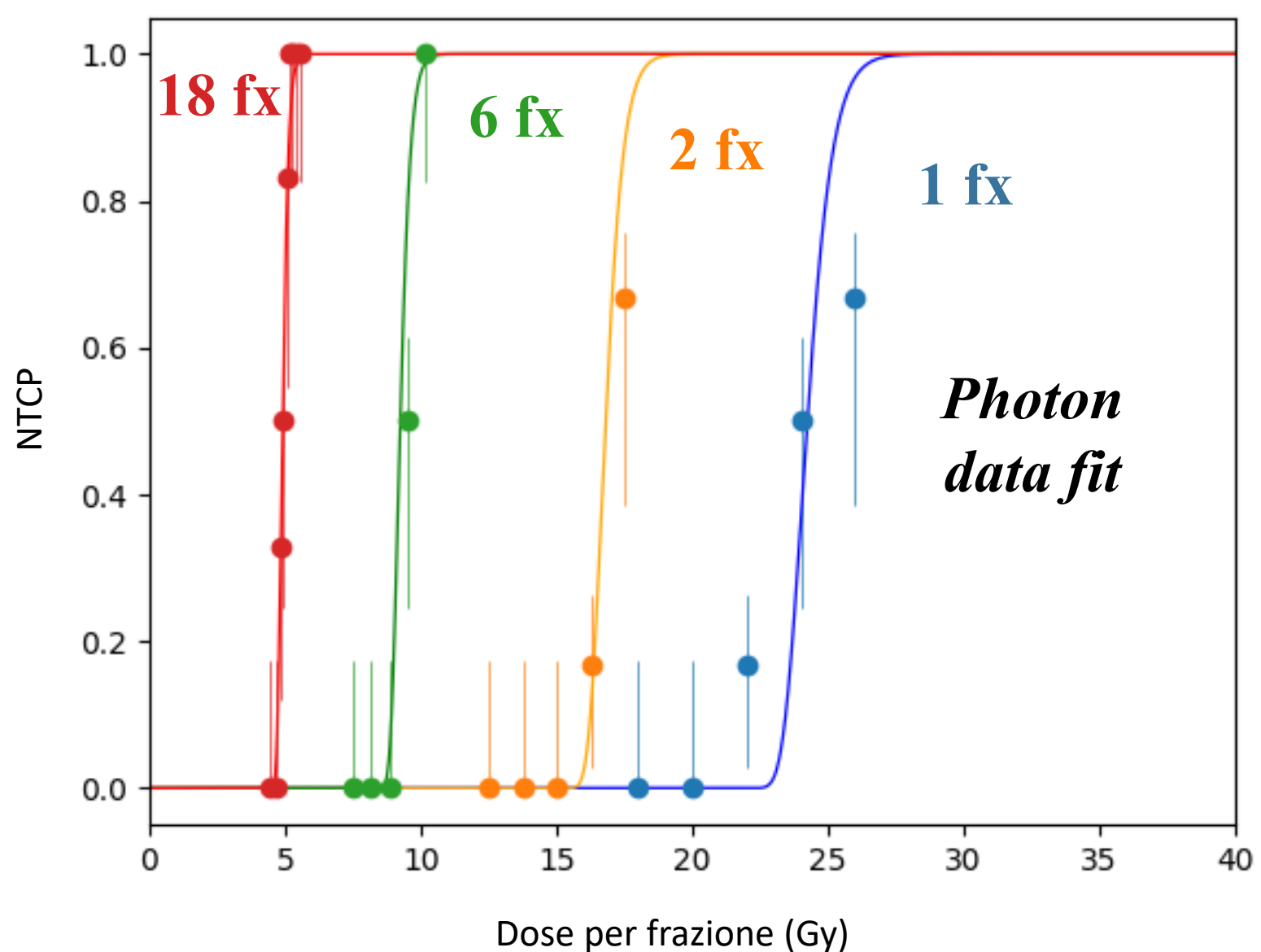
Serial organ



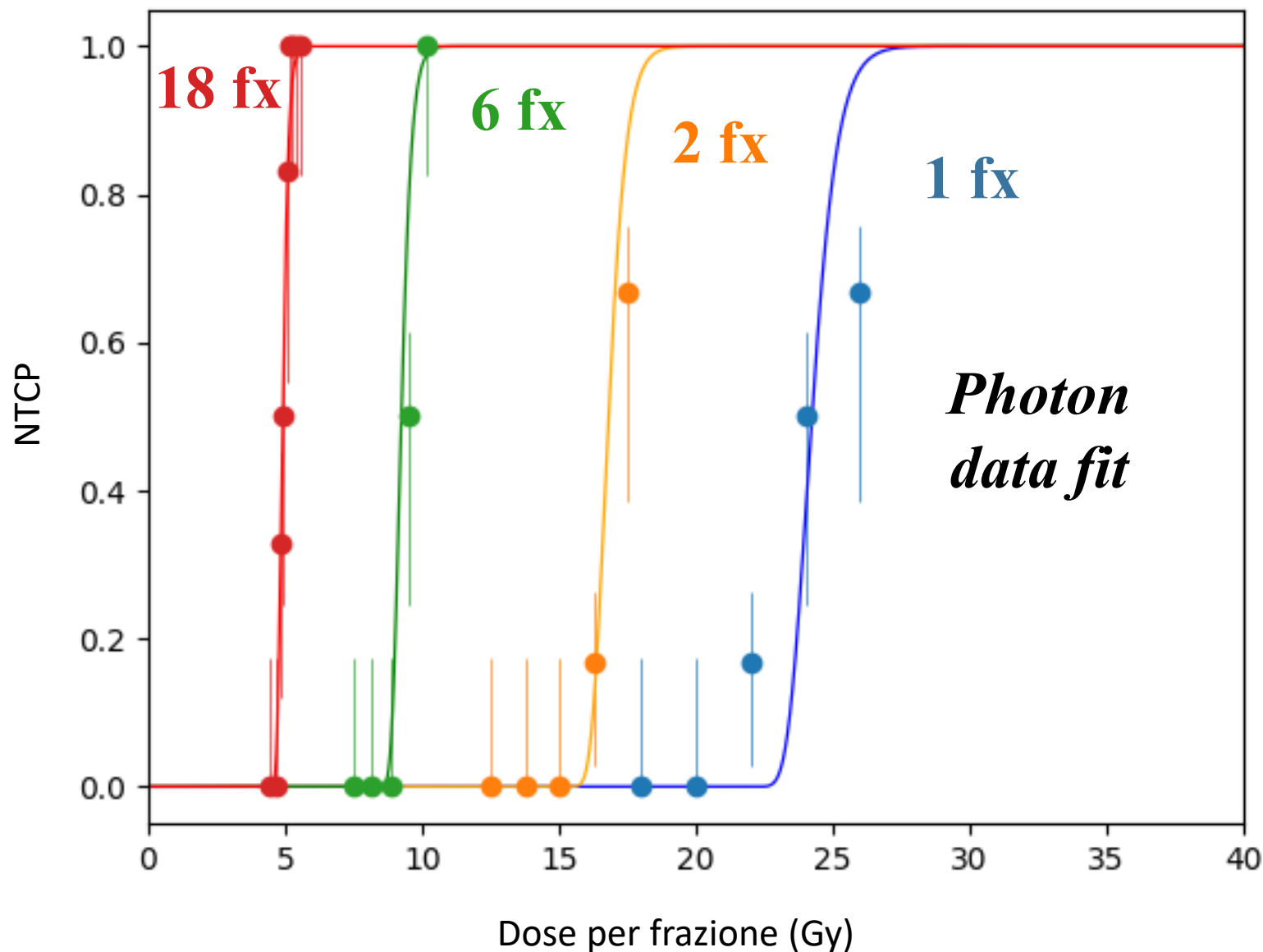
$$\text{NTCP} = 1 - P_0 = 1 - (1 - P_{FSU})^N$$

$$P_{FSU} = (1 - e^{-\alpha nd - \beta nd^2})^k$$

Parameter estimation for ion NTCP predictions



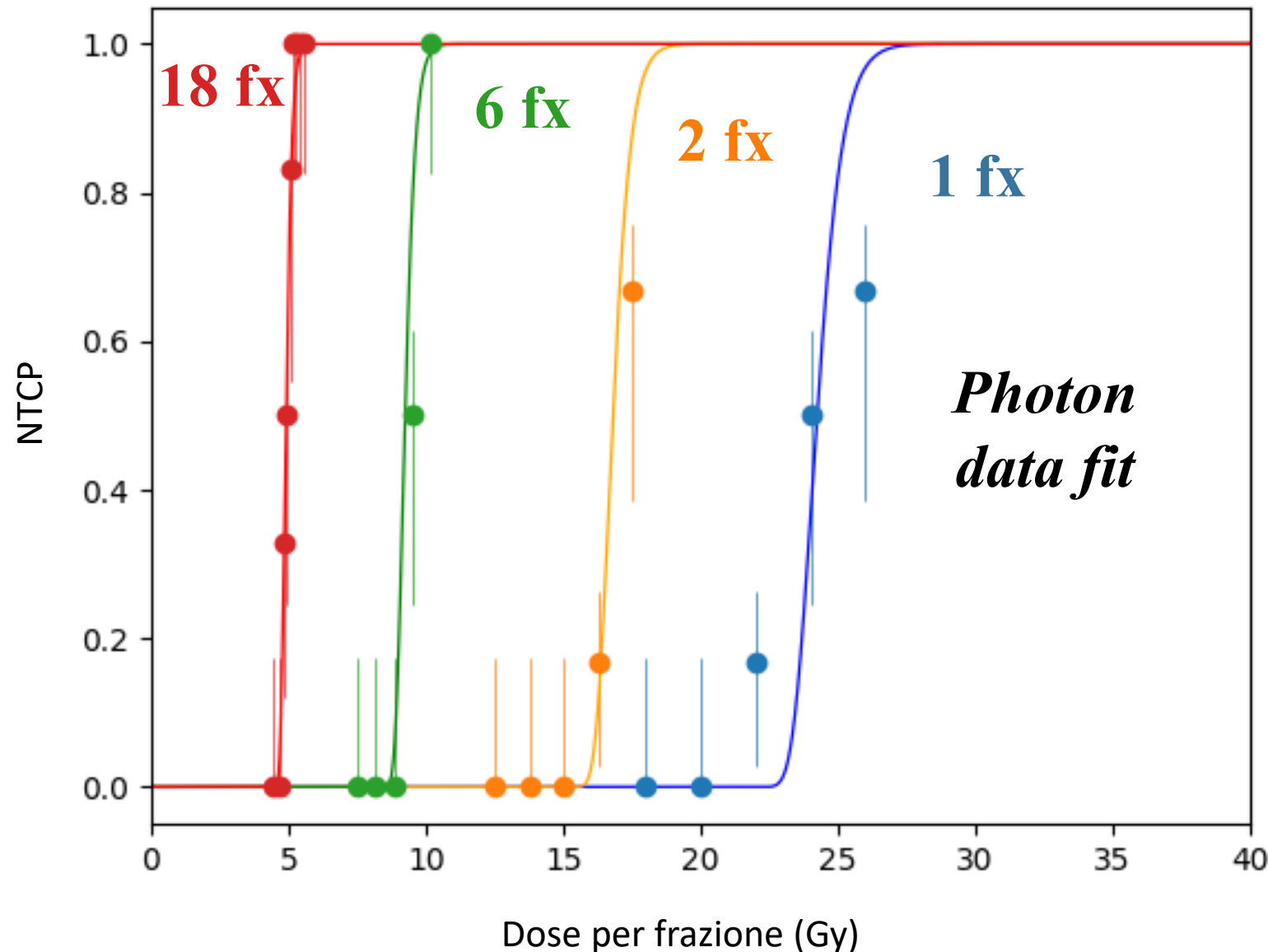
[A. Casali et al., Phys. Med. Biol., 2024]



[A. Casali et al., Phys. Med. Biol., 2024]

Photon **k, N** fixed
for ion NTCP
predictions

Parameter estimation for ion NTCP predictions



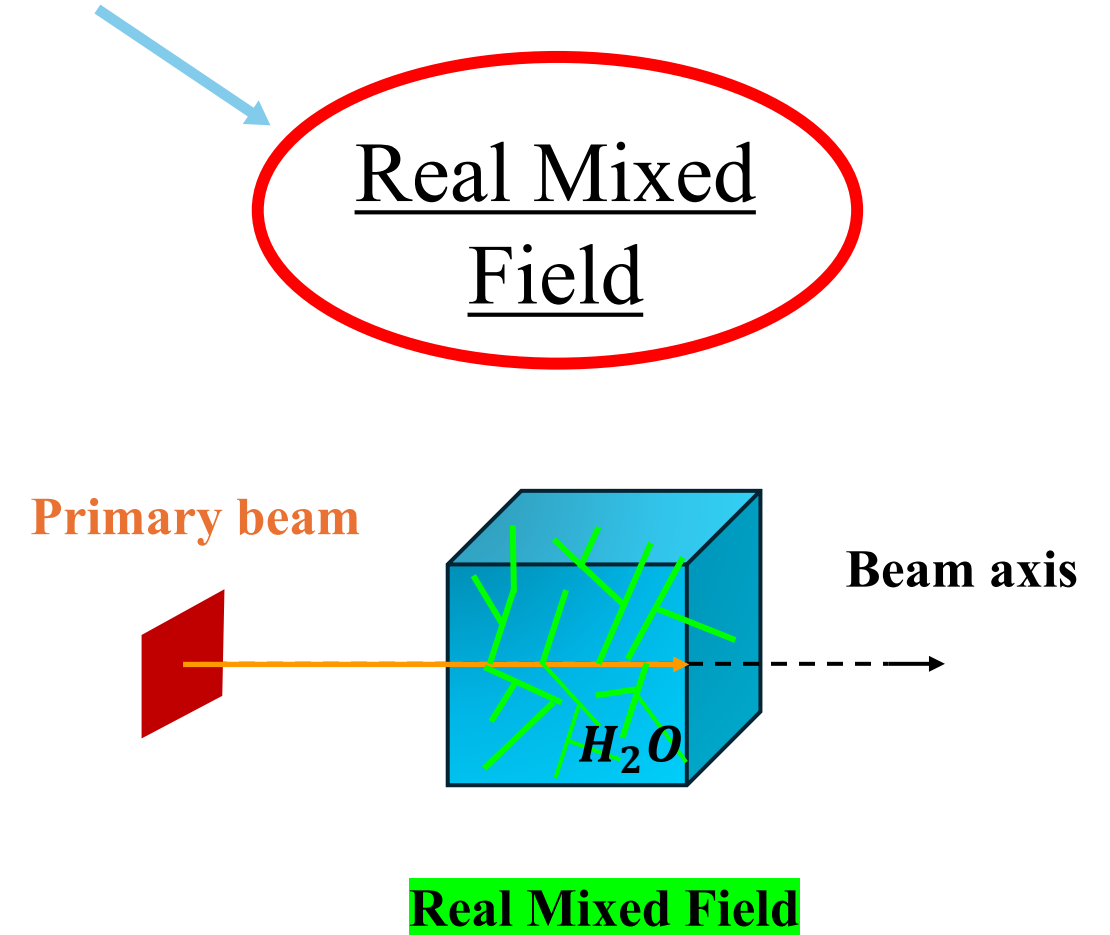
[A. Casali et al., Phys. Med. Biol., 2024]

Photon **k, N** fixed
for ion NTCP
predictions

α_X e β_X

Ion α and β estimation

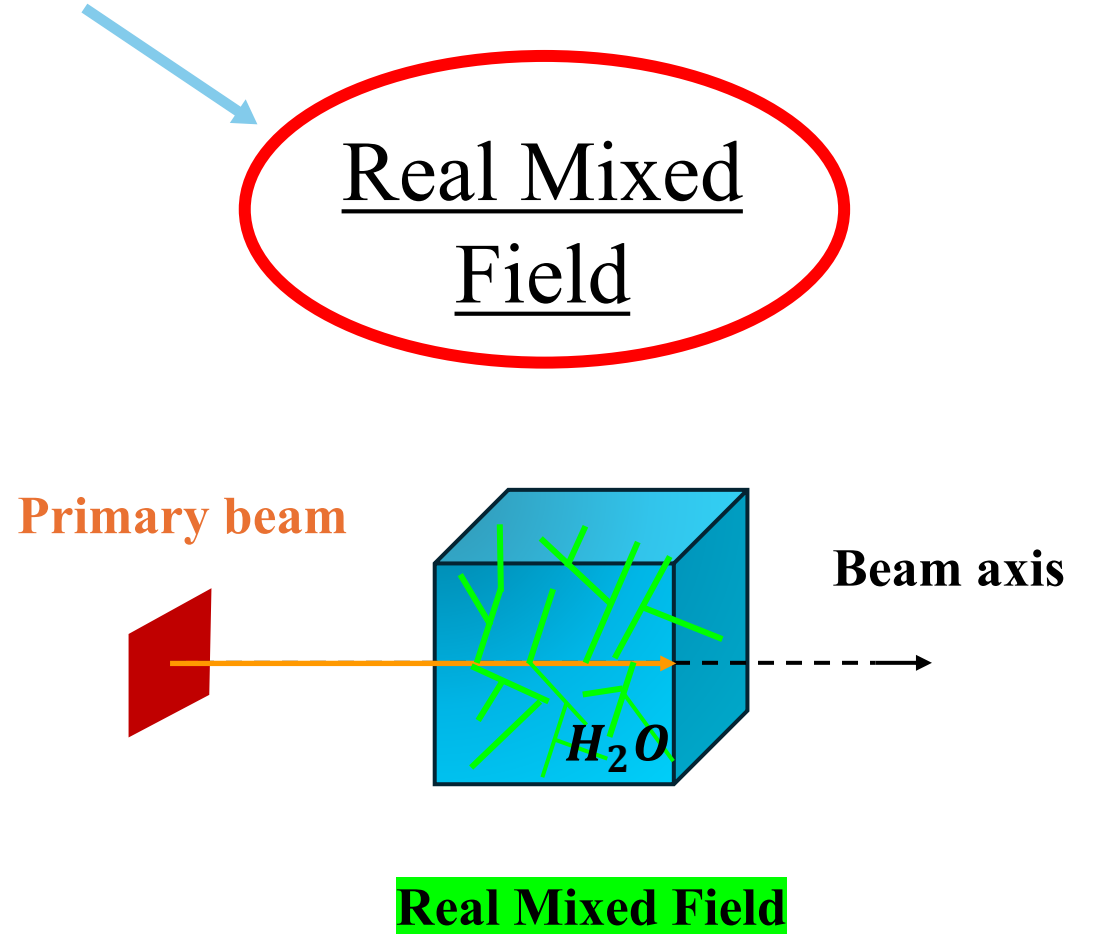
Ion α and β estimation



Ion α and β estimation

**BIANCA-Geant4
interface**

[in collaboration: GEANT4INFN project]



BIANCA

[Ballarini, Carante, Radiat. Phys. And Chem., 2016]

By knowing
 α_X e β_X



BIANCA

[Ballarini, Carante, Radiat. Phys. And Chem., 2016]

By knowing
 α_X e β_X



Z=1 A=1,2,3		
LET	alfa	beta
5	0.161168003608071	0.034227925863557
7.5	0.219155512347106	0.031807059167825
10	0.277730304065006	0.026062986984213
12.5	0.324223249128924	0.031963531745716
15	0.370061833526514	0.032195025167274
17.5	0.421451839190716	0.031121716722449
20	0.482515824349661	0.028525693688078
22.5	0.560520033338037	0.018863044675061
25	0.613244623202487	0.019486893814967
27.5	0.670278414247874	0.018719108913174
30	0.723636950773347	0.019048357687813

Z=2 A=3 (He3)		
LET	alfa	beta
5	0.134484868252636	0.033328267759041
10	0.144914045351193	0.039167916406686
20	0.195309536204132	0.055766427339300
30	0.254263496879065	0.086614721872234
40	0.346232798363745	0.110820821623133
50	0.461751927355611	0.125899692117198
60	0.577156328111620	0.149414730517834
70	0.688177599469057	0.170307321062664
80	0.831202131850177	0.173711239896555
90	0.958976414546513	0.178987749762615

Z=2 A=4 (He4)		
LET	alfa	beta
5	0.122919965474113	0.0282243396663055
10	0.164742642147497	0.0320256389518587

Table of α and
 β for several
particles and
LET values

$LET [keV/\mu m] =$
Stopping power

BIANCA

[Ballarini, Carante, Radiat. Phys. And Chem., 2016]

By knowing
 α_X e β_X



Z=1 A=1,2,3		
LET	alfa	beta
5	0.161168003608071	0.034227925863557
7.5	0.219155512347106	0.031807059167825
10	0.277730304065006	0.026062986984213
12.5	0.324223249128924	0.031963531745716
15	0.370061833526514	0.032195025167274
17.5	0.421451839190716	0.031121716722449
20	0.482515824349661	0.028525693688078
22.5	0.560520033338037	0.018863044675061
25	0.613244623202487	0.019486893814967
27.5	0.670278414247874	0.018719108913174
30	0.723636950773347	0.019048357687813

Z=2 A=3 (He3)		
LET	alfa	beta
5	0.134484868252636	0.033328267759041
10	0.144914045351193	0.039167916406686
20	0.195309536204132	0.055766427339300
30	0.254263496879065	0.086614721872234
40	0.346232798363745	0.110820821623133
50	0.461751927355611	0.125899692117198
60	0.577156328111620	0.149414730517834
70	0.688177599469057	0.170307321062664
80	0.831202131850177	0.173711239896555
90	0.958976414546513	0.178987749762615

Z=2 A=4 (He4)		
LET	alfa	beta
5	0.122919965474113	0.0282243396663055
10	0.164742642147497	0.0320256389518587

