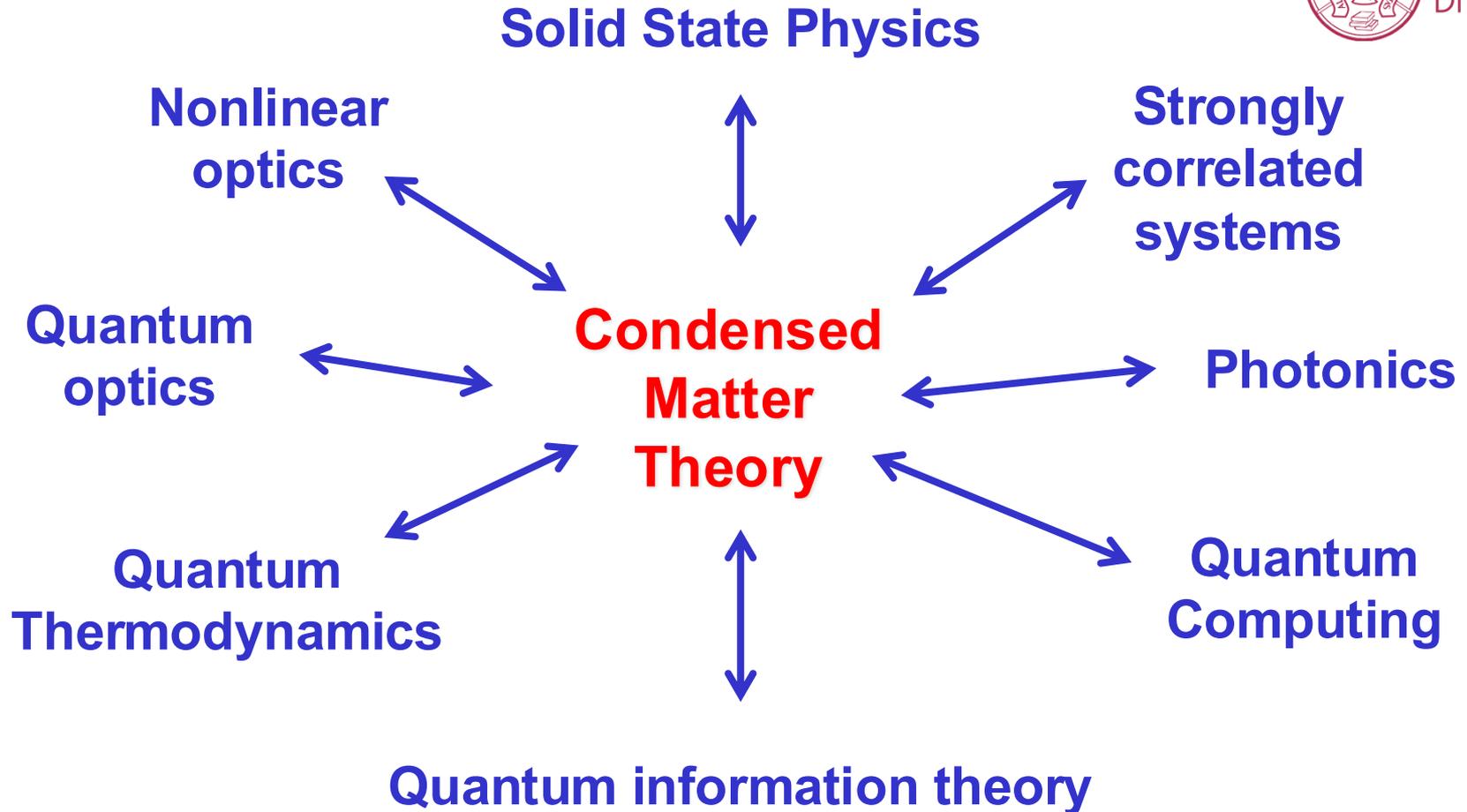


# Fisica Teorica della Materia Condensed Matter Theory

*Dipartimento di Fisica «Alessandro Volta»*

*Istituto Nazionale di Fisica Nucleare*

*Consiglio Nazionale delle Ricerche*



# Research Lines & Coordinators

## Advanced Quantum Mechanics & Quantum Info



**Chiara Macchiavello**



**Lorenzo Maccone**



**Massimiliano Sacchi  
(CNR)**



**Giacomo Guarneri**

## First principles condensed matter theory



**Matteo Cococcioni**

## Quantum Photonics and Nanostructures



**Lucio Andreani**

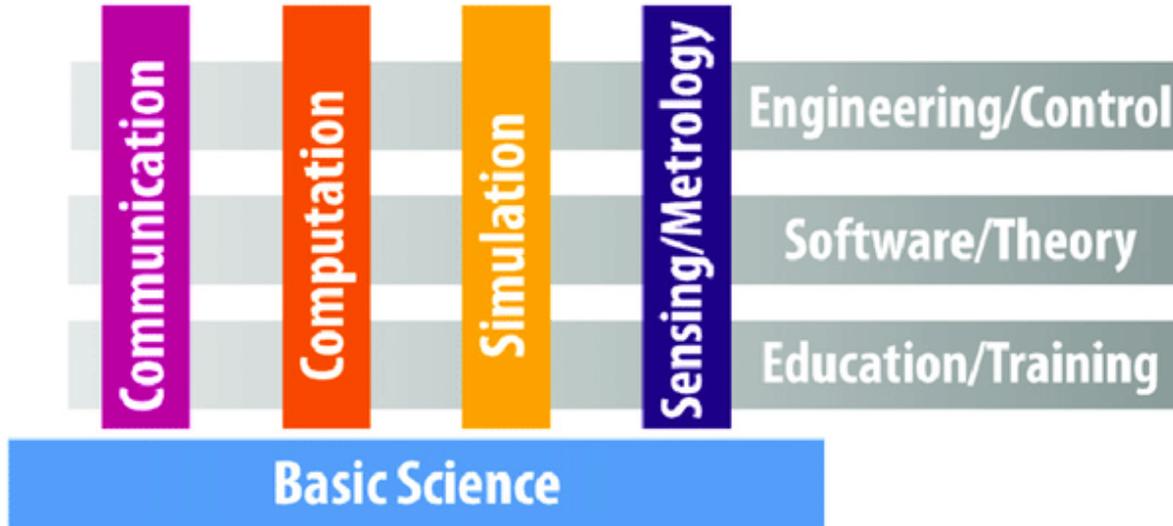


**Dario Gerace**



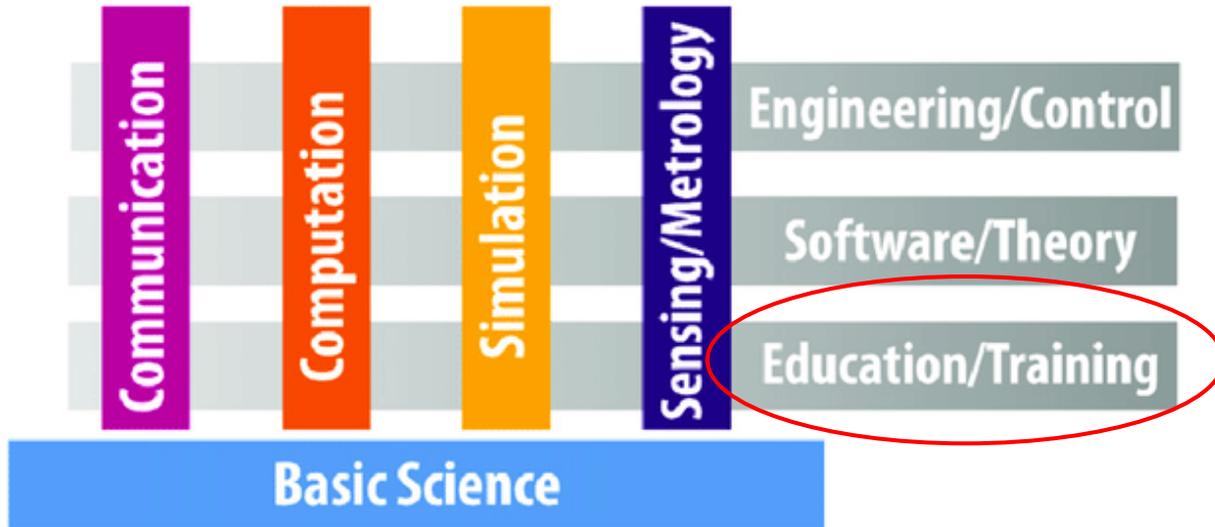