Monochromatic Field

Table of α and
 β for several
particles and
LET values

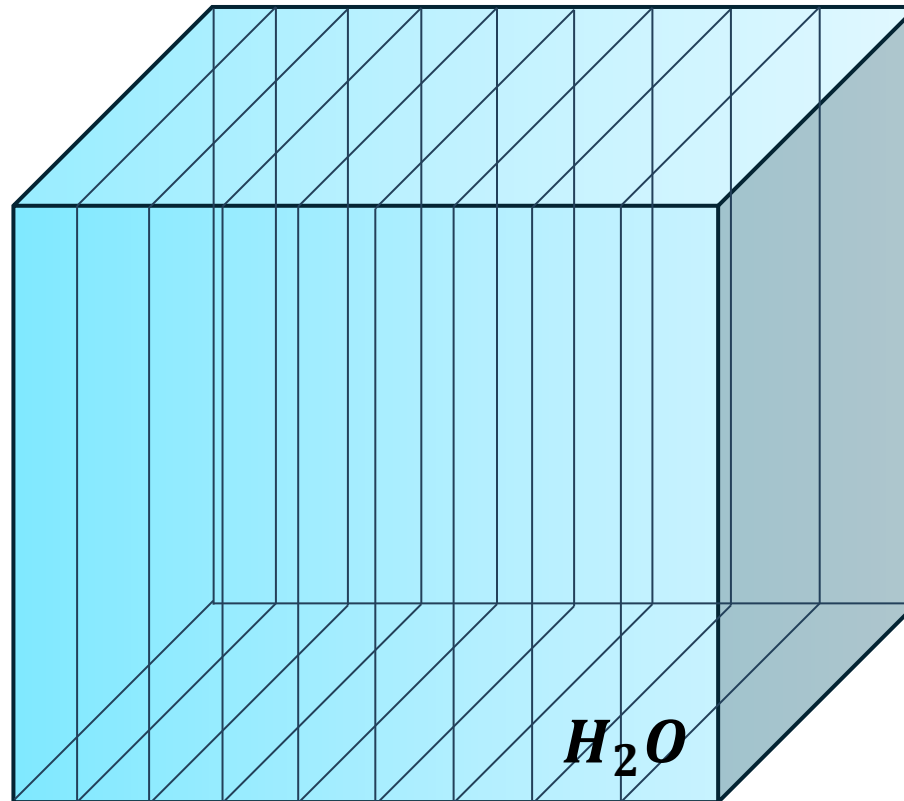
$LET [keV/\mu m] =$
Stopping power

Interface BIANCA - GEANT4

GEANT4 simulation

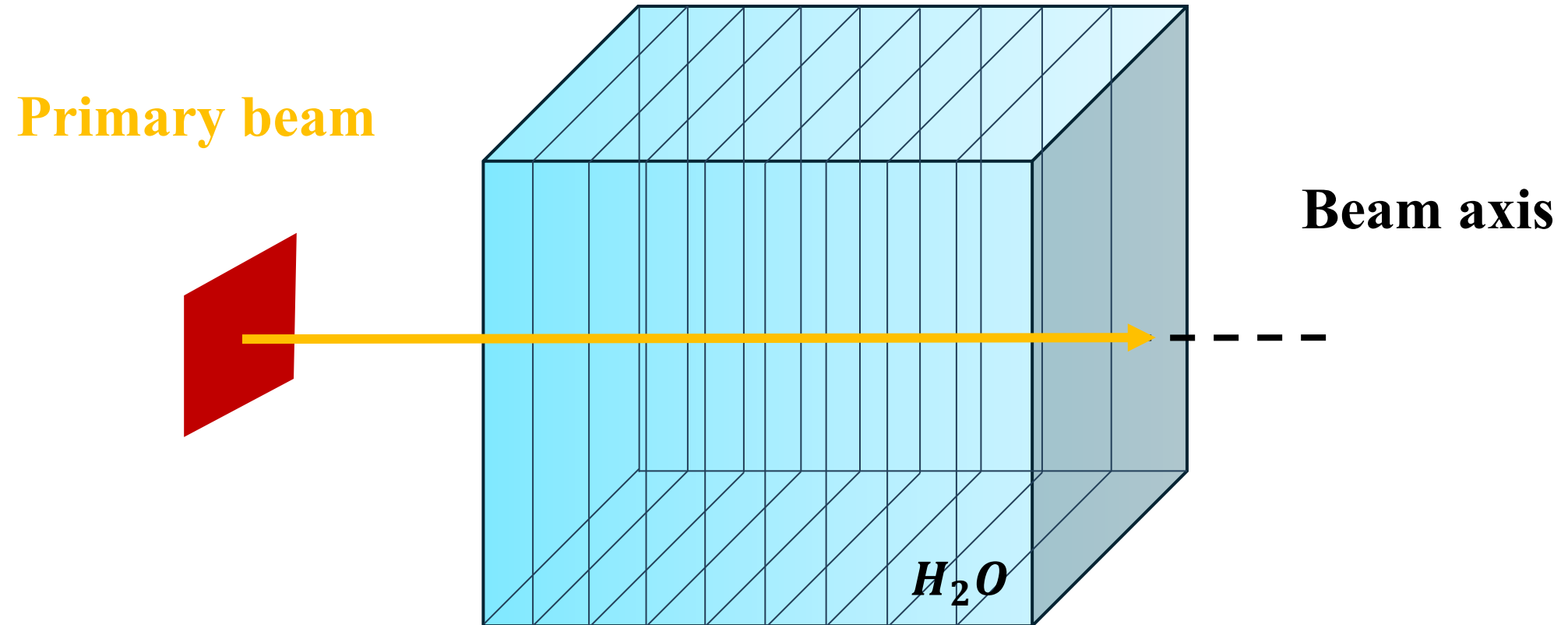
Interface BIANCA - GEANT4

GEANT4 simulation



Interface BIANCA - GEANT4

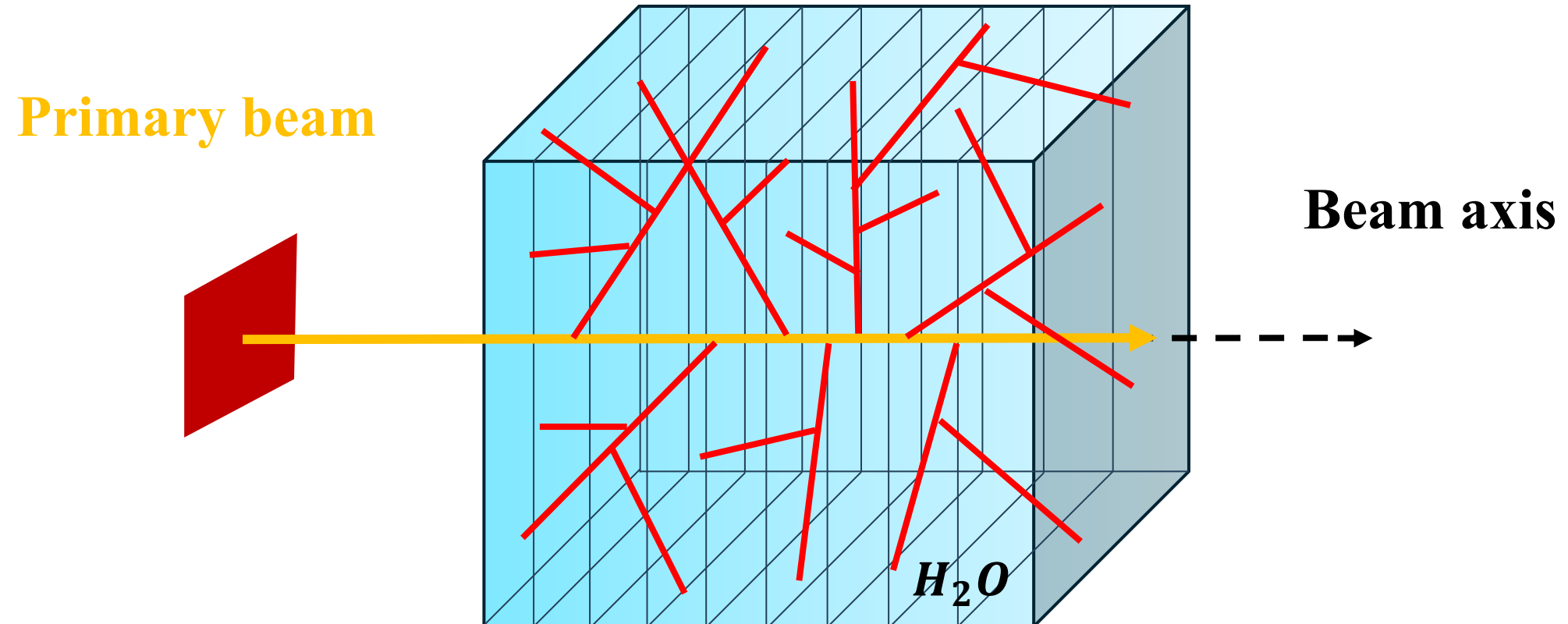
GEANT4 simulation



Interface BIANCA - GEANT4

GEANT4 simulation

Real Mixed Field

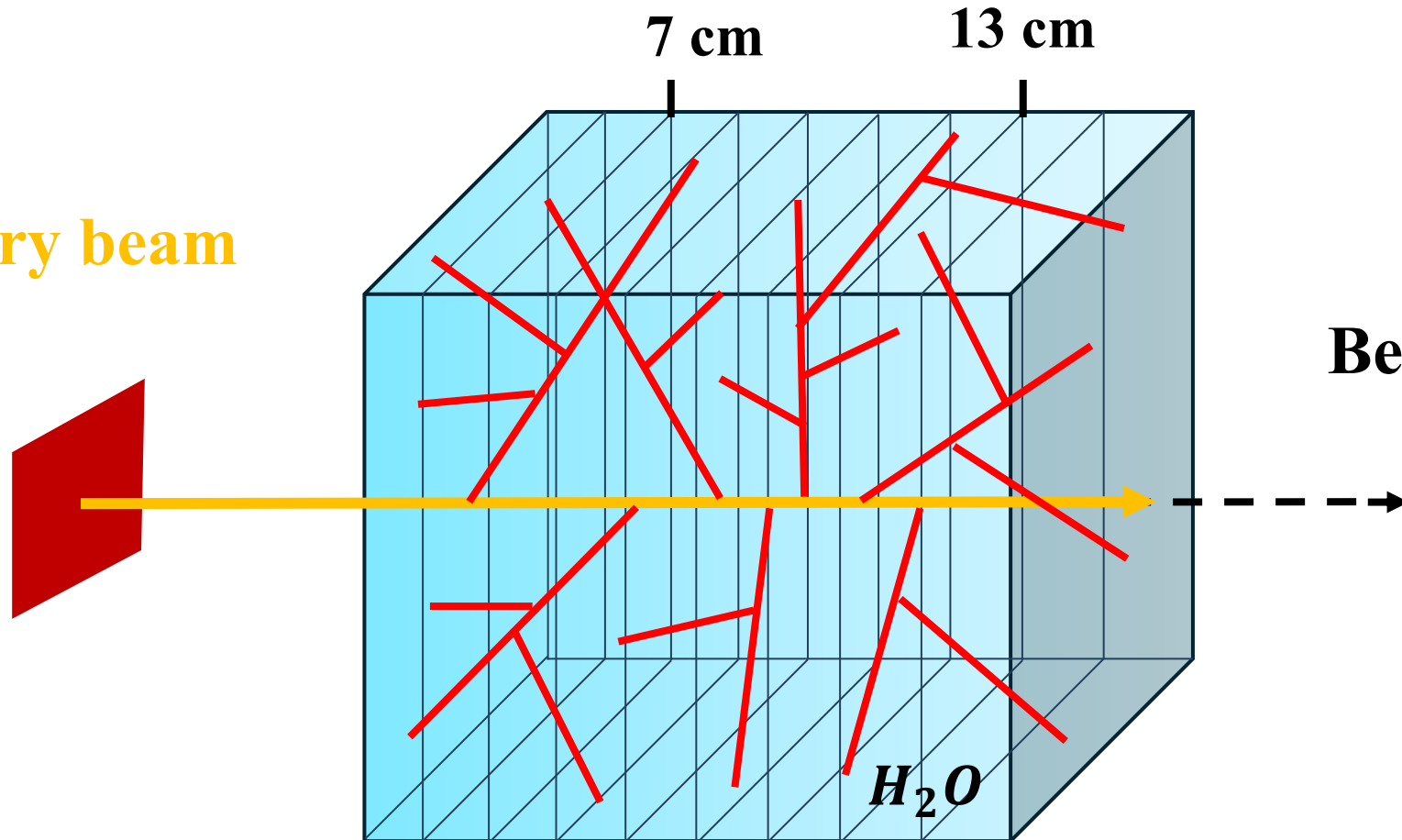


Interface BIANCA - GEANT4

GEANT4 simulation

Real Mixed Field

Primary beam



Physics

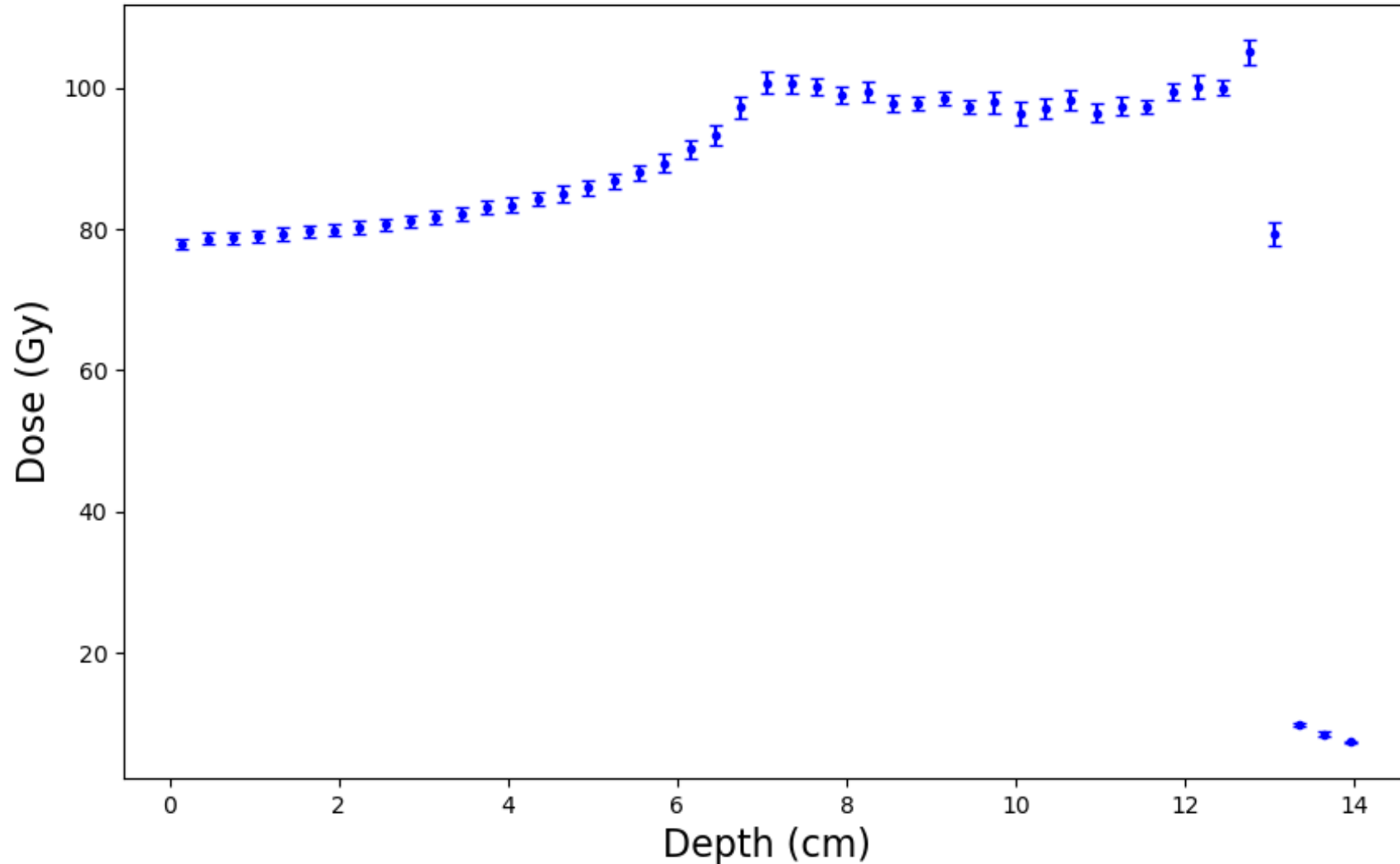
Interface BIANCA - GEANT4

e.g. Carbon ions

Physics

Interface BIANCA - GEANT4

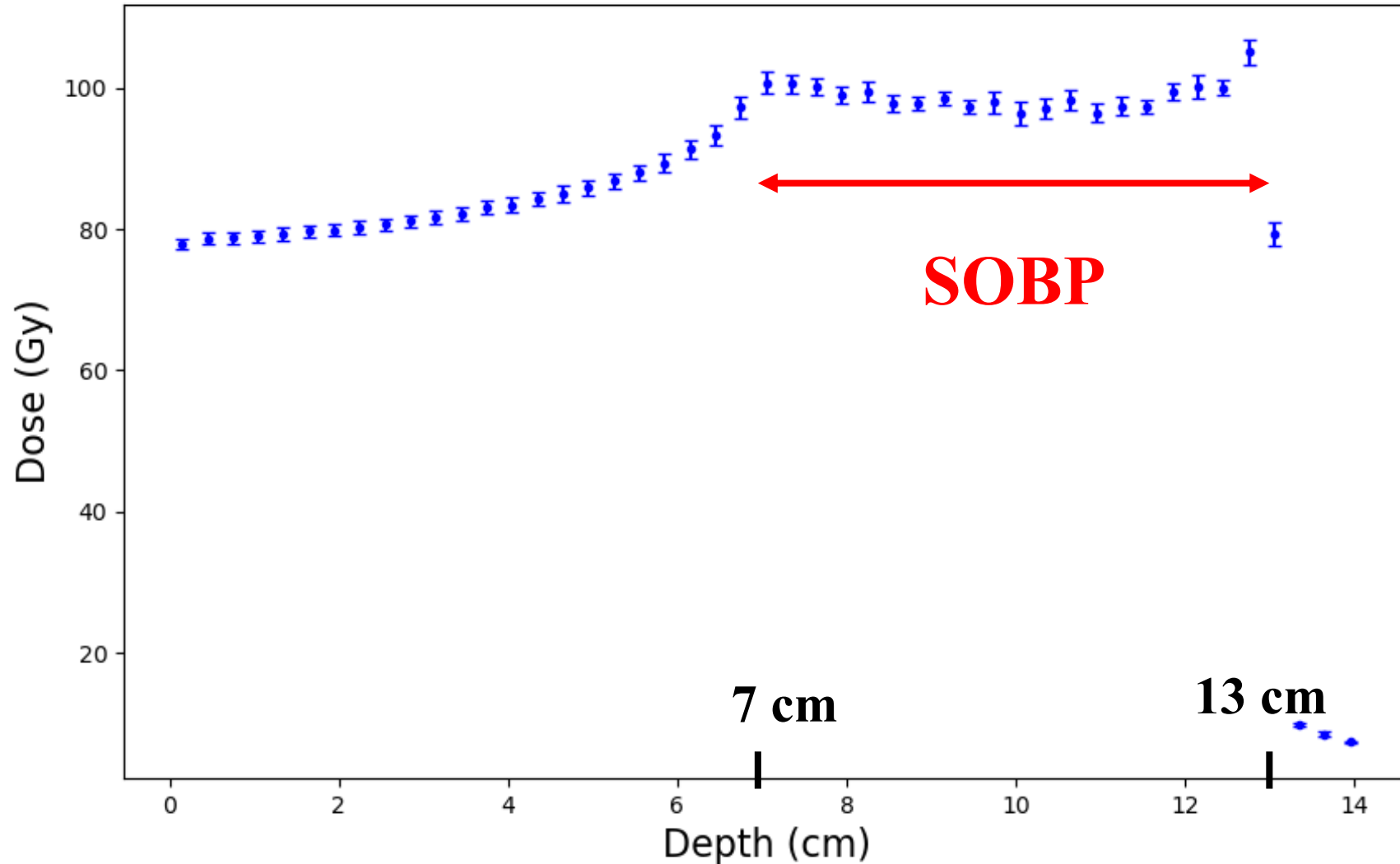
e.g. Carbon ions



Physics

Interface BIANCA - GEANT4

e.g. Carbon ions



Physics

Interface BIANCA - GEANT4

Radiobiology

Interface BIANCA - GEANT4

Radiobiology

Averaged ion

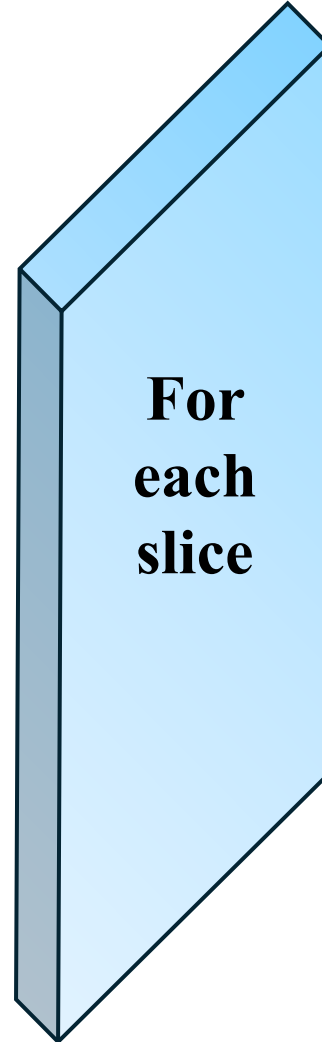
$\bar{\alpha}, \bar{\beta}$

Interface BIANCA - GEANT4

Radiobiology

Averaged ion

$\bar{\alpha}, \bar{\beta}$



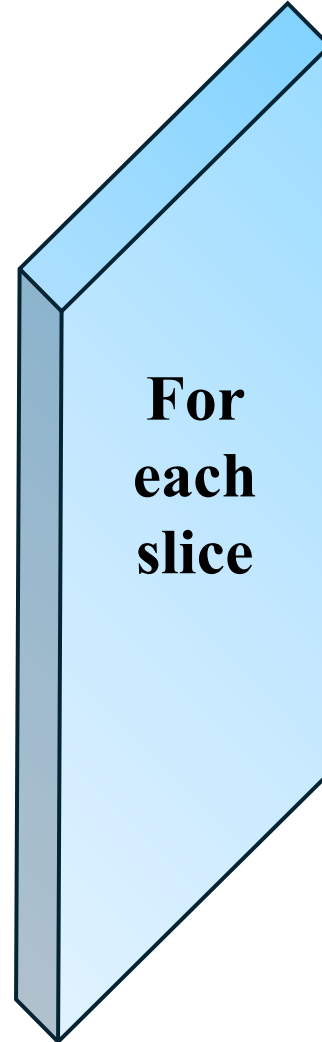
**For
each
slice**

Interface BIANCA - GEANT4

Radiobiology

Averaged ion

$\bar{\alpha}, \bar{\beta}$



$$\bar{\alpha} = \frac{\sum_{i=1}^n \sum_{j=1}^m \alpha_{i,j} D_{i,j}}{\sum_{i=1}^n \sum_{j=1}^m D_{i,j}}$$

$$\bar{\beta} = \left(\frac{\sum_{i=1}^n \sum_{j=1}^m \sqrt{\beta_{i,j} D_{i,j}}}{\sum_{i=1}^n \sum_{j=1}^m D_{i,j}} \right)^2$$

Interface BIANCA - GEANT4

Radiobiology

Averaged ion

$\bar{\alpha}, \bar{\beta}$

For
each
slice

Z=1	A=1,2,3		
LET	alfa	beta	
5	0.161168003608071	0.034227925863557	
7.5	0.219155512347106	0.031807059167825	
10	0.277730304065006	0.026062986984213	
12.5	0.324223249128924	0.031963531745716	
15	0.370061833526514	0.032195025167274	
17.5	0.421451839190716	0.031121716722449	
20	0.482515824349661	0.028525693688078	
22.5	0.560520033338037	0.018863044675061	
25	0.613244623202487	0.019486893814967	
27.5	0.670278414247874	0.018719108913174	
30	0.723636950773347	0.019048357687813	

Z=2	A=3 (He3)		
LET	alfa	beta	
5	0.134484868252636	0.033328267759041	
10	0.144914045351193	0.039167916406686	
20	0.195309536204132	0.055766427339300	
30	0.254263496879065	0.086614721872234	
40	0.346232798363745	0.110820821623133	
50	0.461751927355611	0.125899692117198	
60	0.577156328111620	0.149414730517834	
70	0.688177599469057	0.170307321062664	
80	0.831202131850177	0.173711239896555	
90	0.958976414546513	0.178987749762615	

Z=2	A=4 (He4)		
LET	alfa	beta	
5	0.122919965474113	0.0282243396663055	
10	0.164742642147497	0.0320256389518587	

BIANCA

$$\bar{\alpha} = \frac{\sum_{i=1}^n \sum_{j=1}^m \alpha_{i,j} D_{i,j}}{\sum_{i=1}^n \sum_{j=1}^m D_{i,j}}$$

$$\bar{\beta} = \left(\frac{\sum_{i=1}^n \sum_{j=1}^m \sqrt{\beta_{i,j} D_{i,j}}}{\sum_{i=1}^n \sum_{j=1}^m D_{i,j}} \right)^2$$

Interface BIANCA - GEANT4

Radiobiology

Averaged ion

$\bar{\alpha}, \bar{\beta}$

For
each
slice

Z=1	A=1,2,3		
LET	alfa	beta	
5	0.161168003608071	0.034227925863557	
7.5	0.219155512347106	0.031807059167825	
10	0.277730304065006	0.026062986984213	
12.5	0.324223249128924	0.031963531745716	
15	0.370061833526514	0.032195025167274	
17.5	0.421451839190716	0.031121716722449	
20	0.482515824349661	0.028525693688078	
22.5	0.560520033338037	0.018863044675061	
25	0.613244623202487	0.019486893814967	
27.5	0.670278414247874	0.018719108913174	
30	0.723636950773347	0.019048357687813	

Z=2	A=3 (He3)		
LET	alfa	beta	
5	0.134484868252636	0.033328267759041	
10	0.144914045351193	0.039167916406686	
20	0.195309536204132	0.055766427339300	
30	0.254263496879065	0.086614721872234	
40	0.346232798363745	0.110820821623133	
50	0.461751927355611	0.125899692117198	
60	0.577156328111620	0.149414730517834	
70	0.688177599469057	0.170307321062664	
80	0.831202131850177	0.173711239896555	
90	0.958976414546513	0.178987749762615	

Z=2	A=4 (He4)		
LET	alfa	beta	
5	0.122919965474113	0.0282243396663055	
10	0.164742642147497	0.0320256389518587	

BIANCA

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Interface BIANCA - GEANT4

Radiobiology

Averaged ion

$\bar{\alpha}, \bar{\beta}$

For
each
slice

i - th particle

Z=1	A=1,2,3		
LET	alfa	beta	
5	0.161168003608071	0.034227925863557	
7.5	0.219155512347106	0.031807059167825	
10	0.277730304065006	0.026062986984213	
12.5	0.324223249128924	0.031963531745716	
15	0.370061833526514	0.032195025167274	
17.5	0.421451839190716	0.031121716722449	
20	0.482515824349661	0.028525693688078	
22.5	0.560520033338037	0.018863044675061	
25	0.613244623202487	0.019486893814967	
27.5	0.670278414247874	0.018719108913174	
30	0.723636950773347	0.019048357687813	

Z=2	A=3 (He3)		
LET	alfa	beta	
5	0.134484868252636	0.033328267759041	
10	0.144914045351193	0.039167916406686	
20	0.195309536204132	0.055766427339300	
30	0.254263496879065	0.086614721872234	
40	0.346232798363745	0.110820821623133	
50	0.461751927355611	0.125899692117198	
60	0.577156328111620	0.149414730517834	
70	0.688177599469057	0.170307321062664	
80	0.831202131850177	0.173711239896555	
90	0.958976414546513	0.178987749762615	

Z=2	A=4 (He4)		
LET	alfa	beta	
5	0.122919965474113	0.0282243396663055	
10	0.164742642147497	0.0320256389518587	

BIANCA

$$\bar{\alpha} = \frac{\sum_{i=1}^n \sum_{j=1}^m \alpha_{i,j} D_{i,j}}{\sum_{i=1}^n \sum_{j=1}^m D_{i,j}}$$

$$\bar{\beta} = \left(\frac{\sum_{i=1}^n \sum_{j=1}^m \sqrt{\beta_{i,j} D_{i,j}}}{\sum_{i=1}^n \sum_{j=1}^m D_{i,j}} \right)^2$$

Interface BIANCA - GEANT4

Radiobiology

Averaged ion

$\bar{\alpha}, \bar{\beta}$

For
each
slice

Z=1	A=1,2,3		
LET	alfa	beta	
5	0.161168003608071	0.034227925863557	
7.5	0.219155512347106	0.031807059167825	
10	0.277730304065006	0.026062986984213	
12.5	0.324223249128924	0.031963531745716	
15	0.370061833526514	0.032195025167274	
17.5	0.421451839190716	0.031121716722449	
20	0.482515824349661	0.028525693688078	
22.5	0.560520033338037	0.018863044675061	
25	0.613244623202487	0.019486893814967	
27.5	0.670278414247874	0.018719108913174	
30	0.723636950773347	0.019048357687813	

Z=2	A=3 (He3)		
LET	alfa	beta	
5	0.134484868252636	0.033328267759041	
10	0.144914045351193	0.039167916406686	
20	0.195309536204132	0.055766427339300	
30	0.254263496879065	0.086614721872234	
40	0.346232798363745	0.110820821623133	
50	0.461751927355611	0.125899692117198	
60	0.577156328111620	0.149414730517834	
70	0.688177599469057	0.170307321062664	
80	0.831202131850177	0.173711239896555	
90	0.958976414546513	0.178987749762615	

Z=2	A=4 (He4)		
LET	alfa	beta	
5	0.122919965474113	0.0282243396663055	
10	0.164742642147497	0.0320256389518587	

BIANCA

$$\bar{\alpha} = \frac{\sum_{i=1}^n \sum_{j=1}^m \alpha_{i,j} D_{i,j}}{\sum_{i=1}^n \sum_{j=1}^m D_{i,j}}$$

$$\bar{\beta} = \left(\frac{\sum_{i=1}^n \sum_{j=1}^m \sqrt{\beta_{i,j} D_{i,j}}}{\sum_{i=1}^n \sum_{j=1}^m D_{i,j}} \right)^2$$

i - th

particle

j - th

energy value

Ion NTCP predictions

Real Mixed Field

$$\mathbf{NTCP} = 1 - \left[1 - \left(1 - e^{-\bar{\alpha}nd - \bar{\beta}nd^2} \right)^k \right]^N$$

Ion NTCP predictions

Real Mixed Field

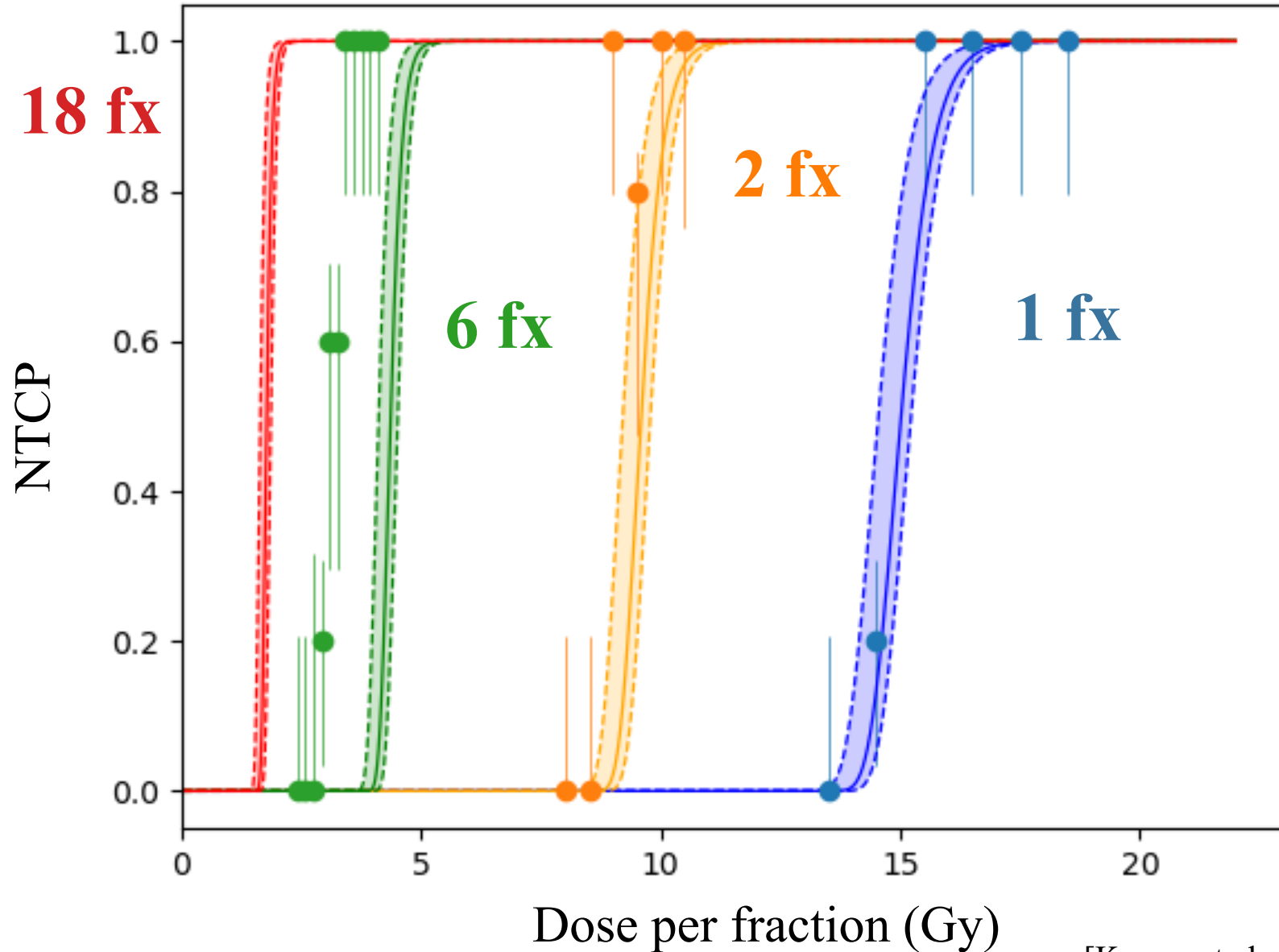
$$\mathbf{NTCP} = 1 - \left[1 - \left(1 - e^{-\bar{\alpha}nd - \bar{\beta}nd^2} \right)^k \right]^N$$

NO free - parameters



Full predictions of
ion NTCP curves

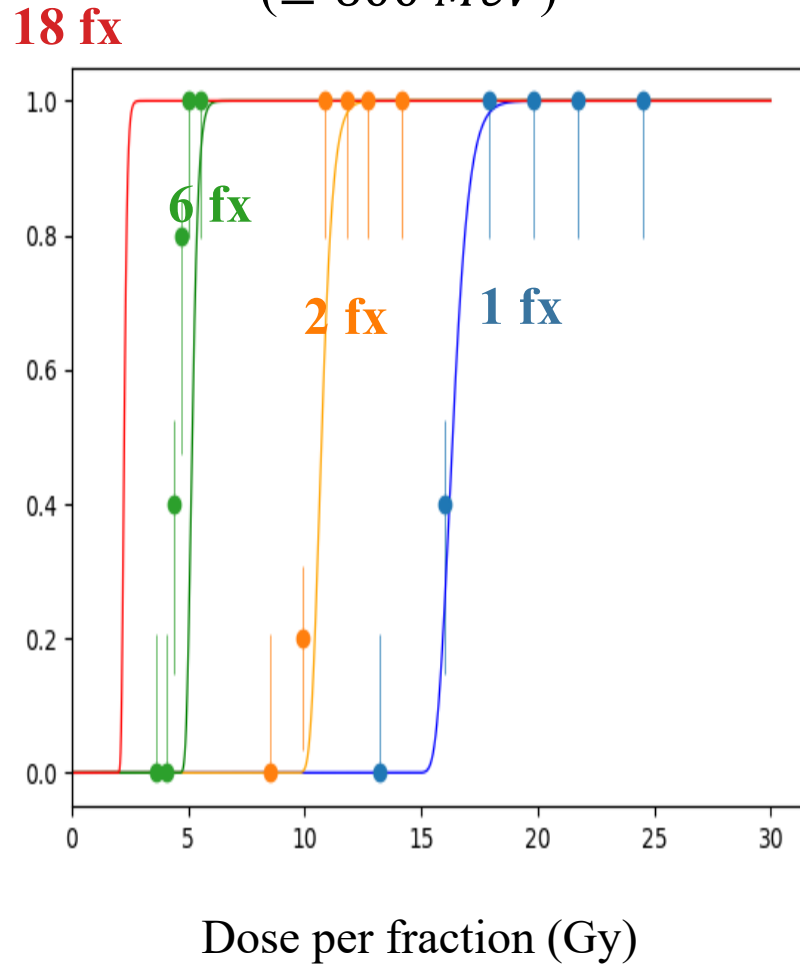
Carbon ions $66 \pm 6 \text{ keV}/\mu\text{m}$ ($\cong 375 \text{ MeV}$)



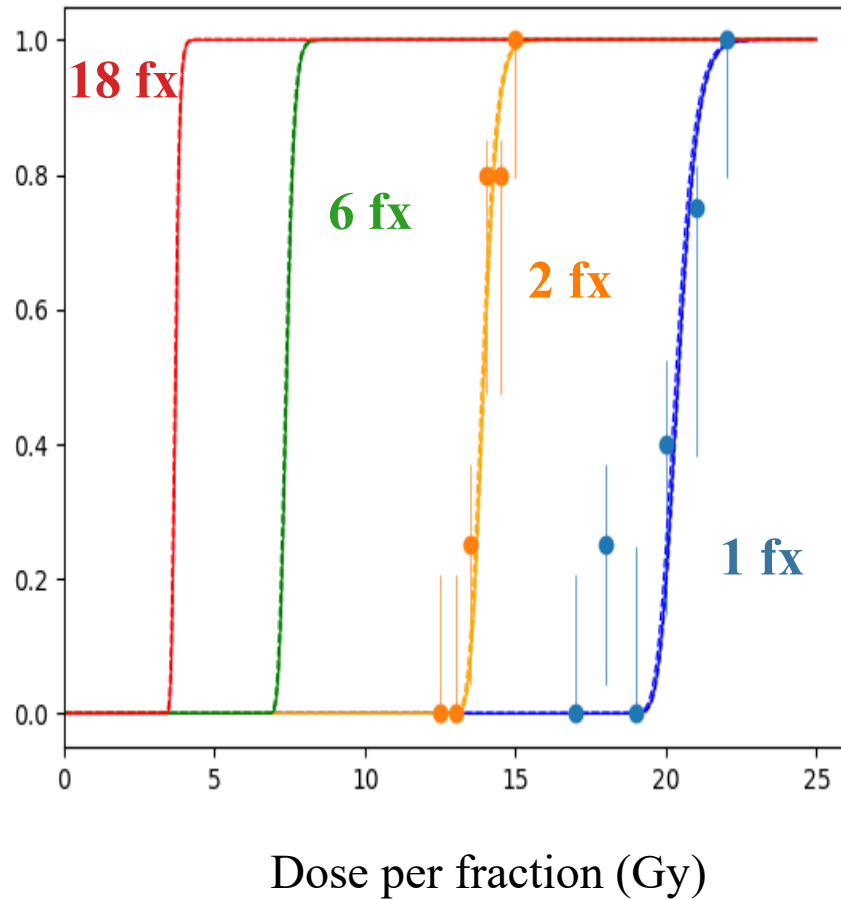
[A. Casali et al., European Physical Journal Special Topics., submitted, **2025**]

For other particles and LET values

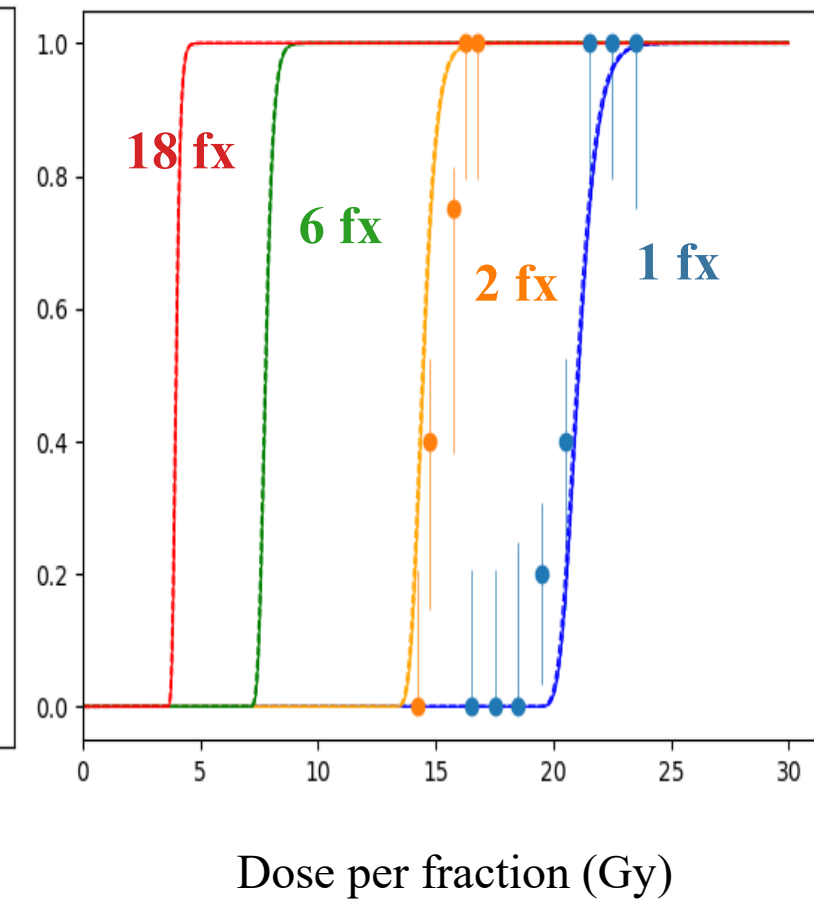
Carbon ions 45 keV/ μm
($\cong 600 \text{ MeV}$)



Helium ions $9.4^{+0.6}_{-1.4} \text{ keV}/\mu\text{m}$
($\cong 90 \text{ MeV}$)



Protons $2.7 \pm 0.1 \text{ keV}/\mu\text{m}$
($\cong 19 \text{ MeV}$)



Validation on other data

Validation on other data



Collected by
**another
research group**

Validation on other data



Collected by
**another
research group**

$$\text{NTCP} = 1 - \left[1 - \left(1 - e^{-\bar{\alpha}nd - \bar{\beta}nd^2} \right)^k \right]^N$$

BIANCA – Geant4
interface

Validation on other data



Collected by
**another
research group**

$$\text{NTCP} = 1 - \left[1 - \left(1 - e^{-\bar{\alpha}nd - \bar{\beta}nd^2} \right)^k \right]^N$$

BIANCA – Geant4
interface

Z=1 A=1,2,3		
LET	alfa	beta
5	0.161168003608071	0.034227925863557
7.5	0.219155512347106	0.031807059167825
10	0.277730304065006	0.026062986984213
12.5	0.324223249128924	0.031963531745716
15	0.370061833526514	0.032195025167274
17.5	0.421451839190716	0.031121716722449
20	0.482515824349661	0.028525693688078
22.5	0.560520033338037	0.018863044675061
25	0.613244623202487	0.019486893814967
27.5	0.670278414247874	0.018719108913174
30	0.723636950773347	0.019048357687813
Z=2 A=3 (He3)		
LET	alfa	beta
5	0.134484868252636	0.033328267759041
10	0.144914045351193	0.039167916406686
20	0.195309536204132	0.055766427339300
30	0.254263496879065	0.086614721872234
40	0.346232798363745	0.110820821623133
50	0.461751927355611	0.125899692117198
60	0.577156328111620	0.149414730517834
70	0.688177599469057	0.170307321062664
80	0.831202131850177	0.173711239896555
90	0.958976414546513	0.178987749762615
Z=2 A=4 (He4)		
LET	alfa	beta
5	0.122919965474113	0.0282243396663055
10	0.164742642147497	0.0320256389518587

Previous
dataset

Validation on other data



Collected by
**another
research group**

$$\text{NTCP} = 1 - \left[1 - \left(1 - e^{-\bar{\alpha}nd - \bar{\beta}nd^2} \right)^k \right]^N$$

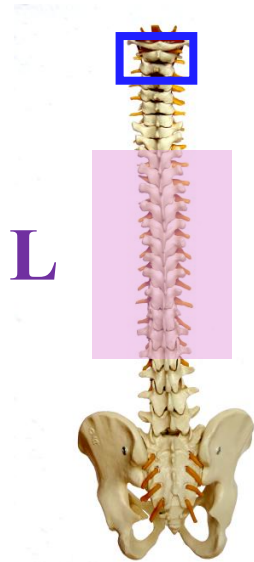
BIANCA – Geant4
interface

Previous
dataset

Previous
dataset

Z=1 A=1,2,3		
LET	alfa	beta
5	0.161168003608071	0.034227925863557
7.5	0.219155512347106	0.031807059167825
10	0.277730304065006	0.026062986984213
12.5	0.324223249128924	0.031963531745716
15	0.370061833526514	0.032195025167274
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20	0.482515824349661	0.028525693688078
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25	0.613244623202487	0.019486893814967
27.5	0.670278414247874	0.018719108913174
30	0.723636950773347	0.019048357687813
Z=2 A=3 (He3)		
LET	alfa	beta
5	0.134484868252636	0.033328267759041
10	0.144914045351193	0.039167916406686
20	0.195309536204132	0.055766427339300
30	0.254263496879065	0.086614721872234
40	0.346232798363745	0.110820821623133
50	0.461751927355611	0.125899692117198
60	0.577156328111620	0.149414730517834
70	0.688177599469057	0.170307321062664
80	0.831202131850177	0.173711239896555
90	0.958976414546513	0.178987749762615
Z=2 A=4 (He4)		
LET	alfa	beta
5	0.122919965474113	0.0282243396663055
10	0.164742642147497	0.0320256389518587

Validation on other data



Collected by
**another
research group**

$$\text{NTCP} = 1 - \left[1 - \left(1 - e^{-\bar{\alpha}nd - \bar{\beta}nd^2} \right)^k \right]^N$$

BIANCA – Geant4
interface

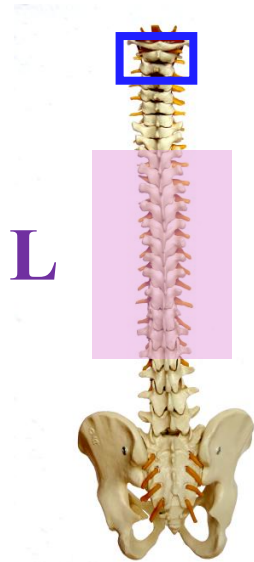
Z=1 A=1,2,3		
LET	alfa	beta
5	0.161168003608071	0.034227925863557
7.5	0.219155512347106	0.031807059167825
10	0.277730304065006	0.026062986984213
12.5	0.324223249128924	0.031963531745716
15	0.370061833526514	0.032195025167274
17.5	0.421451839190716	0.031121716722449
20	0.482515824349661	0.028525693688078
22.5	0.560520033338037	0.018863044675061
25	0.613244623202487	0.019486893814967
27.5	0.670278414247874	0.018719108913174
30	0.723636950773347	0.019048357687813
Z=2 A=3 (He3)		
LET	alfa	beta
5	0.134484868252636	0.033328267759041
10	0.144914045351193	0.039167916406686
20	0.195309536204132	0.055766427339300
30	0.254263496879065	0.086614721872234
40	0.346232798363745	0.110820821623133
50	0.461751927355611	0.125899692117198
60	0.577156328111620	0.149414730517834
70	0.688177599469057	0.170307321062664
80	0.831202131850177	0.173711239896555
90	0.958976414546513	0.178987749762615
Z=2 A=4 (He4)		
LET	alfa	beta
5	0.122919965474113	0.0282243396663055
10	0.164742642147497	0.0320256389518587

Previous
dataset

Previous
dataset

$\propto L$
irradiated
length

Validation on other data



Collected by
**another
research group**

$$\text{NTCP} = 1 - \left[1 - \left(1 - e^{-\bar{\alpha}nd - \bar{\beta}nd^2} \right)^k \right]^N$$

BIANCA – Geant4
interface

Z=1 A=1,2,3		
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40	0.346232798363745	0.110820821623133
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90	0.958976414546513	0.178987749762615
Z=2 A=4 (He4)		
LET	alfa	beta
5	0.122919965474113	0.0282243396663055
10	0.164742642147497	0.0320256389518587