**Marco Liscidini**

# All the related applications in Quantum Technologies



*The quantum technologies roadmap: a European community view,*  
New J. Phys. **20**, 080201 (2018)

# All the related applications in Quantum Technologies



**LM curricula:**

**Fisica della Materia**

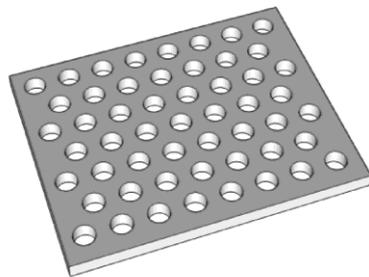
**Fisica delle Tecnologie  
Quantistiche**

*The quantum technologies roadmap: a European community view,*  
New J. Phys. **20**, 080201 (2018)

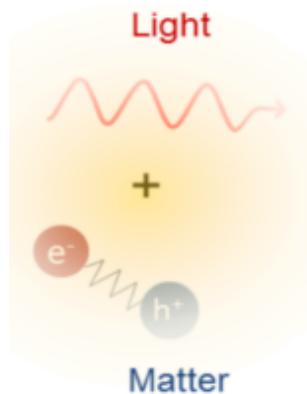


Lucio Andreani

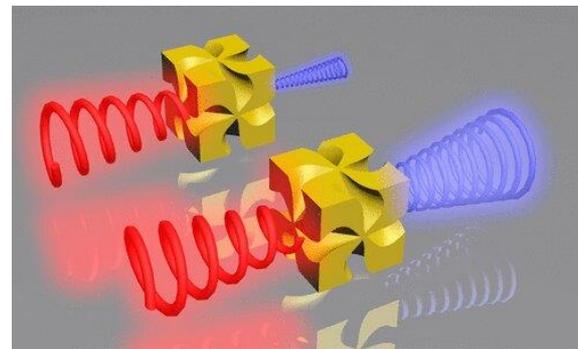
Photonic crystal slabs  
and metasurfaces