Previous
dataset

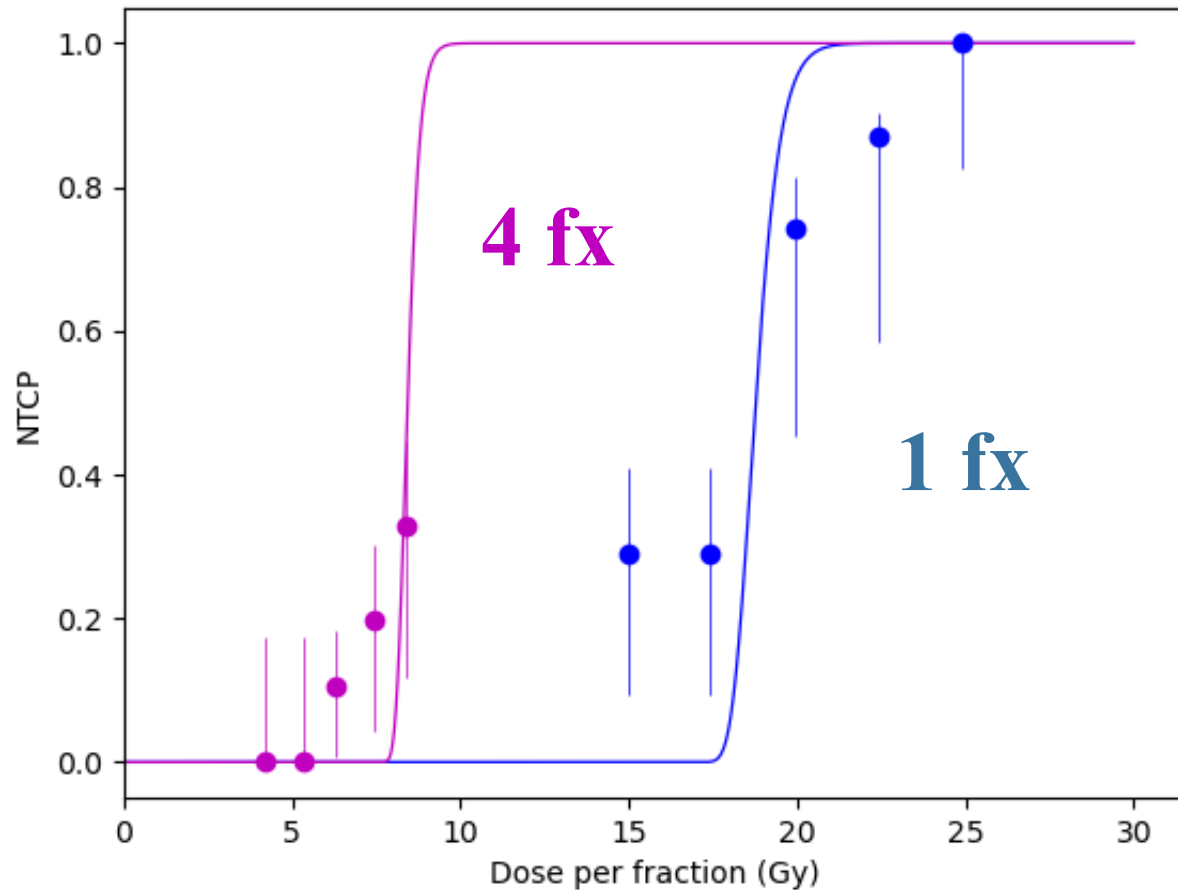
Previous
dataset

$\propto L$
irradiated
length

Previous
dataset

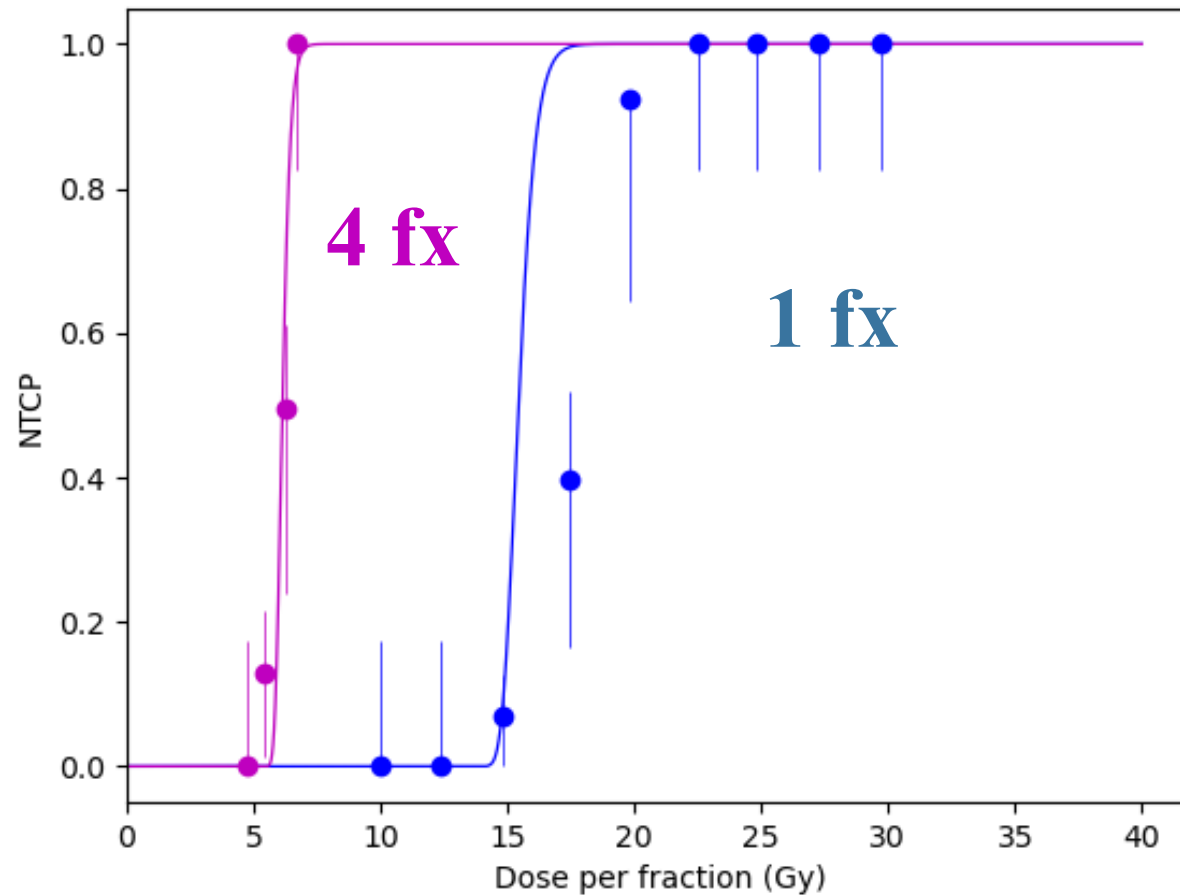
Carbon ions 10 keV/ μm

($\cong 5500 \text{ MeV}$)



Carbon ions 80 keV/ μm

($\cong 285 \text{ MeV}$)



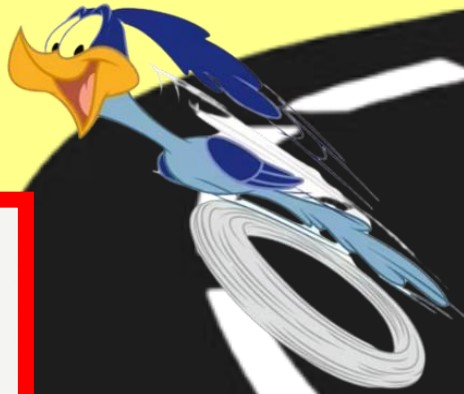
Existing
NTCP
models

Our
approach for
NTCP models

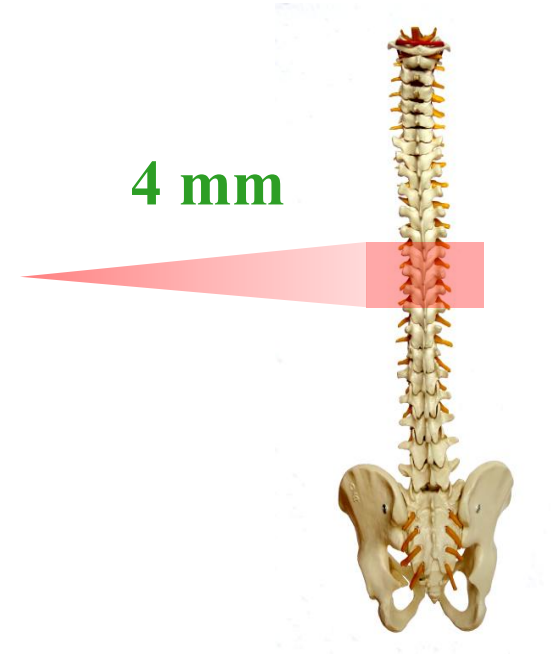
LITERATURE

Modelling
Volume
Effect

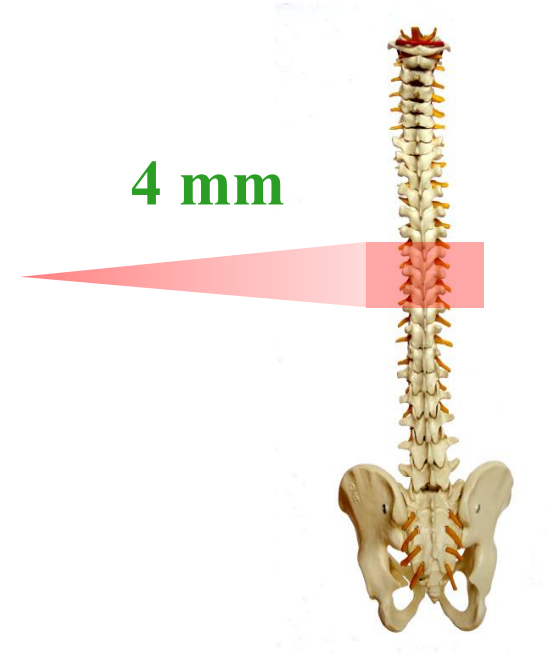
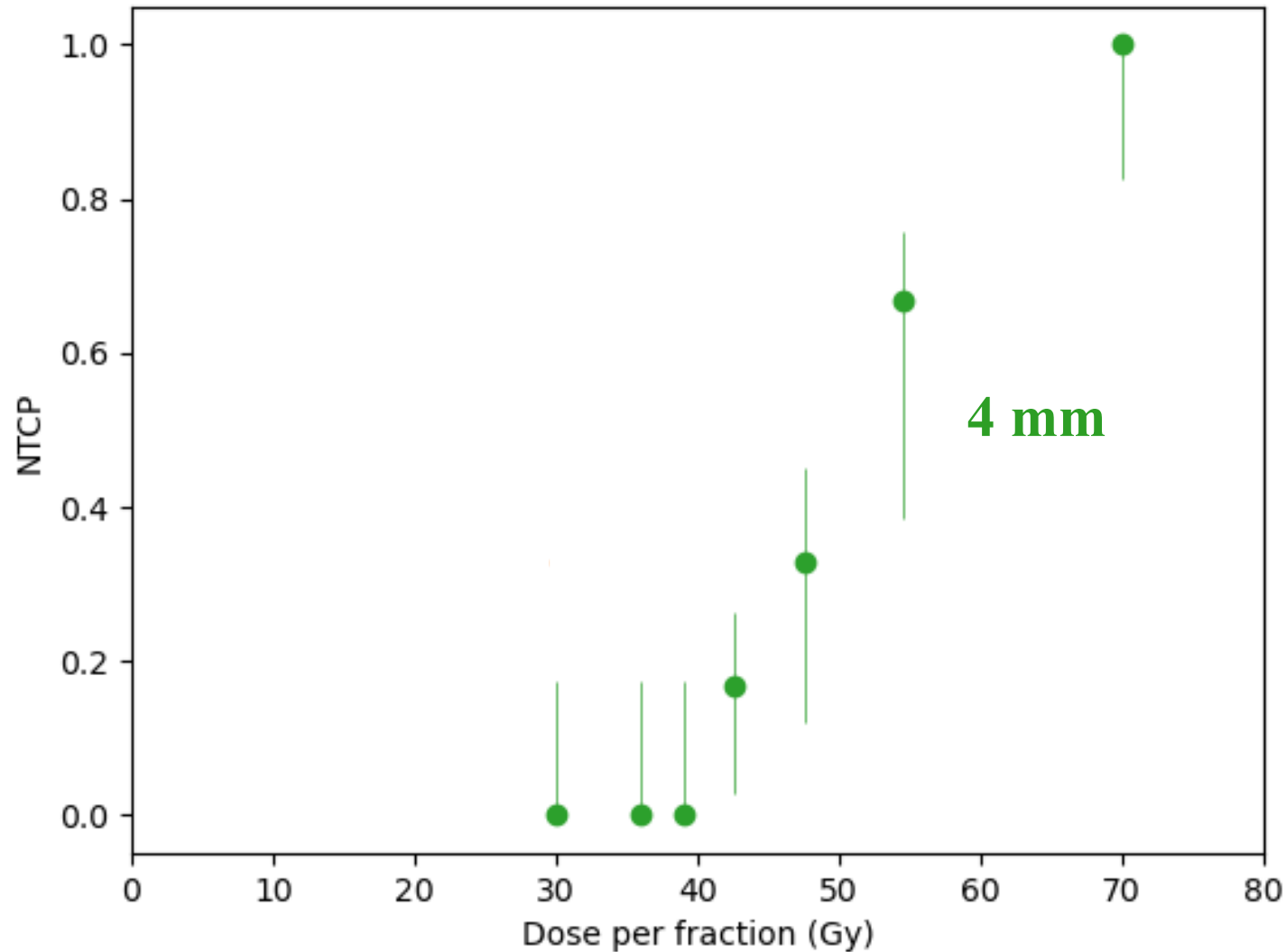
INNOVATION



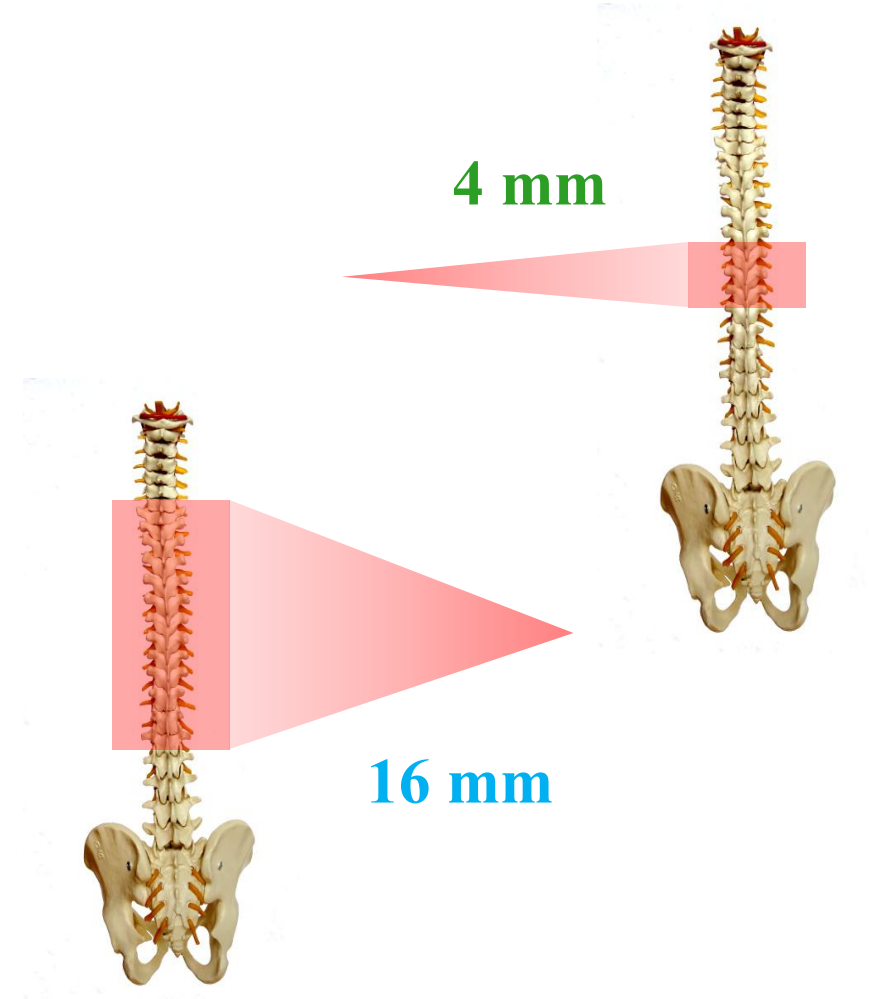
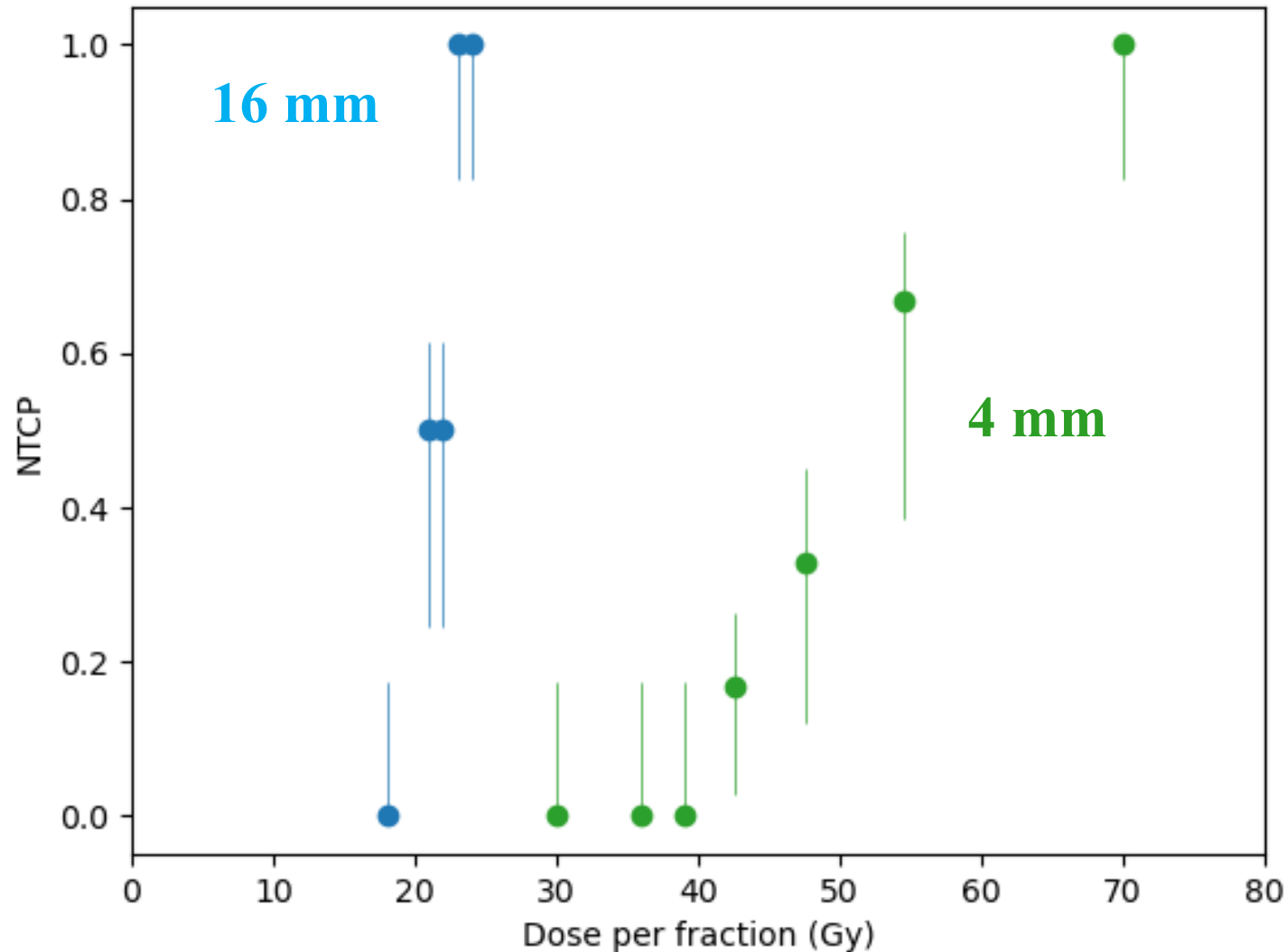
Open Problems: Volume Effect



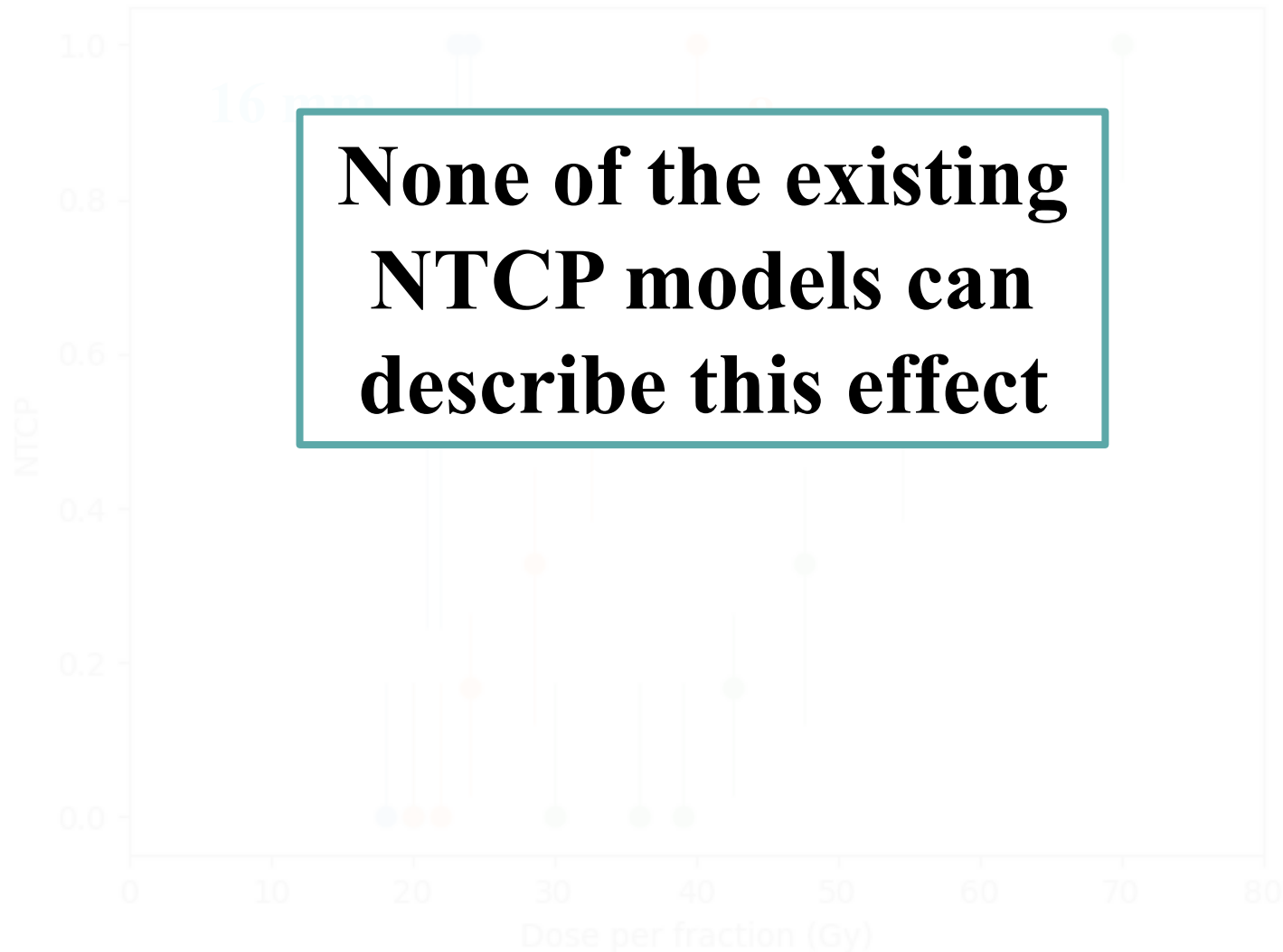
Open Problems: Volume Effect



Open Problems: Volume Effect

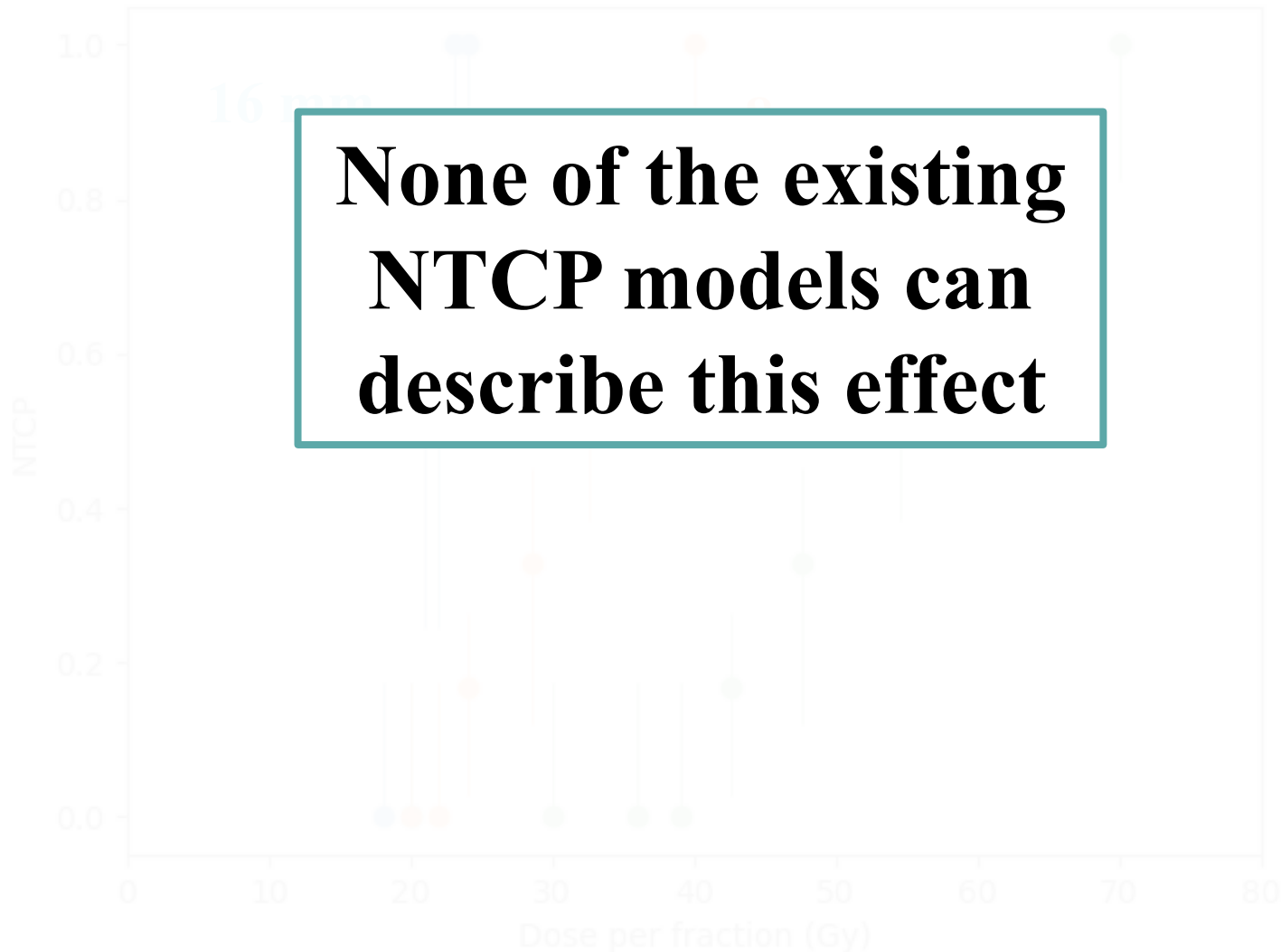


Open Problems: Volume Effect



Open Problems: Volume Effect

**None of the existing
NTCP models can
describe this effect**



*Cell
migration*

Shirato model

Critical Element model

$$\mathbf{NTCP} = 1 - \left[1 - \left(1 - e^{-\alpha nd - \beta nd^2} \right)^k \right]^{\frac{L}{L1}}$$