Light-matter interaction,  
exciton and polaritons  
(= half wave, half matter:  
mixed modes of the  
electromagnetic field and  
of a material excitation)



Chiral and topological photonics

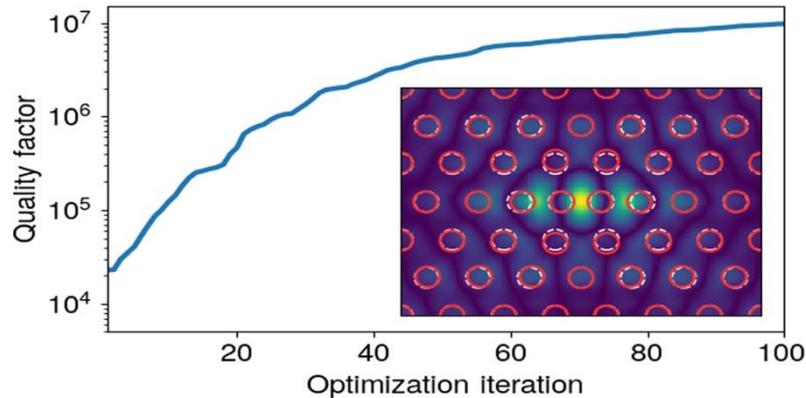


Expt and applications: quantum,  
silicon photonics, optoelectronics

& development of computational  
methods: optimization, inverse  
design...

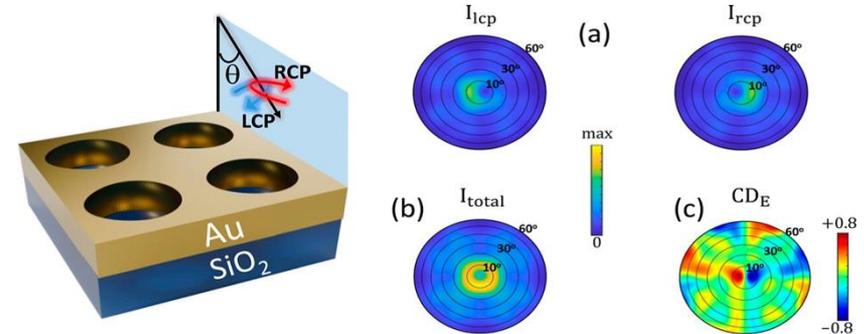
# Recent highlights

Legume: A guided-mode expansion method for photonic crystal slabs for inverse design and light-matter interaction



Poster no 11 (day 1)

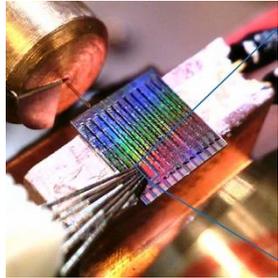
Boosting Chirality with Bound States in the Continuum in Plasmonic Metasurfaces



Posters no 64 & 78 (day 2)

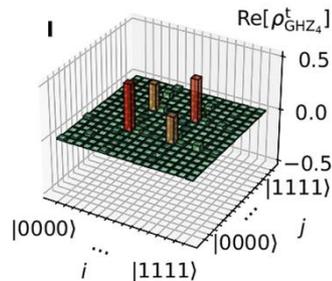
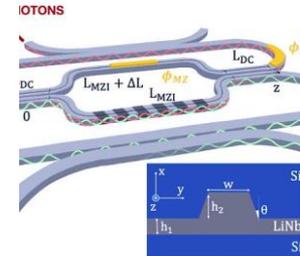
with various colleagues: D. Gerace, S. Zanotti, H. Ali, G. Pellegrini, F. Marabelli, F. Floris...

Marco Liscidini



Classical and  
quantum  
nonlinear  
photonics

Light-matter  
interaction integrated  
photonic systems



Generation and  
characterization of  
quantum states

[liscidini.com](http://liscidini.com)





# Quantum fluids of light

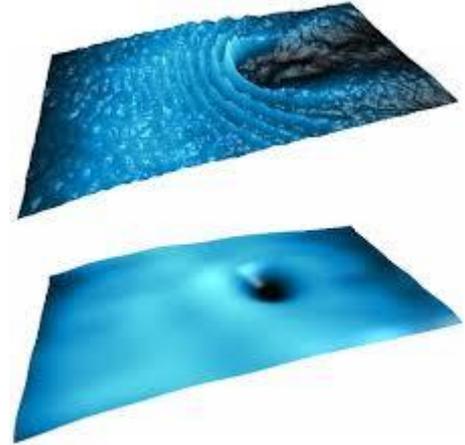
- Emulating the physics of quantum fluids with optical systems



classical fluid



superfluid He

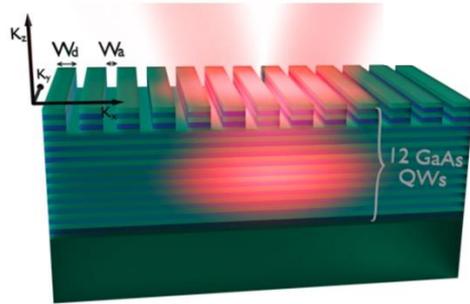


superfluid light

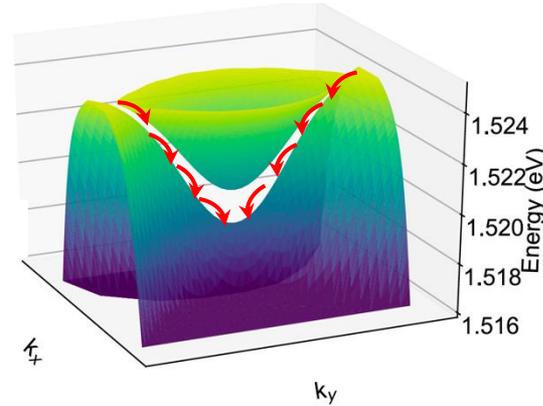
- new physics arising from driven-dissipative nature of photonic systems

# Condensation from a photonic crystal BIC

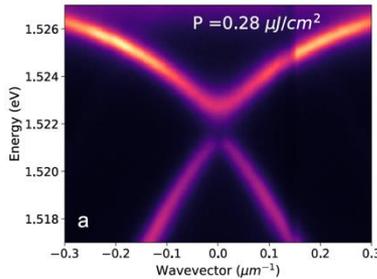
Symmetry-protected BICs at  $\Gamma$   
are supported by 1D gratings



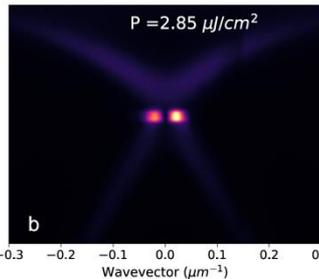
2D lower polariton branches



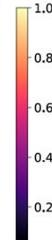
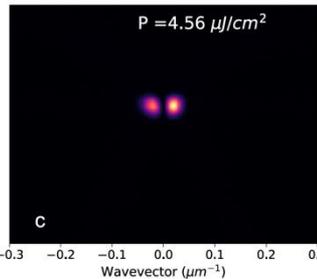
< threshold



@ threshold



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Ardizzone et al., Nature **605**, 447 (2022)

Nigro & Gerace, PRB **108**, 085305 (2023)

Riminucci et al., PRL **131**, 246901 (2023)

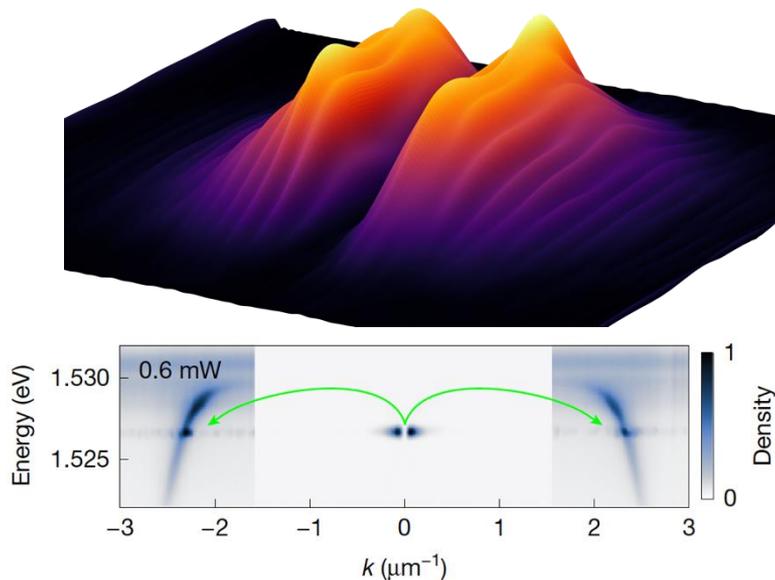
Collaboartion with CNR-Nanotec



# Recent highlights



D. Nigro, D. Trypogeorgos, A. Gianfrate, D. Sanvitto, I. Carusotto, D. Gerace,  
*Supersolidity of Polariton Condensates in Photonic Crystal Waveguides*,  
Phys. Rev. Lett. **134**, 056002 (2025)