Shirato model

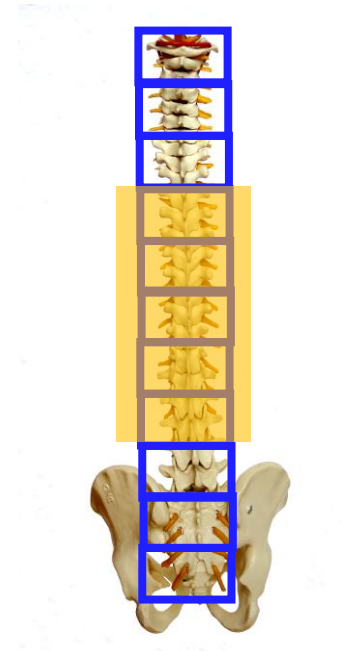
Critical Element model

$$\mathbf{NTCP} = 1 - \left[1 - \left(1 - e^{-\alpha nd - \beta nd^2} \right)^k \right]^{\frac{L}{L1} N}$$

Shirato model

Critical Element model

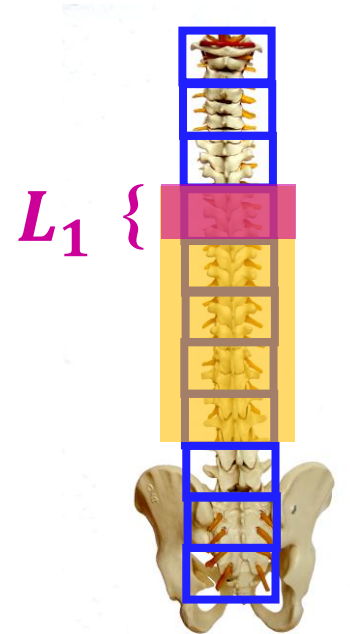
$$\text{NTCP} = 1 - \left[1 - \left(1 - e^{-\alpha nd - \beta nd^2} \right)^k \right]^{\frac{L}{L_1} N}$$



Shirato model

Critical Element model

$$\text{NTCP} = 1 - \left[1 - \left(1 - e^{-\alpha nd - \beta nd^2} \right)^k \right]^{\frac{L}{L_1} N}$$



Shirato model

Probability of killing 1 cell

Migration term

$$\text{NTCP} = 1 - \left[1 - \left[(1 - e^{-\alpha nd - \beta nd^2}) \mathbf{M(I)} \right]^k \right]^{\frac{L}{L1}}$$

Shirato model

Probability of killing 1 cell

Migration term

$$\text{NTCP} = 1 - \left[1 - \left[(1 - e^{-\alpha nd - \beta nd^2}) \mathbf{M}(\mathbf{I}) \right]^k \right]^{\frac{L}{L+1}}$$

- ✗ I from fit
- ✗ Validation limited to one dataset
- ✗ Multiple parameter sets fit the data

LITERATURE

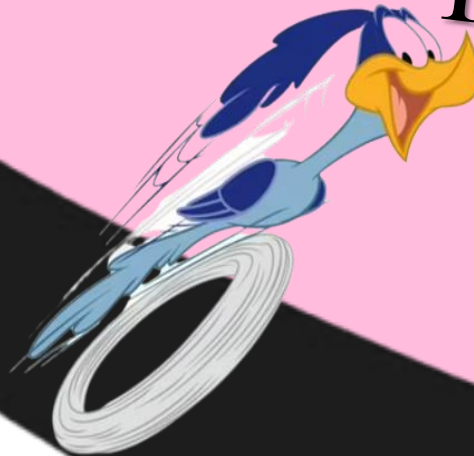
Modelling
Volume
Effect

Existing
NTCP
models

Our
approach for
NTCP models

INNOVATION

**Volume
Effect:
my ideas**



Volume Effect: my ideas

*Critical Element
model*

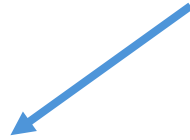
$$\mathbf{NTCP} = 1 - \left[1 - \left(1 - e^{-\alpha nd - \beta nd^2} \right)^k \right]^{\frac{L}{L1}}$$

Volume Effect: my ideas

*Critical Element
model*

$$\text{NTCP} = 1 - \left[1 - \left(1 - e^{-\alpha nd - \beta nd^2} \right)^k \right]^{\frac{L}{L_1}}$$

**Dose out of
target**

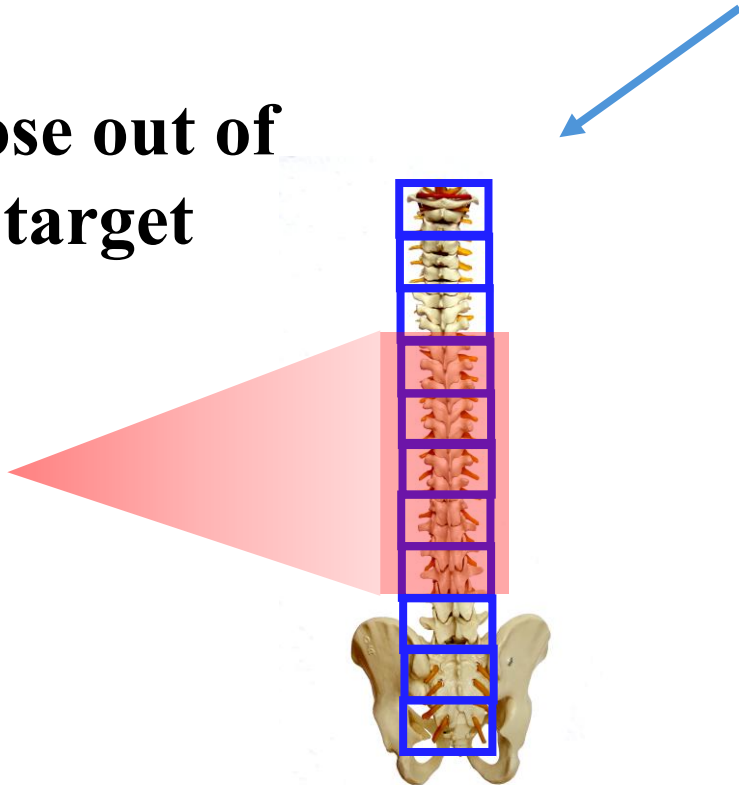


Volume Effect: my ideas

*Critical Element
model*

$$\text{NTCP} = 1 - \left[1 - \left(1 - e^{-\alpha nd} - \beta nd^2 \right)^k \right]^{\frac{L}{L1}}$$

**Dose out of
target**

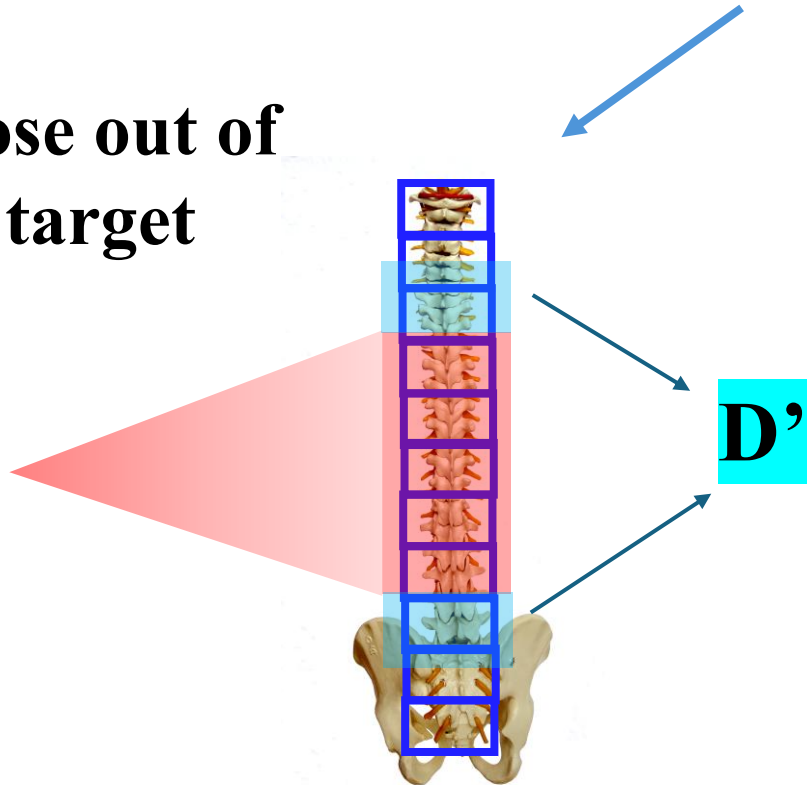


Volume Effect: my ideas

*Critical Element
model*

$$\text{NTCP} = 1 - \left[1 - \left(1 - e^{-\alpha nd} - \beta nd^2 \right)^k \right]^{\frac{L}{L1}}$$

**Dose out of
target**

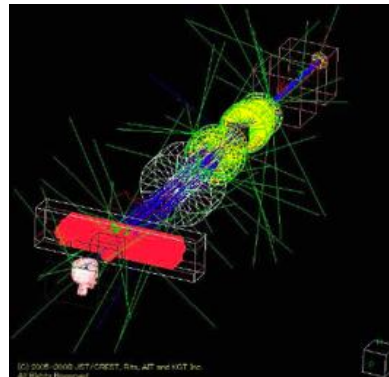
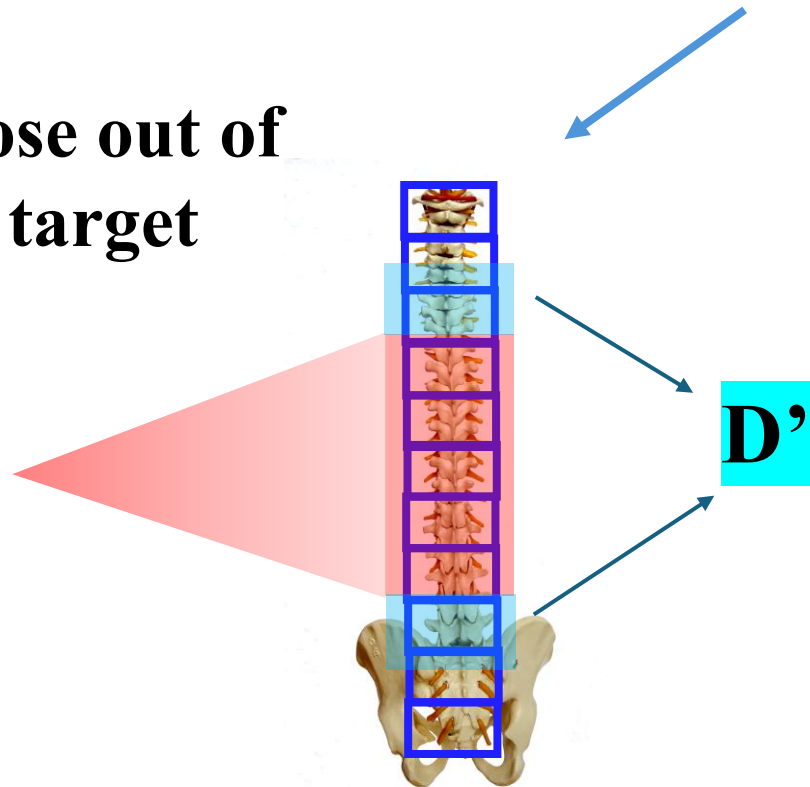


Volume Effect: my ideas

*Critical Element
model*

$$\text{NTCP} = 1 - \left[1 - \left(1 - e^{-\alpha nd} - \beta nd^2 \right)^k \right]^{\frac{L}{L1}}$$

**Dose out of
target**



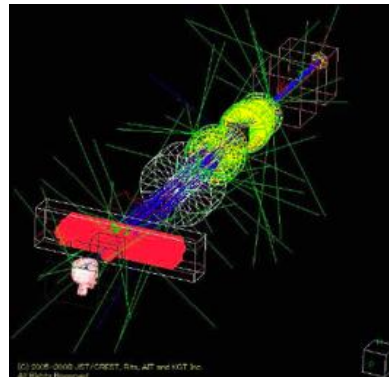
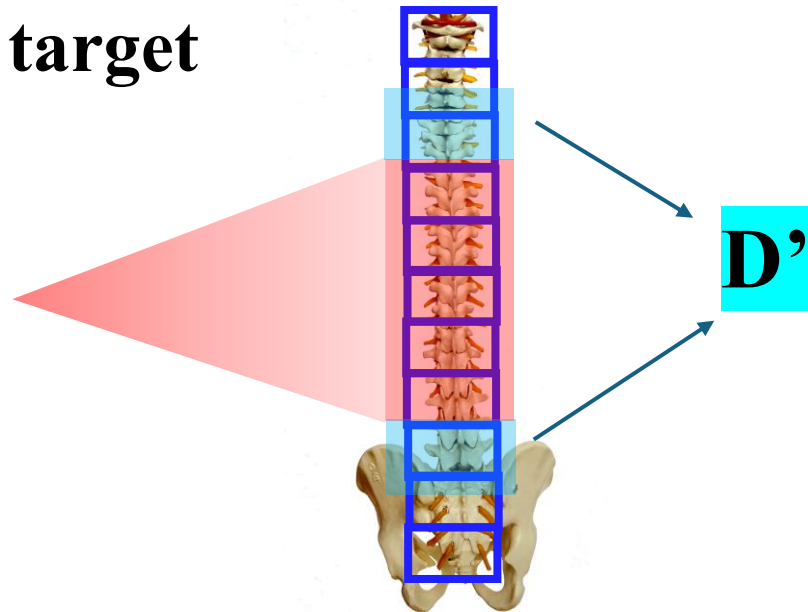
Volume Effect: my ideas

*Critical Element
model*

$$\text{NTCP} = 1 - \left[1 - \left(1 - e^{-\alpha nd} - \beta nd^2 \right)^k \right]^{\frac{L}{L_1}}$$

**Dose out of
target**

**Cell
migration
probability**

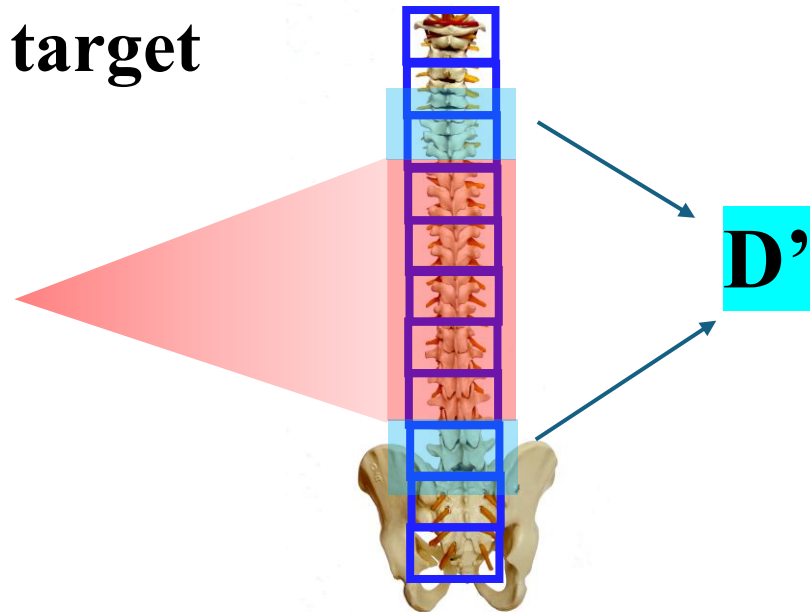


Volume Effect: my ideas

*Critical Element
model*

$$\text{NTCP} = 1 - \left[1 - \left(1 - e^{-\alpha nd} - \beta nd^2 \right)^k \right]^{\frac{L}{L1}}$$

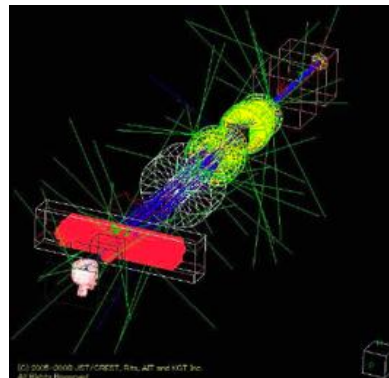
**Dose out of
target**



*From
experiment
 $d_c \sim 2 \text{ mm}$*

**Cell
migration
probability**

$\propto d_c$
critical distance

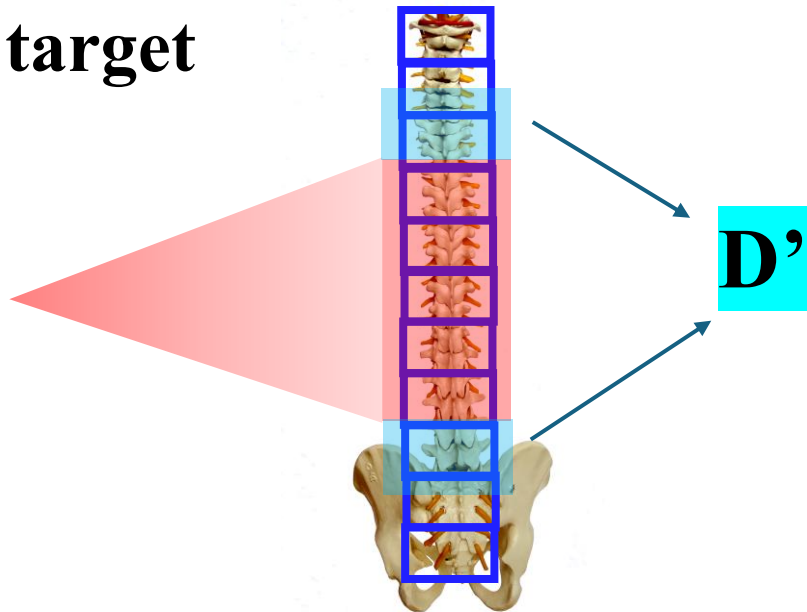


Volume Effect: my ideas

*Critical Element
model*

$$\text{NTCP} = 1 - \left[1 - \left(1 - e^{-\alpha nd} - \beta nd^2 \right)^k \right]^{\frac{L}{L1}}$$

**Dose out of
target**

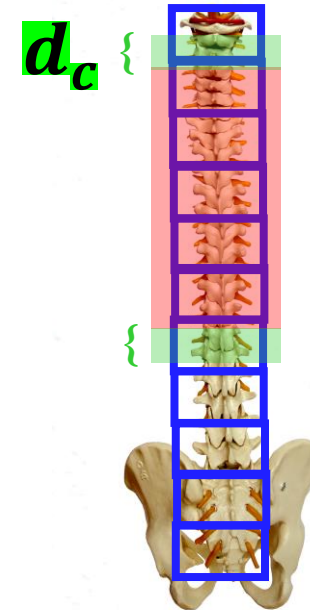


*From
experiment
 $d_c \sim 2 \text{ mm}$*



**Cell
migration
probability**

$\propto d_c$
critical distance



Take home messages

Our approach

[**A. Casali** et al., Phys. Med. Biol., **2024**]

[**A. Casali** et al., European Physical Journal Special Topics., submitted, **2025**]

Take home messages

Our approach

[A. Casali et al., Phys. Med. Biol., **2024**]

[A. Casali et al., European Physical Journal Special Topics., submitted, **2025**]



Patient-specific
treatment plans



Take home messages

Our approach

[A. Casali et al., Phys. Med. Biol., **2024**]

[A. Casali et al., European Physical Journal Special Topics., submitted, **2025**]



Patient-specific
treatment plans



NTCP (k , N , α , β)
few parameters

Take home messages

Our approach

[A. Casali et al., Phys. Med. Biol., **2024**]

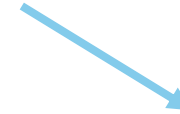
[A. Casali et al., European Physical Journal Special Topics., submitted, **2025**]



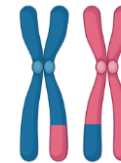
Patient-specific
treatment plans



NTCP (k, N, α, β)
few parameters



BIANCA
for chromosome
damages



Take home messages

Our approach

[A. Casali et al., Phys. Med. Biol., 2024]

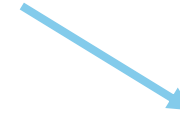
[A. Casali et al., European Physical Journal Special Topics., submitted, 2025]



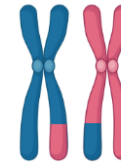
Patient-specific
treatment plans



NTCP (k, N, α, β)
few parameters



BIANCA
for chromosome
damages



Stochastic effects



e.g. radiation-induced
tumours

Take home messages

Our approach

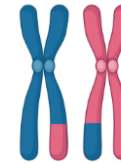
[A. Casali et al., Phys. Med. Biol., 2024]

[A. Casali et al., European Physical Journal Special Topics., submitted, 2025]