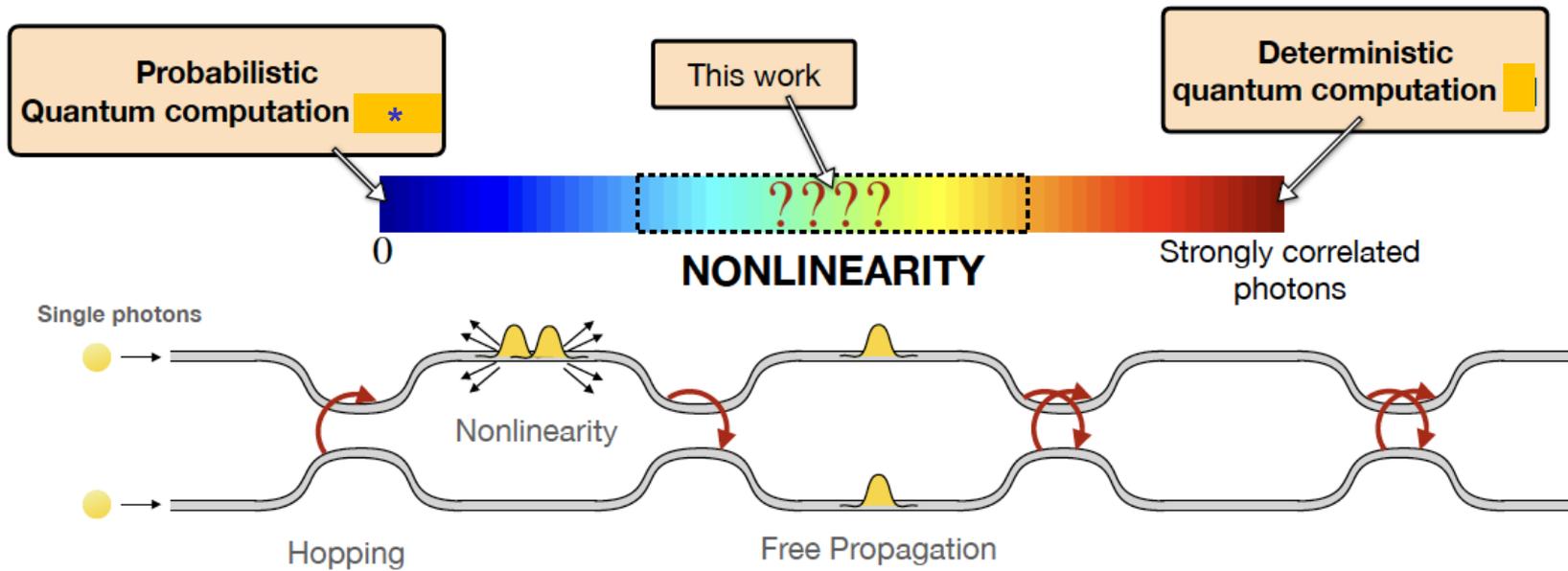


D. Trypogeorgos et al.,  
*Emergent supersolidity in Photonic  
Crystal Polariton Condensates*,  
Nature **639**, 337 (2025)

**Collaboartion with  
CNR-Nanotec**



# Quantum nonlinear interferometers

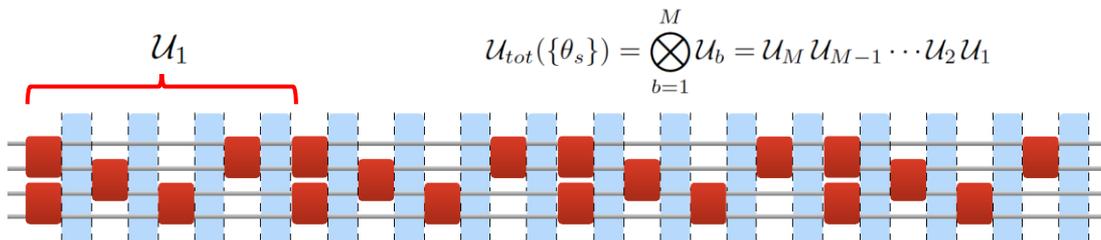


**Current students involved: Davide Rinaldi (PhD)**  
**Antonio Martucci (Master)**  
**Matilde Miccoli (Master)**

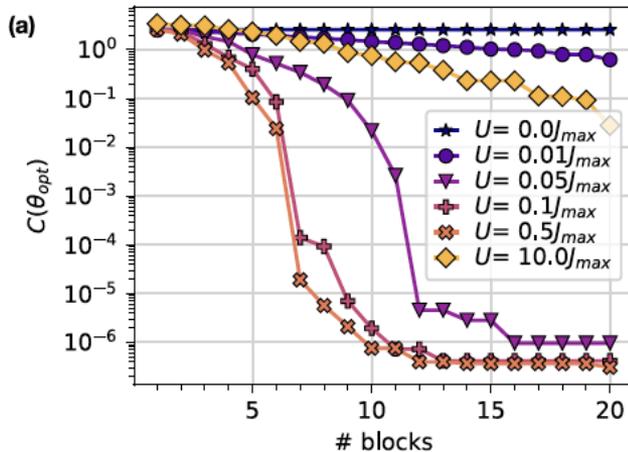
\* KLM (Knill-Laflamme-Milburn) paradigm



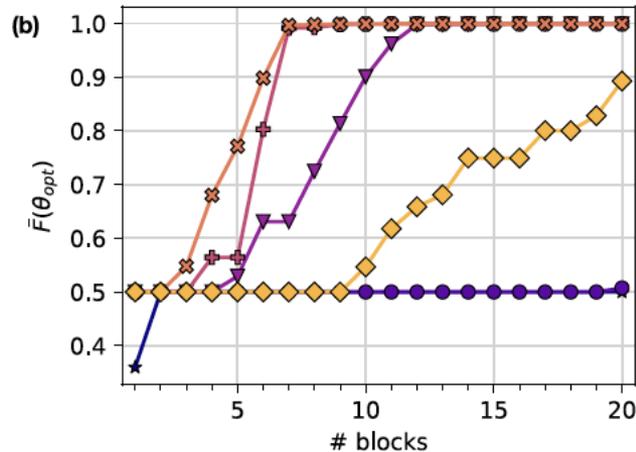
# Recent highlights



cost function  $\rightarrow C(\{\theta_s\}) = \sum_{i,j \in S} |\mathcal{U}_{tot}(\{\theta_s\})_{i,j} - \mathcal{T}_{i,j}|^2$



gate fidelity  $\rightarrow \bar{F}(\{\theta_s^{opt}\}) = \frac{1}{|S|} \sum_{i \in S} |\langle i | \mathcal{U}_{tot}^\dagger(\{\theta_s^{opt}\}) \mathcal{T} | i \rangle|^2$



Scala, Nigro, Gerace,

“Deterministic entangling gates with nonlinear quantum photonic interferometers”

Communications Physics 7, 118 (2024)



# Quantum computers as a digital quantum simulators

Most physical models can be expressed as sum of local terms

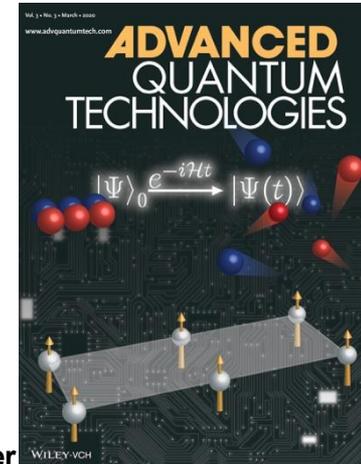
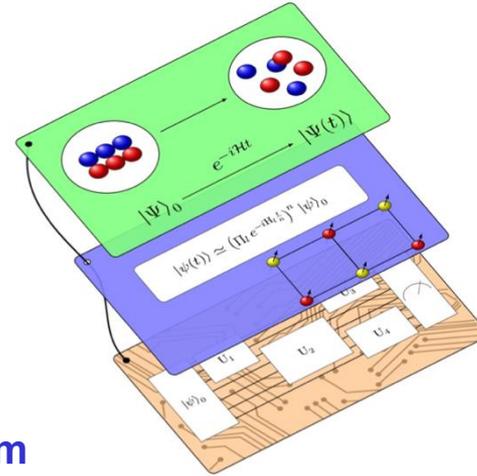
$$\hat{\mathcal{H}} = \sum_k^L \hat{\mathcal{H}}_k$$



QC as a programmable device that uses quantum mechanics to simulate any such model efficiently

→ New frontier for CM theory

F. Tacchino, A. Chiesa, S. Carretta, D. Gerace,  
review on *Quantum Computers as universal quantum simulators*  
Adv. Quant. Tech. **3**, 1900052 (2020)



Front Cover



# Quantum simulations & Quantum Machine Learning



UNIVERSITÀ  
DI PAVIA

- **Adiabatic quantum state preparation on quantum hardware**
- **Digital quantum simulation of Lattice Gauge Theories**
- **Digital quantum simulation of Hubbard models on a lattice**
- **Resource-efficient quantum algorithm for linear systems of equations**

**See Poster n. 46, A103**

Cugini, Nigro, Bruno, Gerace, Phys. Rev. Research **7**, L012074 (2025)

Cugini, Guarnieri, Motta, Gerace, arXiv preprint arXiv:2505.13717 (to appear 2026)

Ghisoni, Scala, Bajoni, Gerace, arXiv preprint arXiv:2409.08929 (to appear in PRA, 2026)

**Current students involved: Davide Cugini, Francesco Ghisoni (PhD)**

**Alice Montemezzani (Master)**



## GIACOMO GUARNIERI

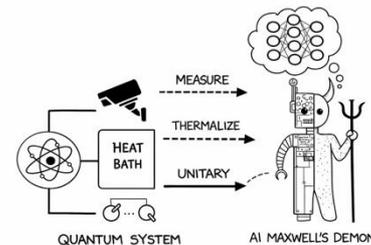
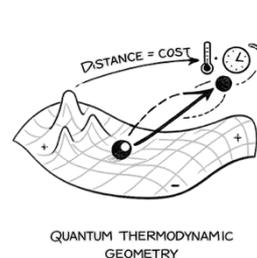
With many collaborators @UNIPV, e.g. Dario Gerace, Marco Liscidini, Chiara Macchiavello, Lorenzo Maccone, Massimiliano Sacchi, Davide Rinaldi, Davide Cugini, Gaia Candreva, Emanuele Tumbiolo, Luca Razzoli, Giovanni Chesi



### MAIN RESEARCH LINES

#### ❖ Quantum Thermodynamics of Precision

Ultimate limits and optimal control protocols that connect information, measurements and feedback to dissipation and fluctuations; stochastic trajectory analysis of work, heat and entropy production.

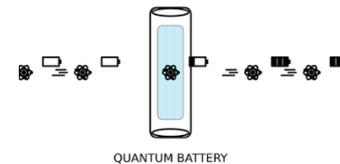
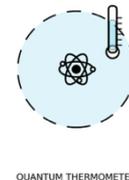
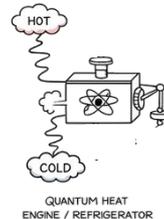


#### ❖ Quantum Maxwell's demon with finite resources

Fundamental bridge between Thermodynamics and Information Theory, including the role of measurements, of quantum coherence and engagement and of finite resources.