Patient-specific
treatment plans



$NTCP (k, N, \alpha, \beta)$
few parameters



BIANCA
for chromosome
damages



Stochastic effects

e.g. radiation-induced
tumours

Worth implementing to make
it as general as possible

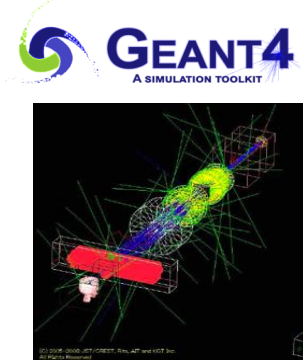
PhD project: detailed steps



PhD project: detailed steps

BIANCA – Geant4

NTCP in
mixed field



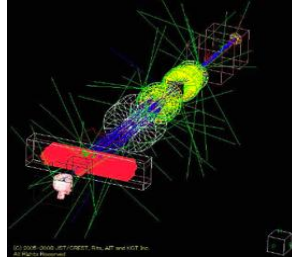
Start

Finish

PhD project: detailed steps

✓ **BIANCA – Geant4**

NTCP in
mixed field



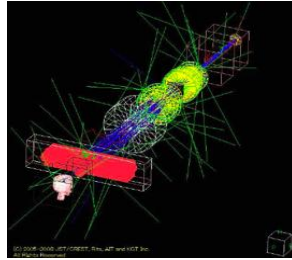
Start

Finish

PhD project: detailed steps

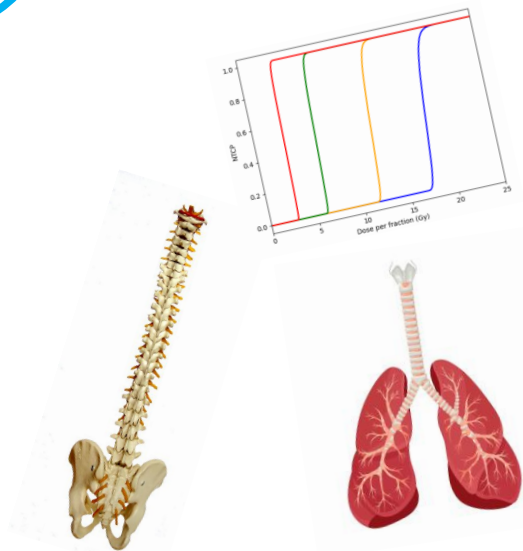
✓ **BIANCA – Geant4**

NTCP in
mixed field



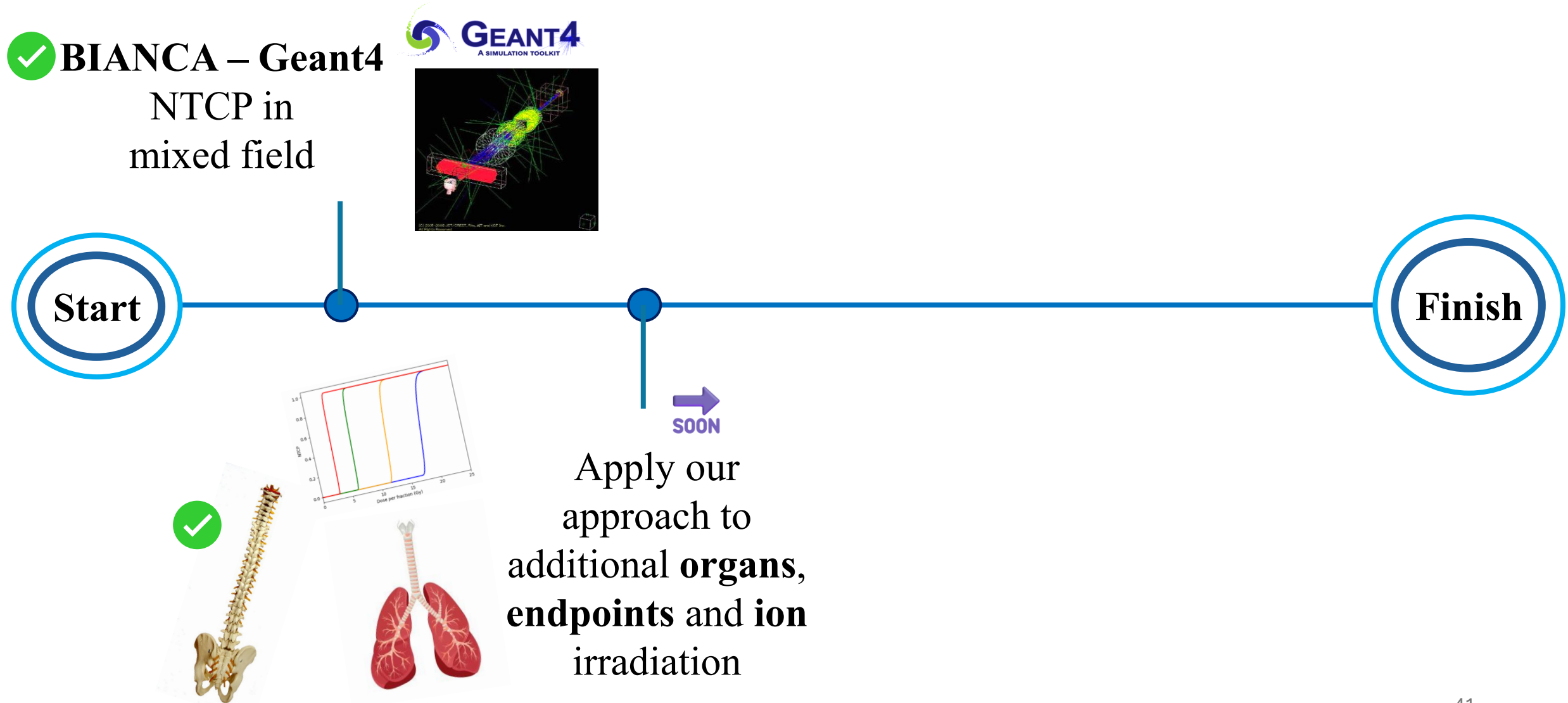
Start

Finish

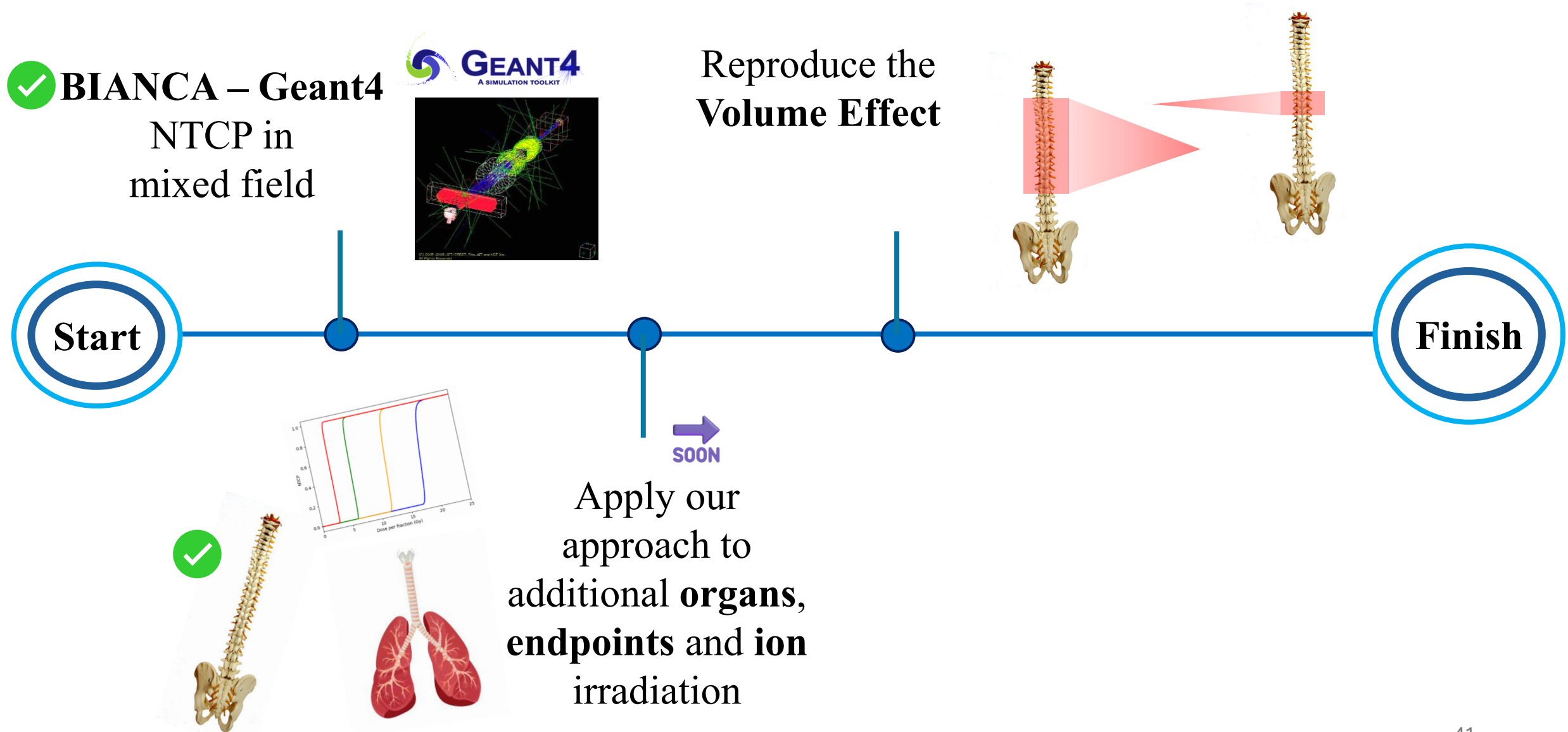


Apply our
approach to
additional **organs**,
endpoints and **ion**
irradiation

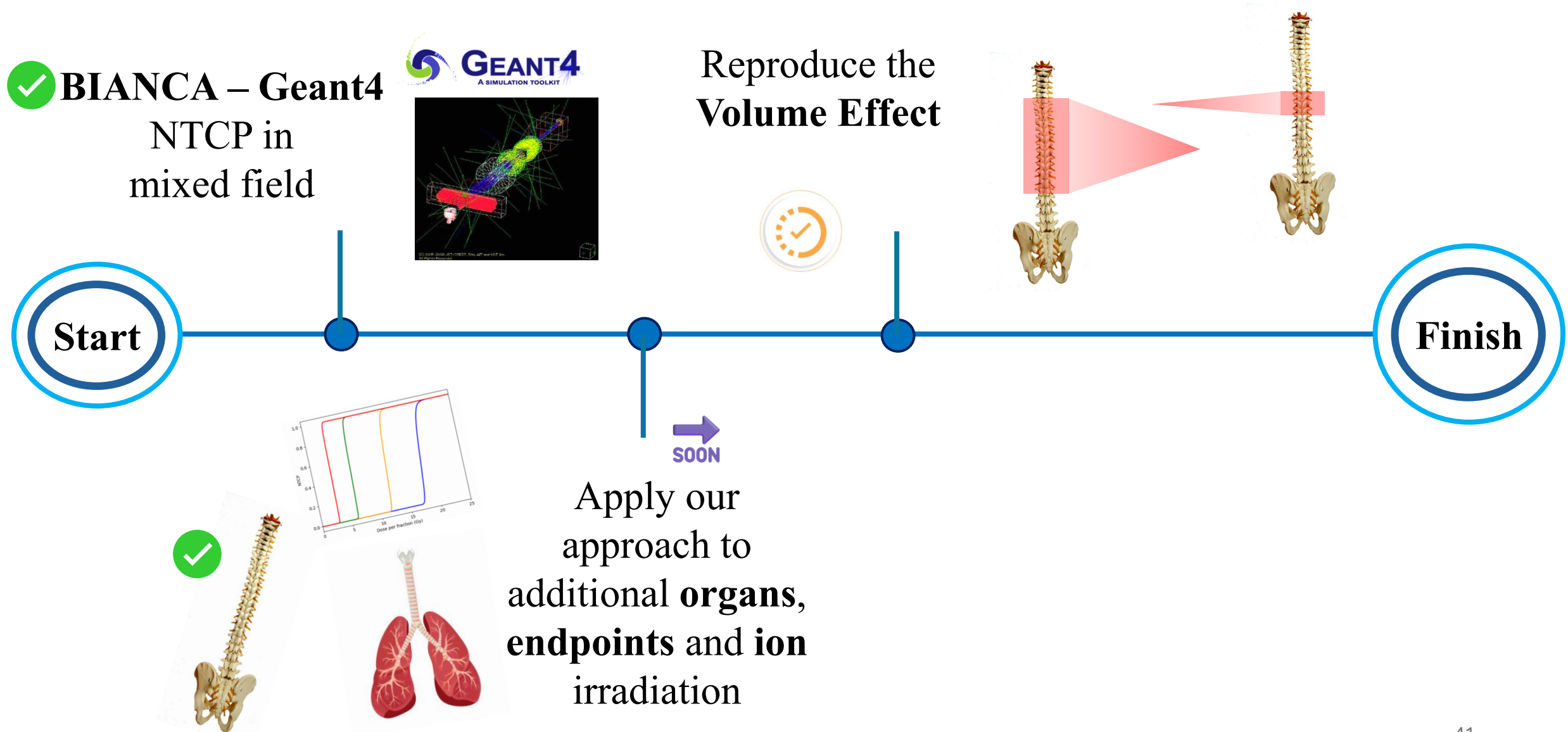
PhD project: detailed steps



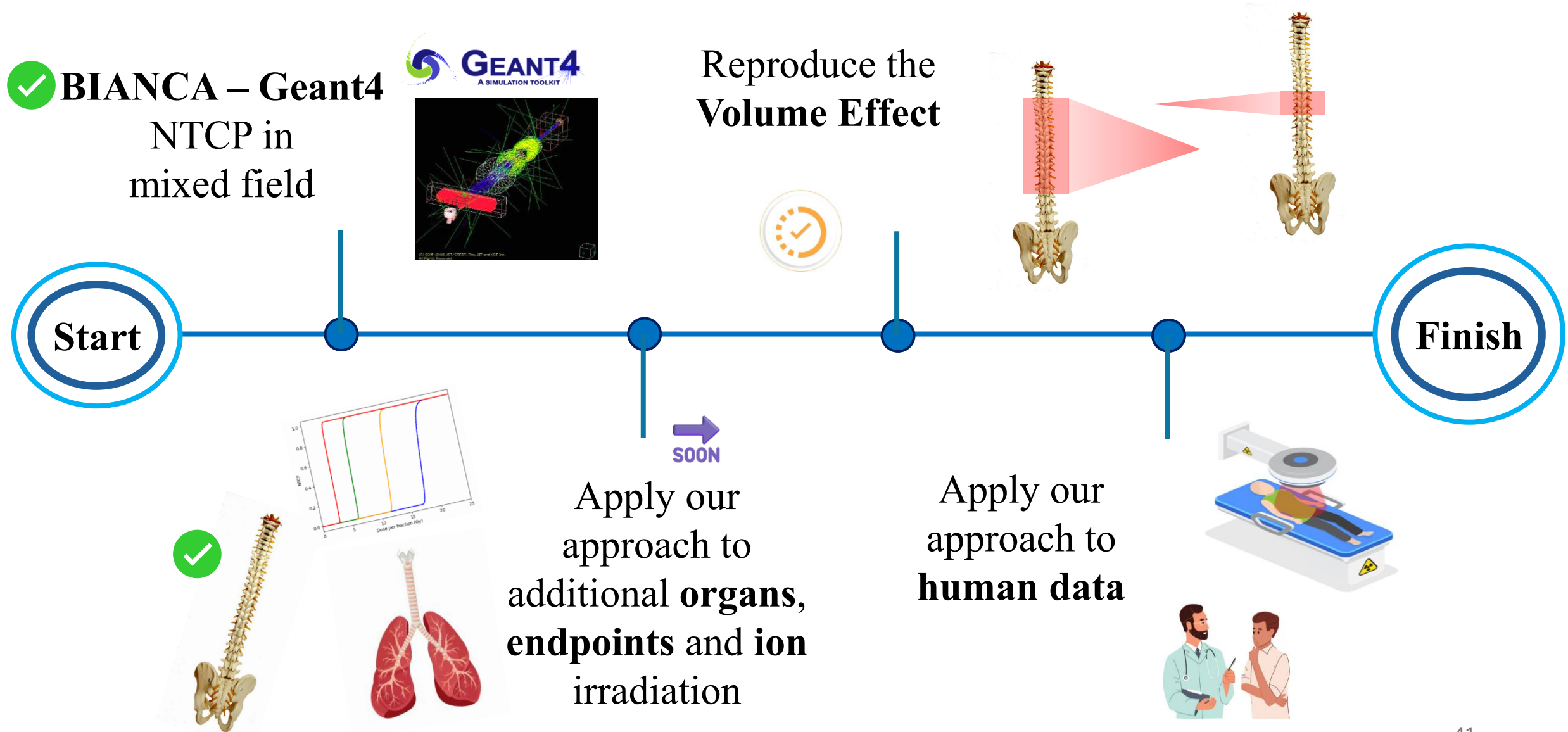
PhD project: detailed steps



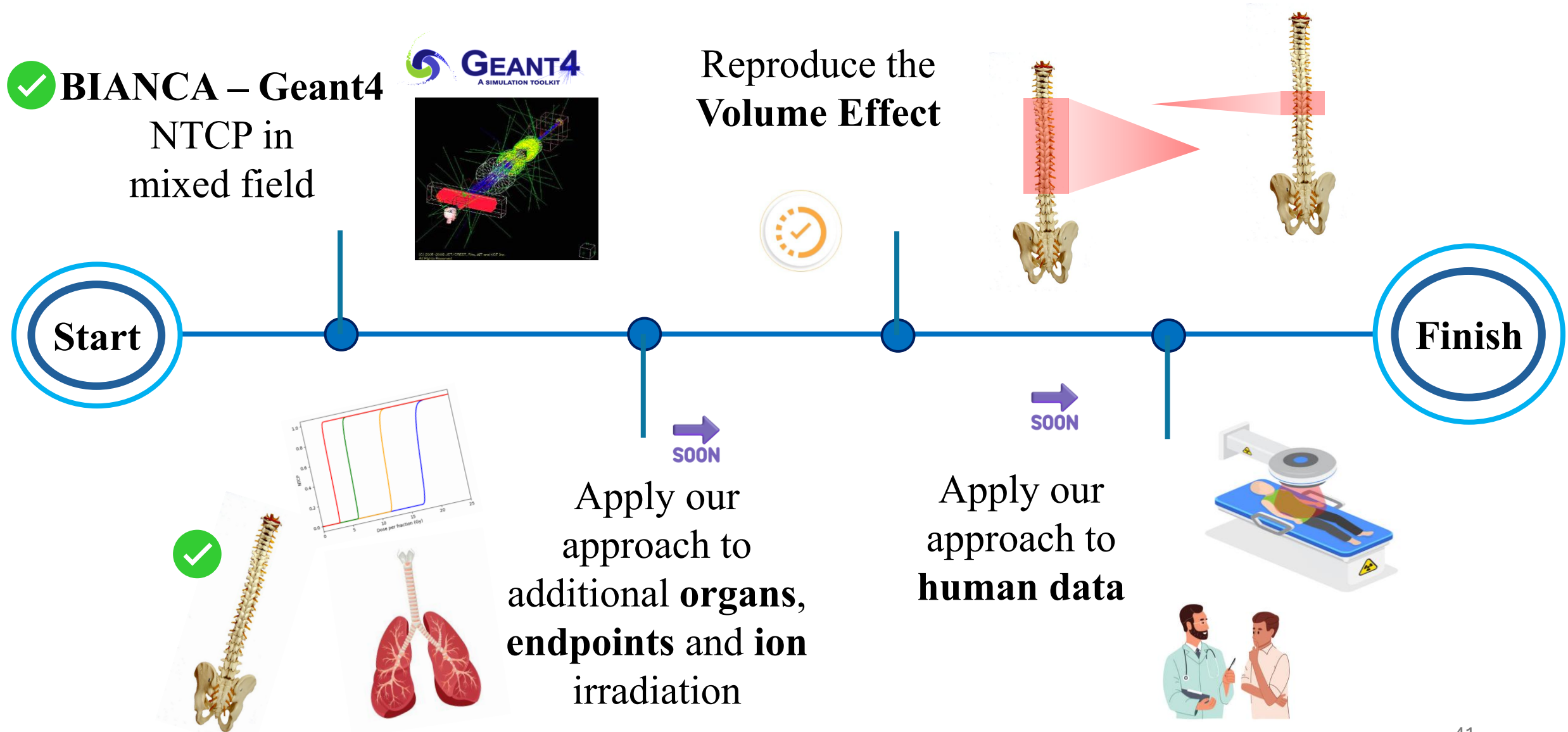
PhD project: detailed steps



PhD project: detailed steps



PhD project: detailed steps

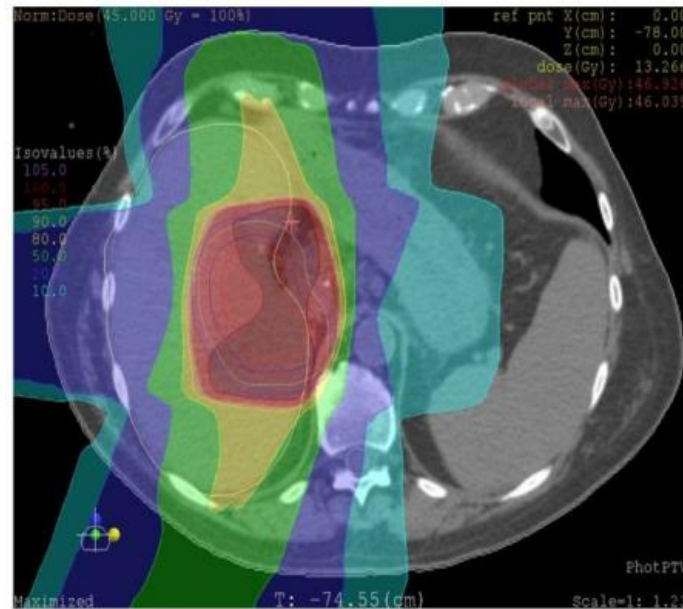


Back up slides

What is Hadrontherapy?

[Image credit: Grant et al., BioMed research international. (2014), 389048. 10.1155/2014/389048]

Photons

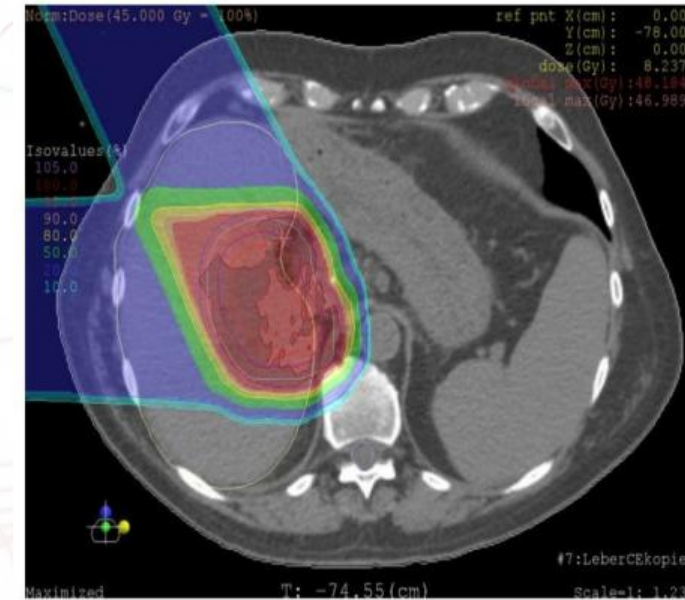


➤ 3 Beams

Normal Tissue

Proton Spread
Out Bragg Peak

➤ 2 Beams



[Image credit: H. Rocken, Vrian Medical Systems]

Depth (cm)

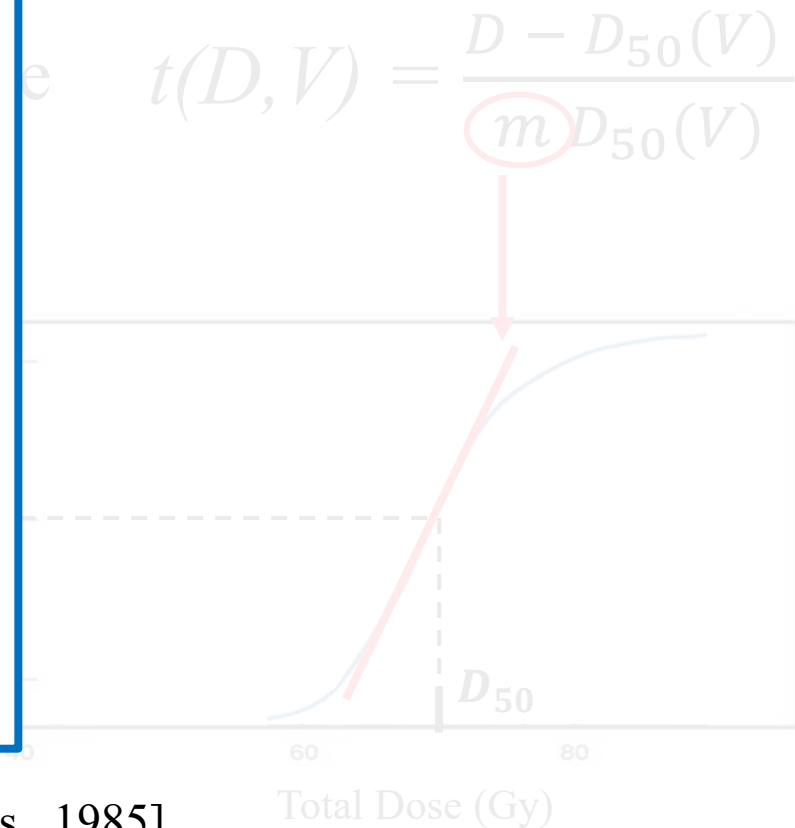
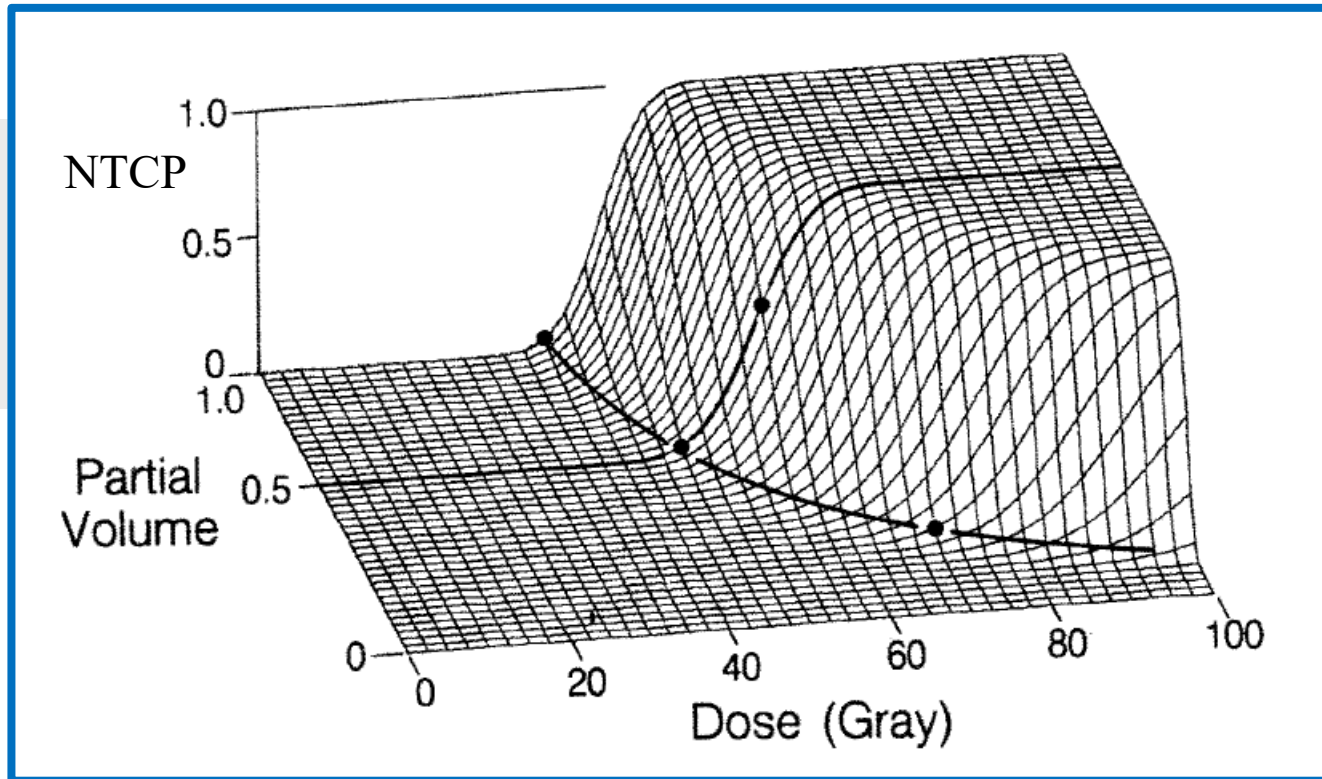
Lyman – Kutcher - Burman (LKB) model

Phenomenological

Assumptions:

$$NTCP(D, V) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^t \exp\left(-\frac{x^2}{2}\right) dx$$

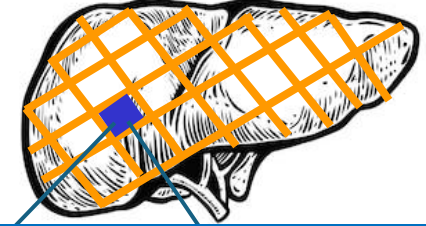
Uniform dose



[J. T. Lyman, Radiat. Res., 1985]

Relative Seriality model

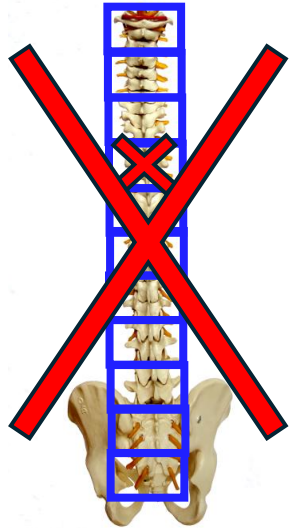
Phenomenological / Mechanistic



$$NTCP(d_i, v_i) = \left\{ 1 - \prod_{i=1}^m \left[1 - \left(e^{-ke^{-\alpha nd_i - \beta nd_i^2}} \right)^s \right]^{v_i} \right\}^{1/s}$$

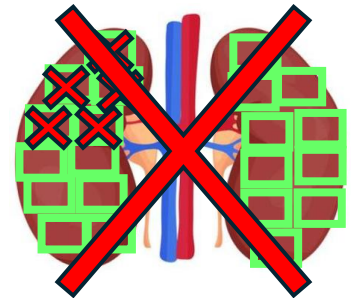
Serial organ $s = 1$

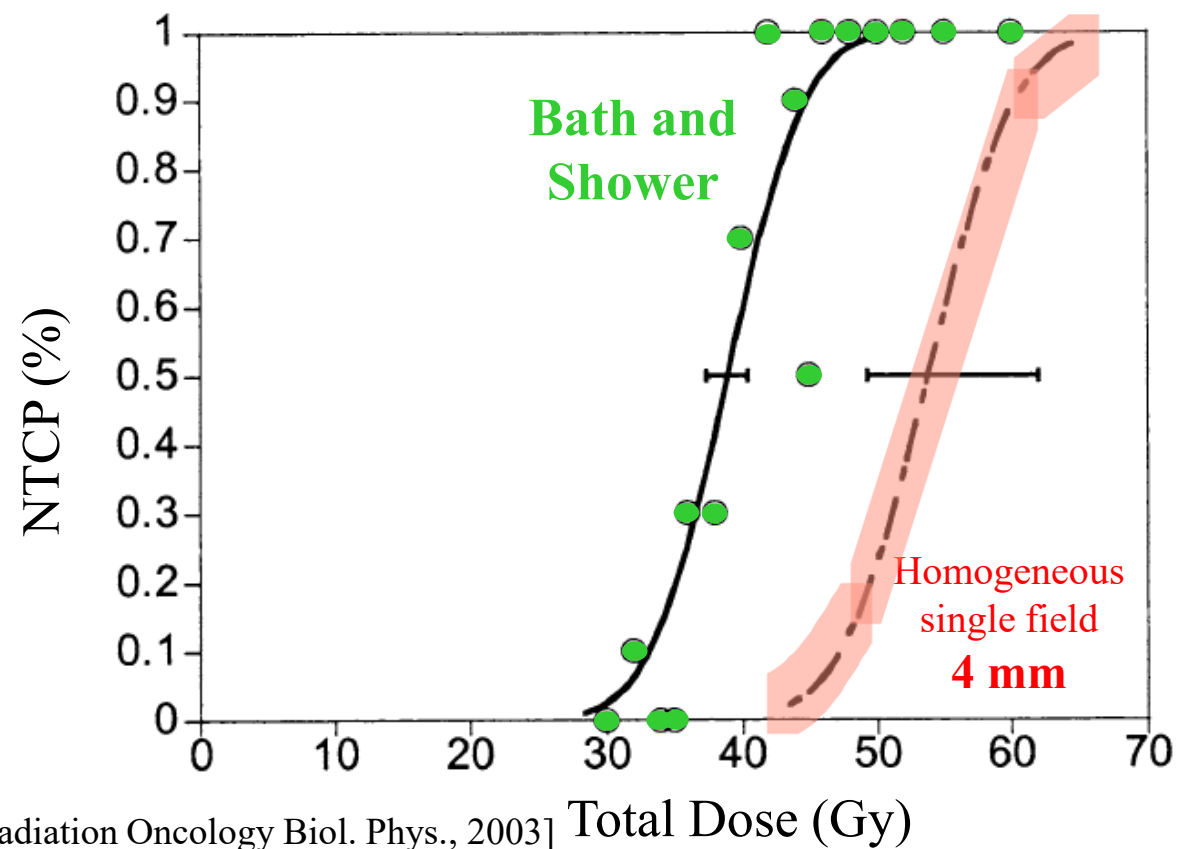
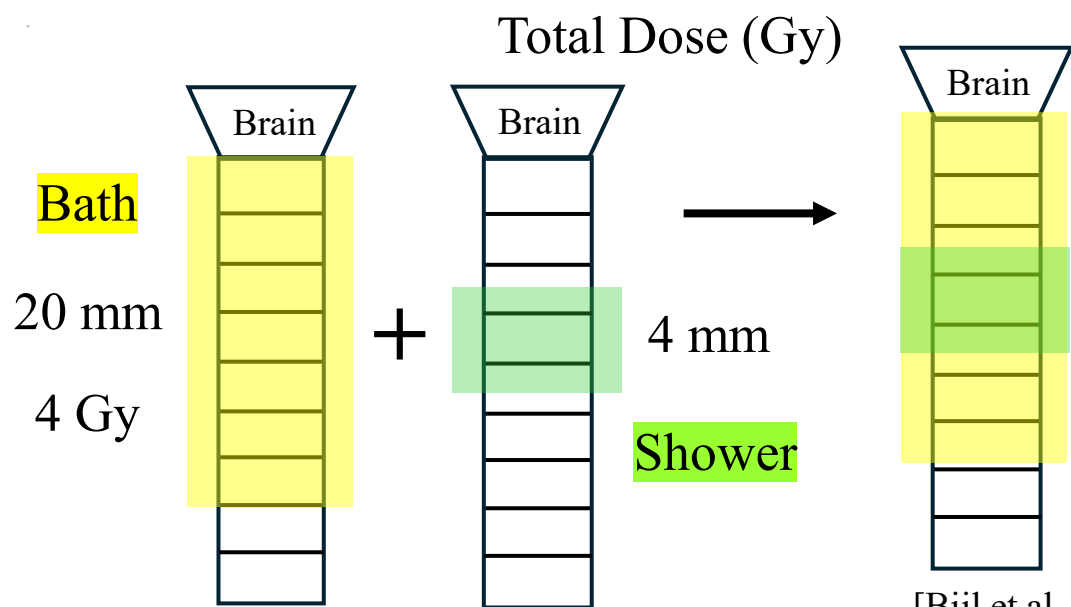
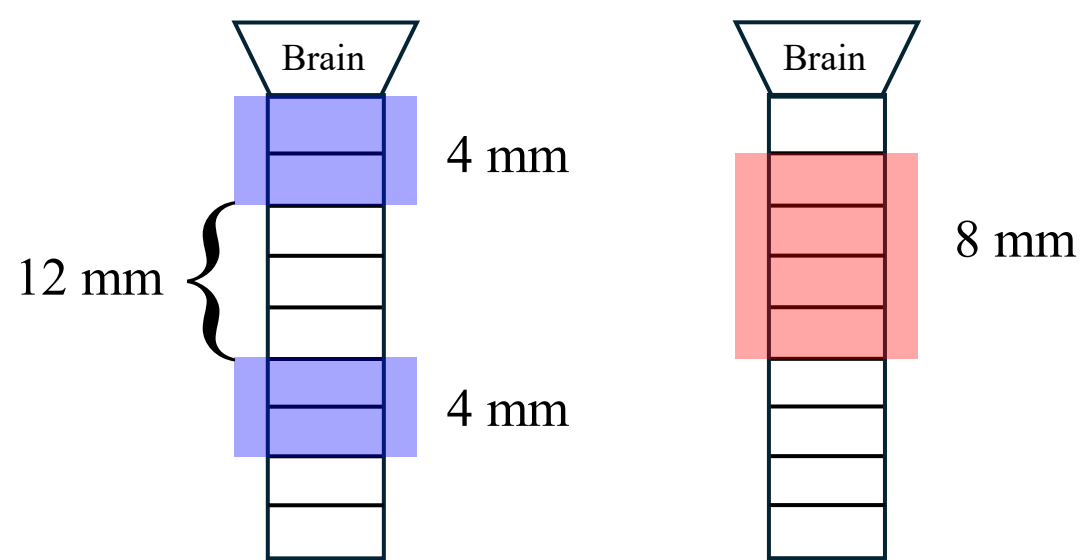
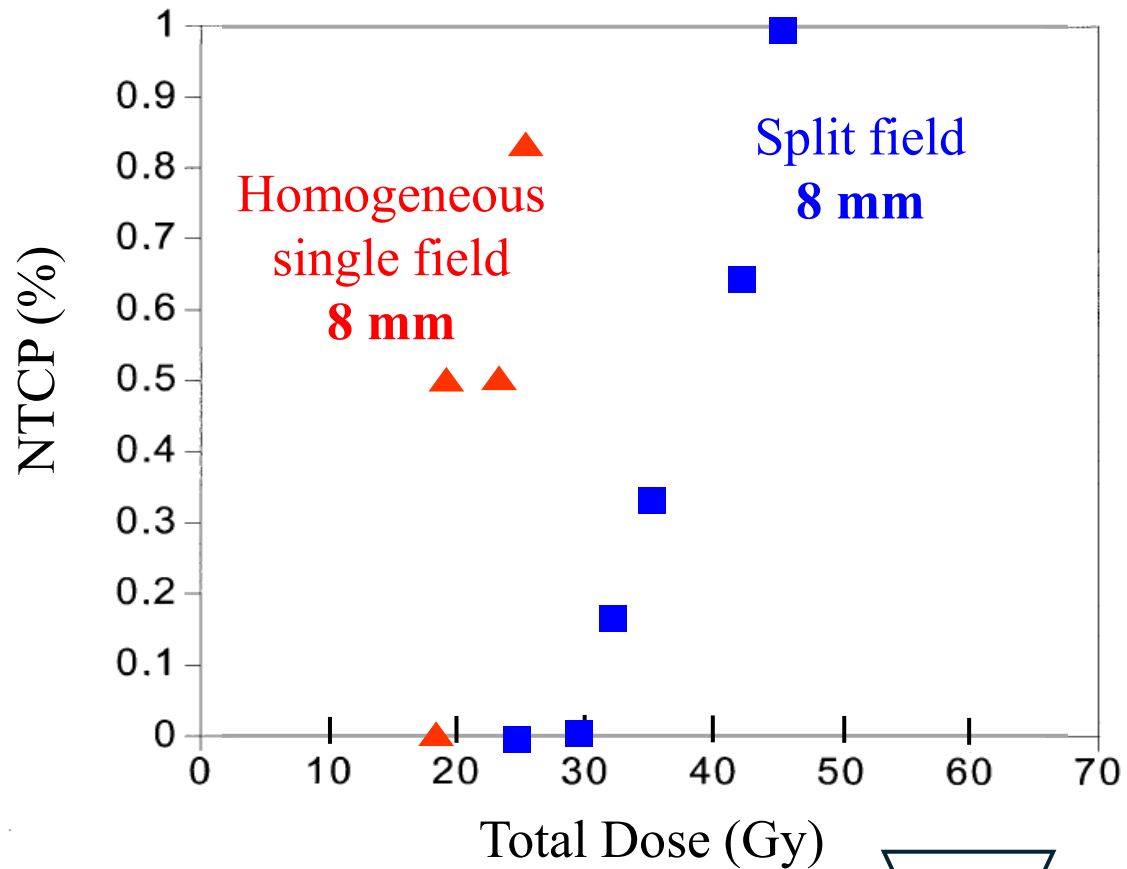
Parallel organ $s \rightarrow 0$



$$P(d_i)_{FSU} = \prod_{i=1}^m [1 - P(d_i)_{FSU}]^{v_i}$$

$$P(d_i)_{FSU} = 1 - \exp \left[\sum_{i=1}^m v_i P(d_i)_{FSU} \right]$$





[Bijl et al., Int. J. Radiation Oncology Biol. Phys., 2003]

Shirato model

*Critical Element
model*

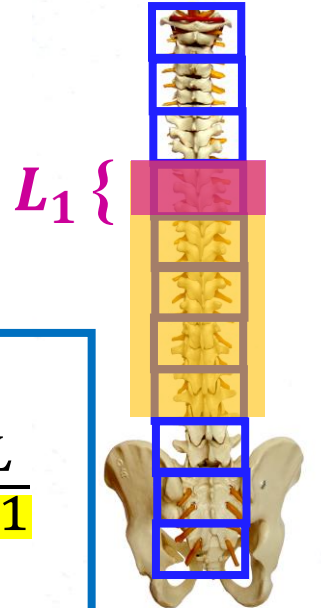
$$\text{NTCP} = 1 - \left[1 - \left(1 - e^{-\alpha nd} - \beta nd^2 \right)^k \right]^{\frac{L}{L_1} N}$$

Prob. to kill 1 cell

NTCP =

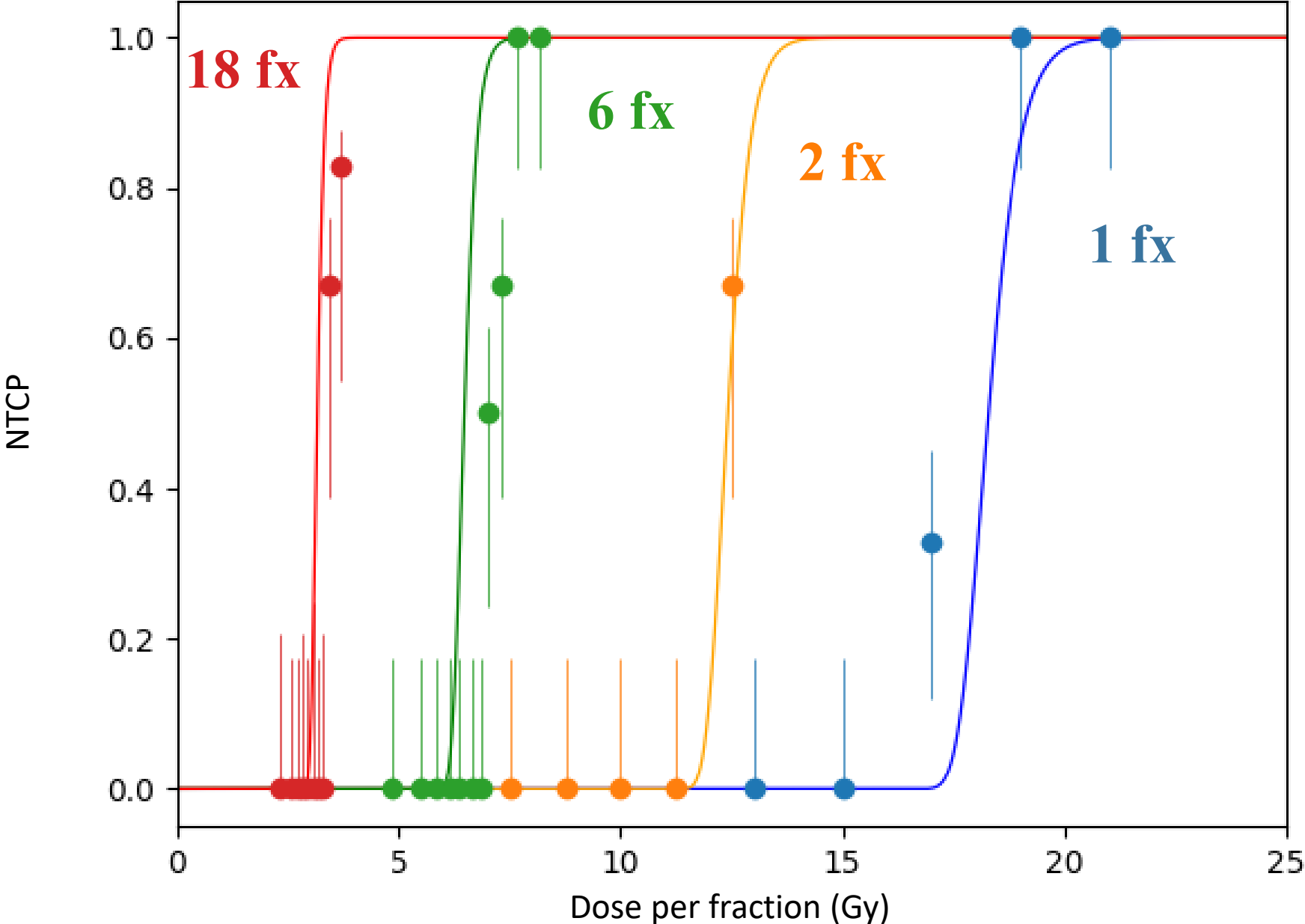
$$= 1 - \left[1 - \left[\left(1 - e^{-\alpha nd} - \beta nd^2 \right) \left(1 - e^{(-\alpha nd - \beta nd^2) N \cdot I} \right) \right]^k \right]^{\frac{L}{L_1}}$$