#### ❖ Quantum thermal machines, refrigerators and thermometers

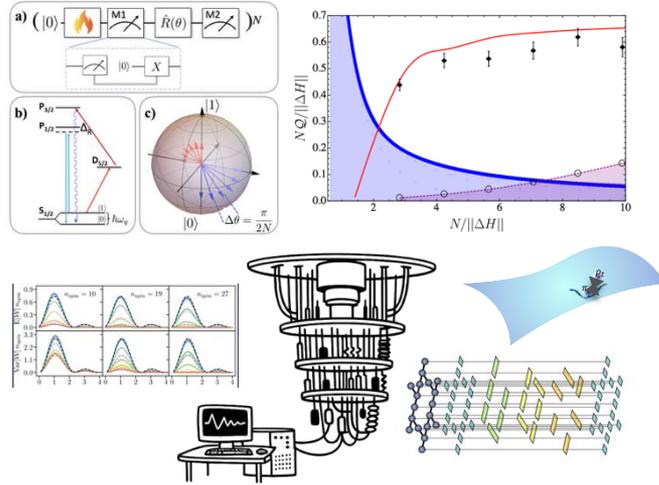
Models and strategies to estimate the efficiency of quantum thermal machines and thermodynamic parameters such as temperature.



#### ❖ Collision models and quantum batteries

Microscopic and stroboscopic descriptions of open quantum systems, applied to optimal energy storage and extraction in the paradigm of quantum batteries.

## THE IMPACT OF QUANTUM SIGNATURES IN QUANTUM THERMODYNAMICS



H. Miller, G.G. et al, **PRL** 125, 160602

H. Miller, ..., G.G. **PRL**126, 210603 ; **PRE** 103, 052138

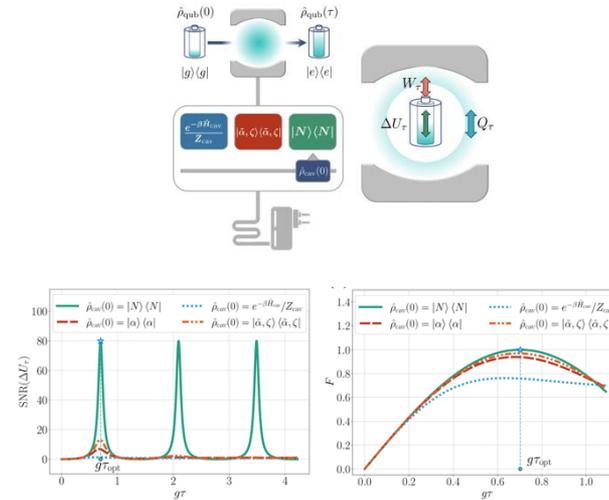
G.G. , J. Eisert, H. Miller , **PRL** 133, 070405

O. Onishchenko & G. G., et al. **Nat. Comm.** 15 (1), 6974

M. Motta, ..., G.G. , **PRL** 135, 180601

**POSTER 45 (day 1)**

## GENUINE QUANTUM ADVANTAGES IN QUANTUM BATTERY CHARGING



D. Rinaldi, R. Filip, D. Gerace, G.G. **PRA** 112, 012205

D. Rinaldi, R. Filip, D. Gerace, G.G. **arXiv** 2601.12183

**POSTER 94 (day 2)**

# Quantum information theory

## Research areas:

Quantum computation

Quantum machine learning

Quantum communication

Quantum metrology

Fundamental concepts

Quantum thermodynamics

## Team:

Chiara Macchiavello, Lorenzo Maccone, Massimiliano Sacchi

Giovanni Chesi, Giacomo Guarnieri, Davide Poderini

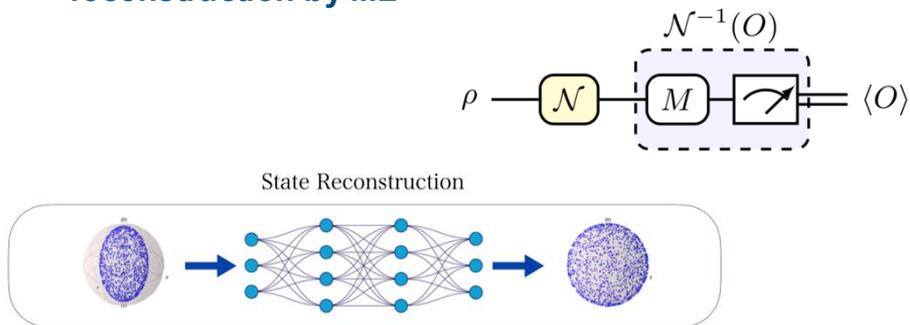
Simone Roncallo, Angela Rosy Morgillo, Emanuele Tumbiolo

# Quantum computation

- Quantum algorithms: q JPEG (downsampling via QFT & discard high frequency qubits), resampling algorithms for multidimensional signals