Migration term



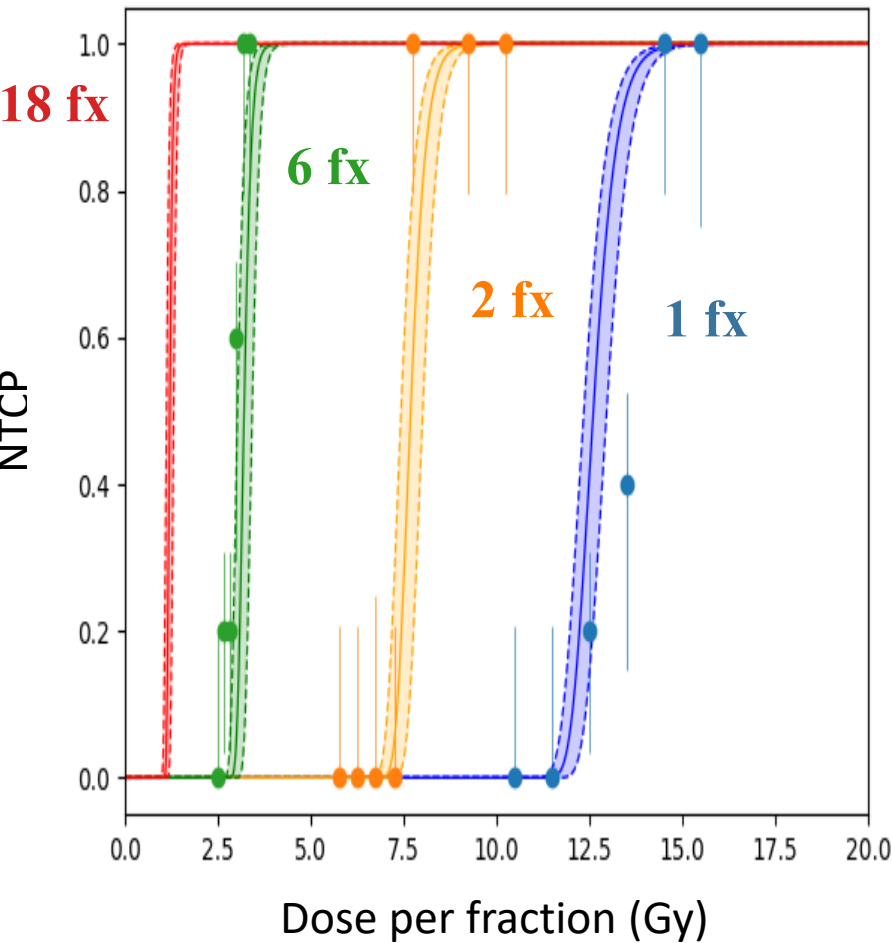
Carbon ions 13 keV/μm

Monochromatic
Field

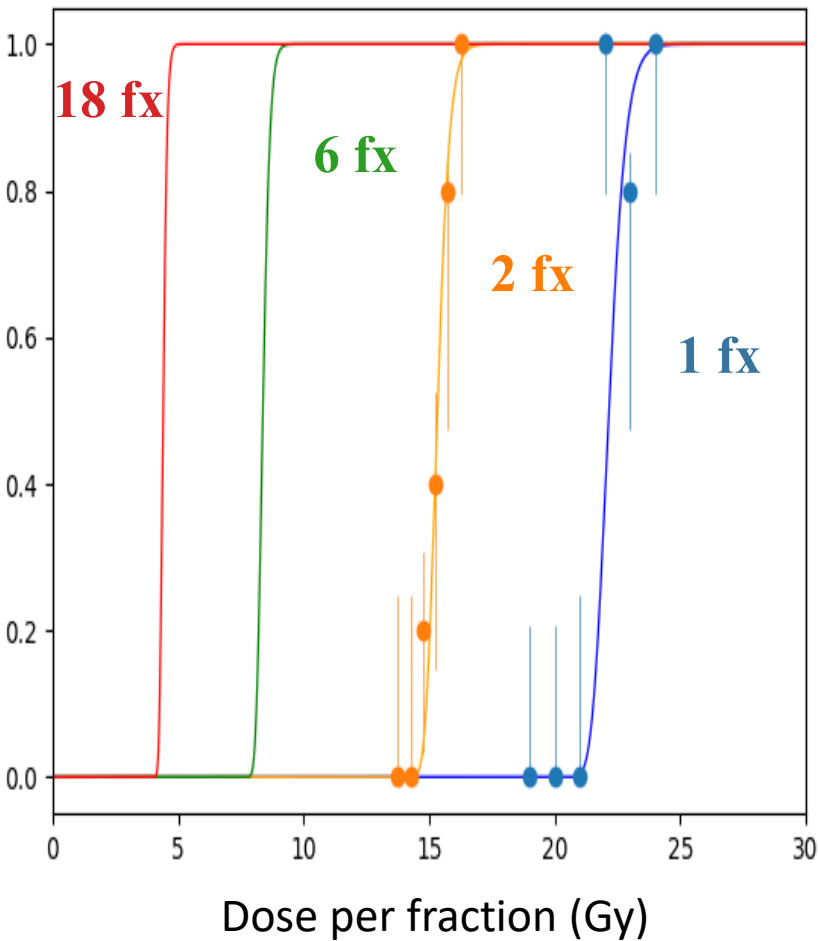


Monochromatic Field

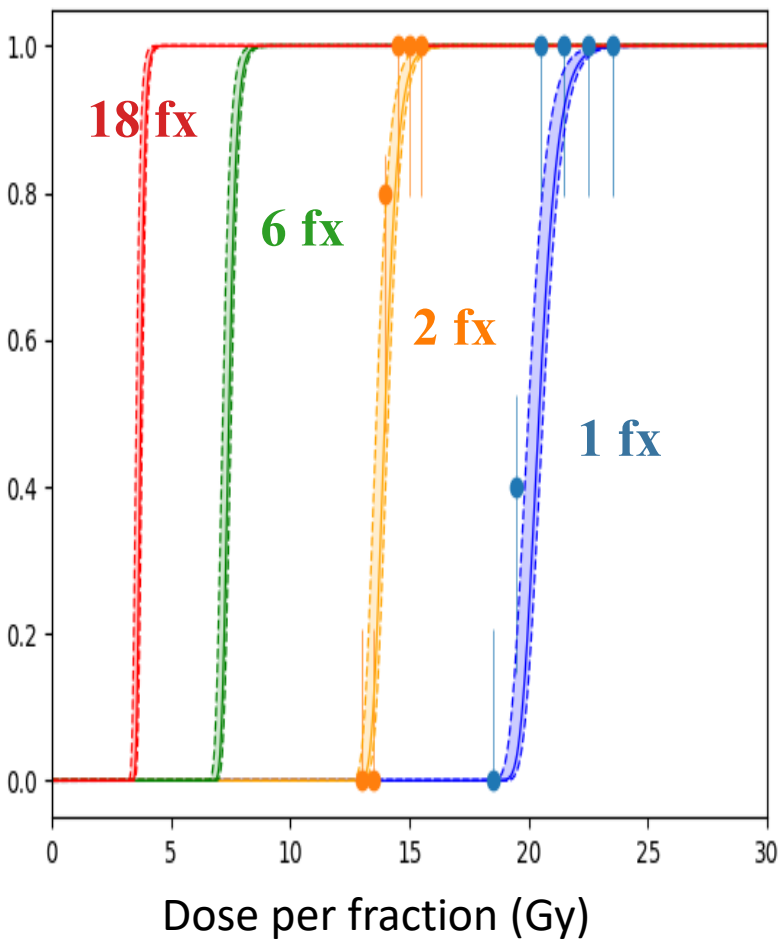
Carbon ions 99 ± 13 keV/μm



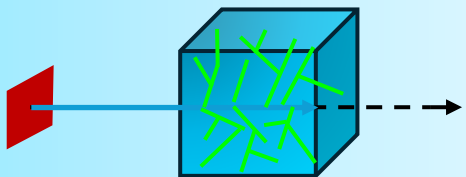
Helium ions 2.9 keV/μm



Protons 5.5^{+1.6}_{-0.6}



2



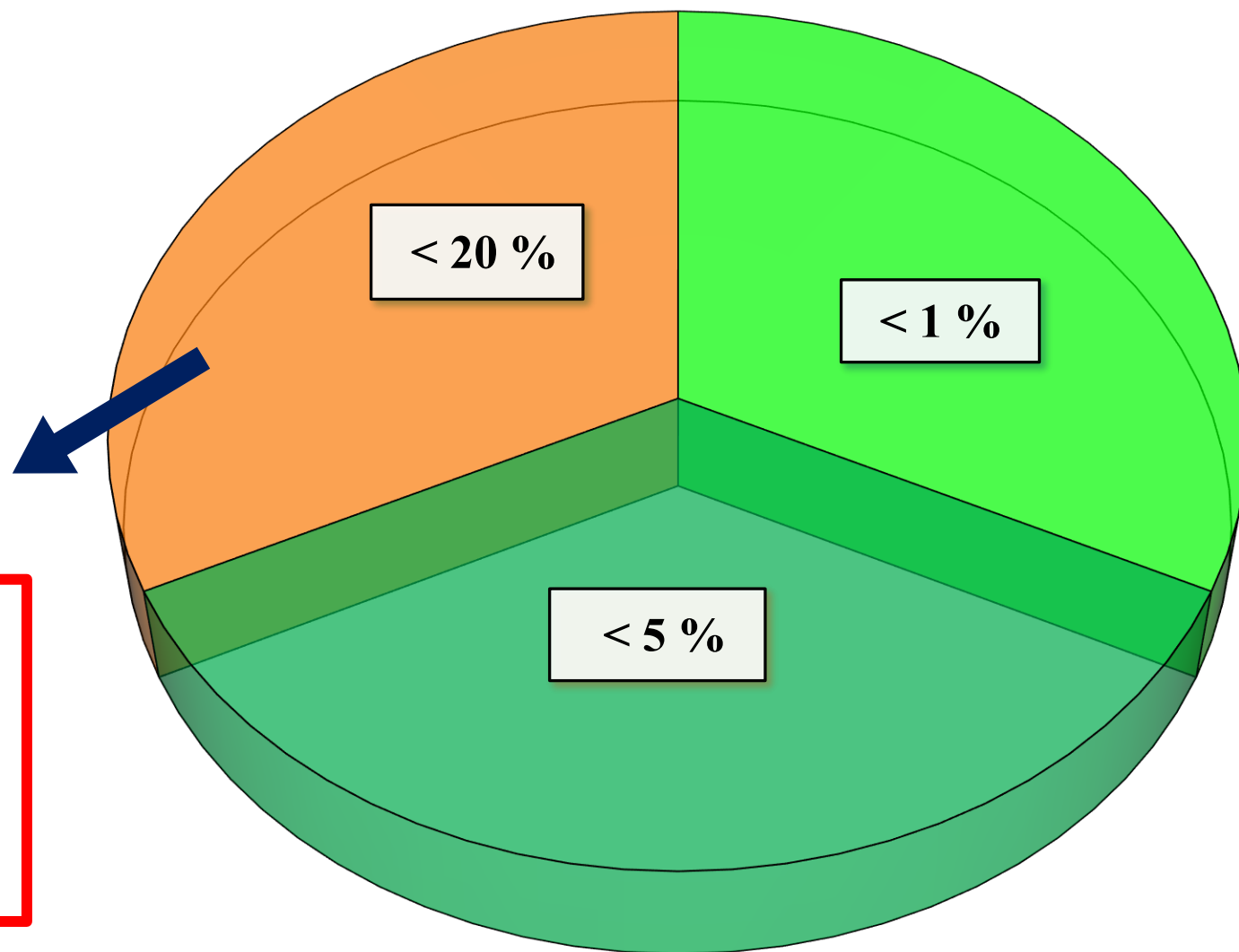
Statistical analysis

Real Mixed Field

$$\frac{|D_{50}^{mixed} - D_{50}^{mono}|}{D_{50}^{mono}} \times 100$$

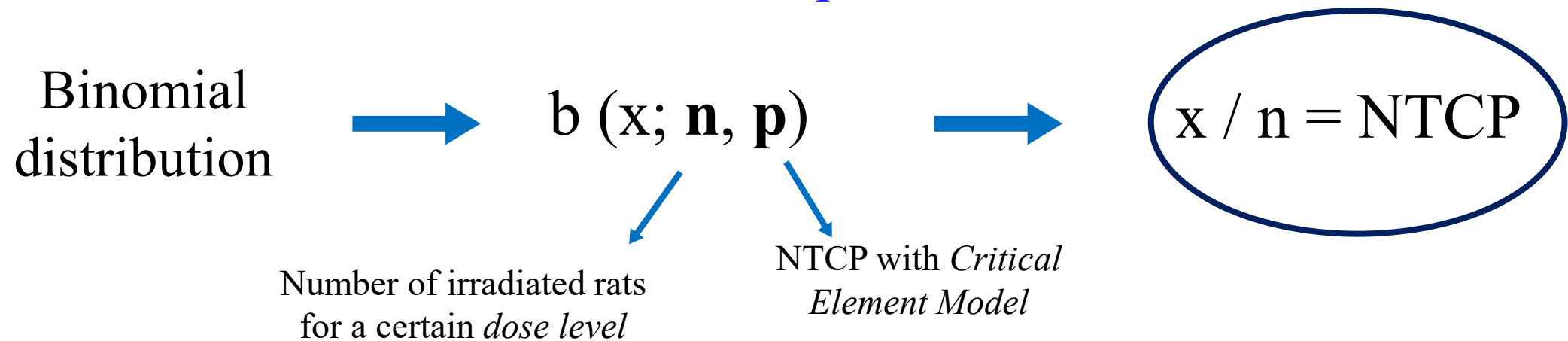
C ions high LET

47 / 56 **NOT** significant
difference mono - mixed



MC simulation for p-values

1. NTCP simulated experimental data:



2. N repeated extractions

MC simulation for p-values

3. χ^2_R between simulated NTCP and NTCP predicted with the model

4. Count $\chi^2_{R_{sim}} > \chi^2_{R_{sperim}}$ (c)

5. Divide c for the repetition number (N)



P-value

P-values

p - value > 5%



Particella	LET (keV /μm)	<i>p-values</i> (%)	
Ioni carbonio	13	—	2.9
	16	—	1.3
	21	↑	18.5
	36	↑	5.6
	45	↑	20.6
	66 ± 6	—	3.3
	99 ± 13	↑	15.6
	125 ± 25	↑	59.0

Particella	LET (keV /μm)	<i>p-values</i> (%)	
Protoni	1.4	↑	18.4
	2.7 ± 0.1	↑	47.4
	3.9 ± 0.2	↑	48.4
	5.5 ^{+1.6} _{-0.6}	↑	59.0
Particella	LET (keV /μm)	<i>p-values</i> (%)	
Ioni elio	2.9	↑	30.9
	9.4 ^{+0.6} _{-1.4}	↑	70.8
	14.4 ^{+1.1} _{-1.9}	↑	23.3
	20.7 ^{+7.3} _{-2.2}	↑	89.3

Clopper-Pearson equations

$x =$ n. rats with paresis

$n =$ n. irradiated rats

$$\sum_{k=x}^n \binom{n}{k} p_1^k (1 - \textcircled{p_1})^{n-k} = \frac{1 - CL}{2}$$

$$\sum_{k=0}^x \binom{n}{k} p_2^k (1 - \textcircled{p_2})^{n-k} = \frac{1 - CL}{2}$$

$$\mathbf{X} = \mathbf{0} \quad \longrightarrow \quad p_1 = 0 \quad \quad p_2 = 1 - \sqrt[n]{1 - CL}$$

$$\mathbf{X} = \mathbf{1} \quad \longrightarrow \quad p_1 = \sqrt[n]{1 - CL} \quad \quad p_2 = 1$$

Incomplete Beta Function

$$I_p(x, n - x + 1) = \sum_{k=x}^n \binom{n}{k} p^k (1 - p)^{n-k}$$

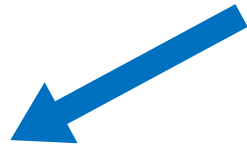
Statistical analysis
Photon fit



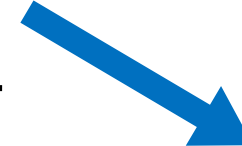
$$\chi_R^2 = 0.49$$

p-value = 89.5 %

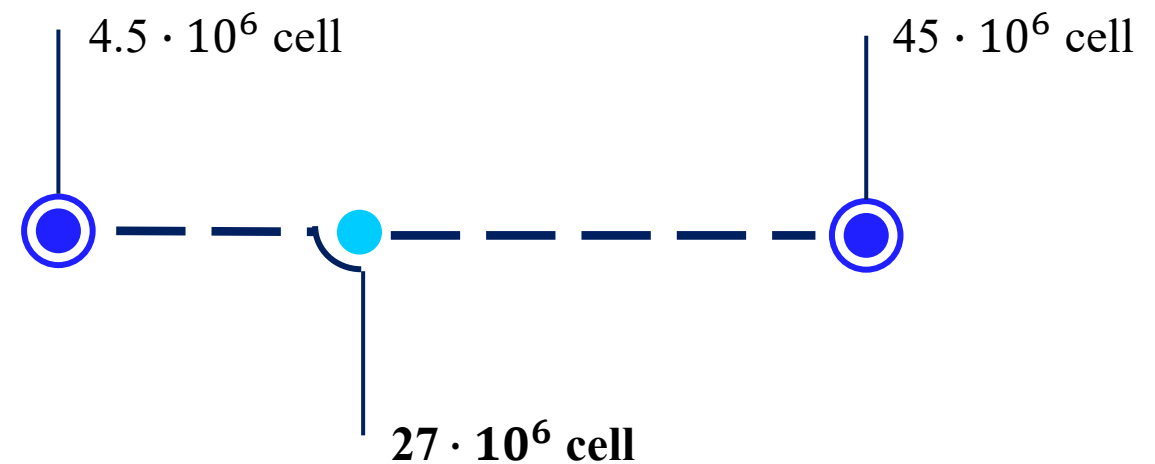
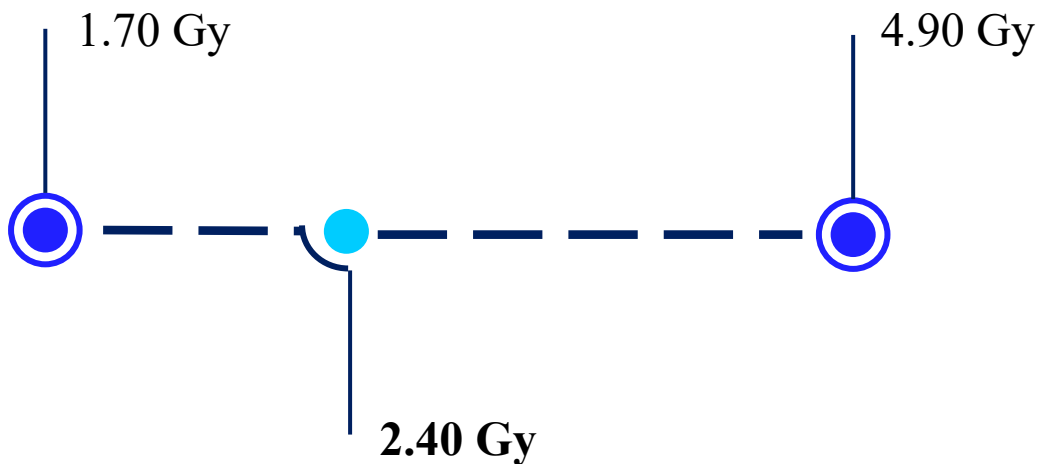
Best-fit parameters



$$\alpha/\beta$$



$$k \cdot N$$

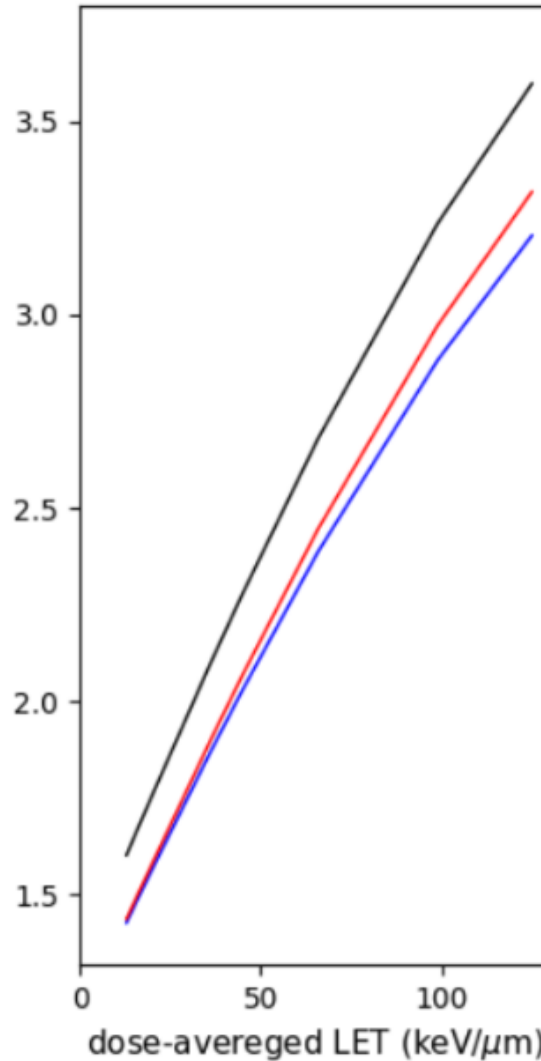
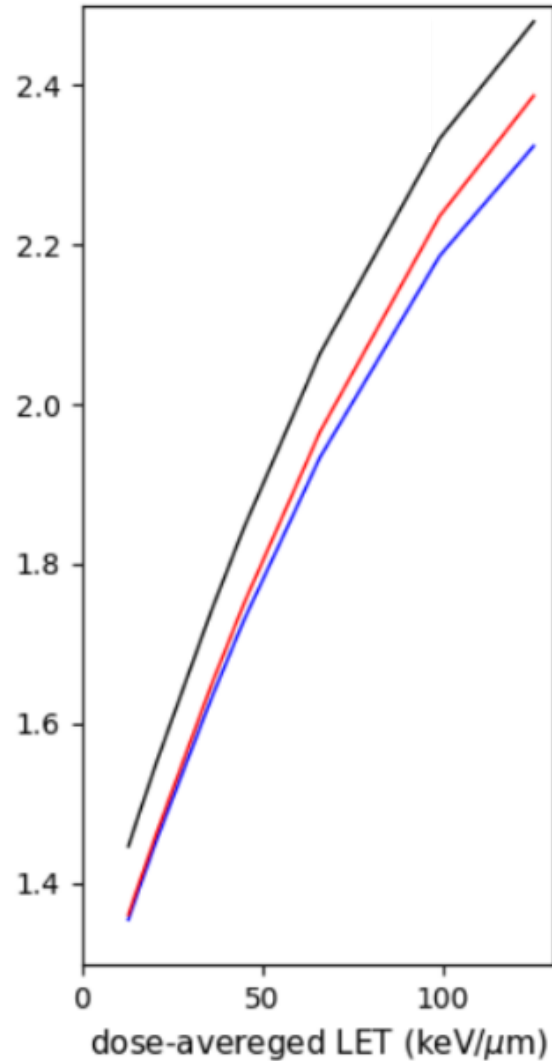
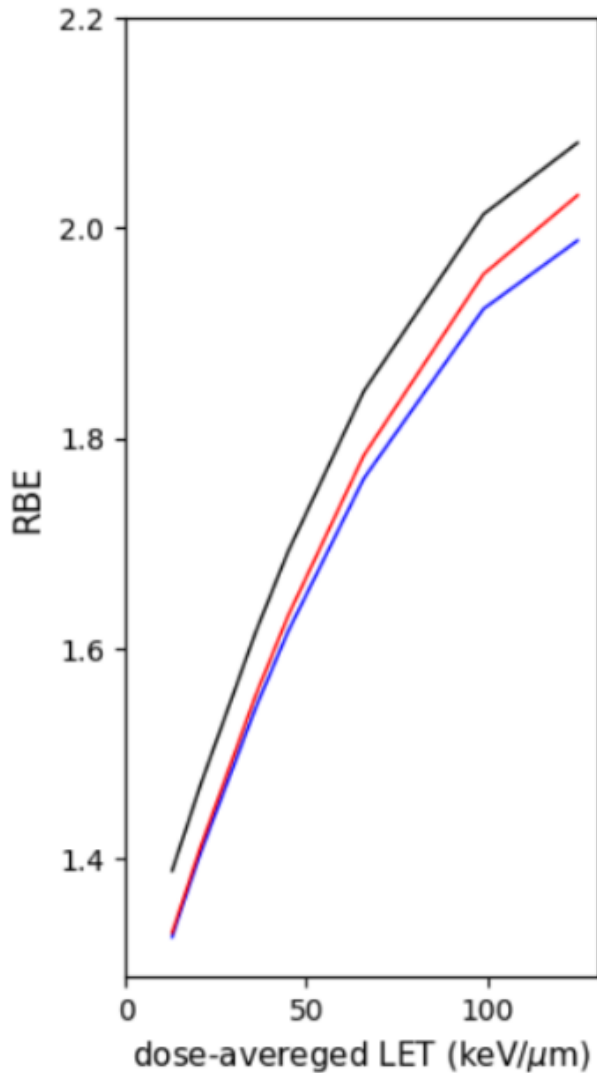


RBE (different *outcome* levels)

Carbon ions 1 fraction

Carbon ions 2 fractions

Carbon ions 6 fractions



RBE with NTCP = 0.5

RBE with NTCP = 0.01

Cell survival RBE

RBE (cfr LEM)