See Poster 65

- Noise mitigation: noise deconvolution (analytic), state reconstruction by ML



Encode



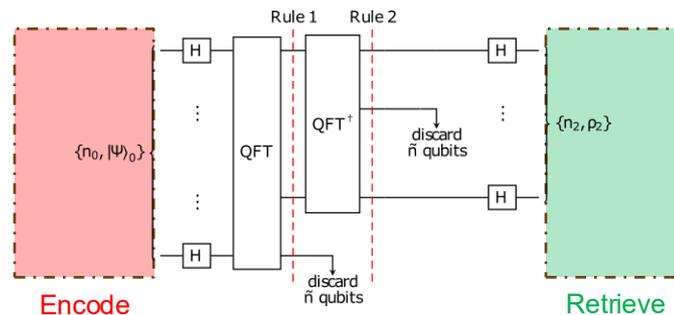
512 x 512 pixels  
18 qubits



Retrieve

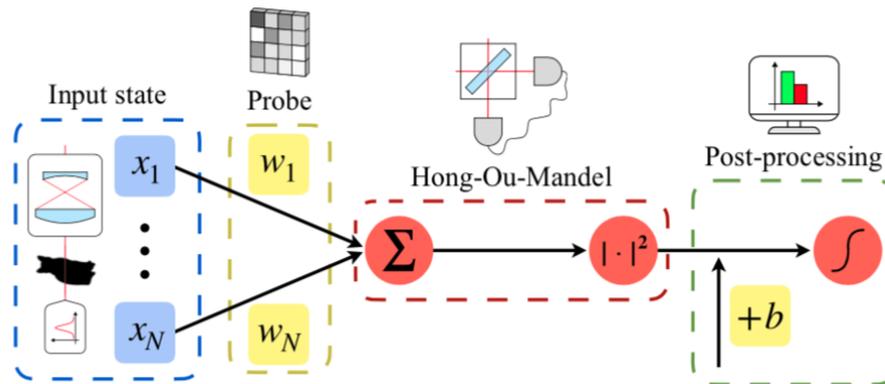
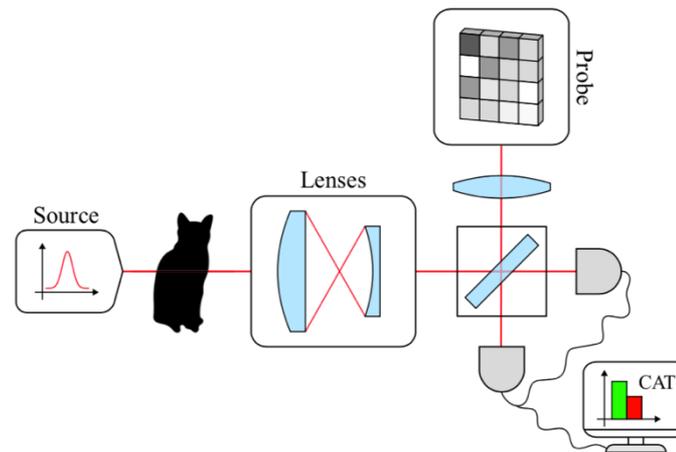


64 x 64 pixels  
12 qubits



# Quantum machine learning

- Quantum optical classifier with superexponential speedup (classification without image reconstruction via Hong-Ou-Mandel effect)
- Quantum optical protocol for a shallow network, keeping superexp. advantage

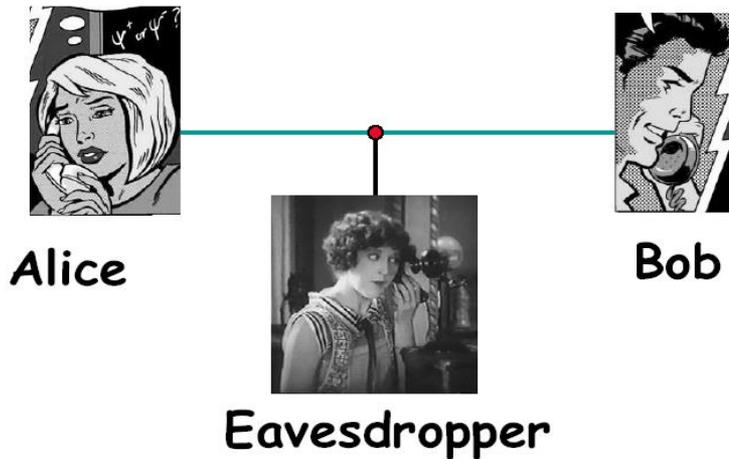


See Poster 65

with Maccone, Morgillo, Roncallo, Tumbiolo

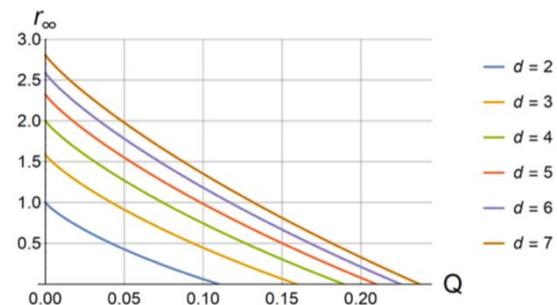
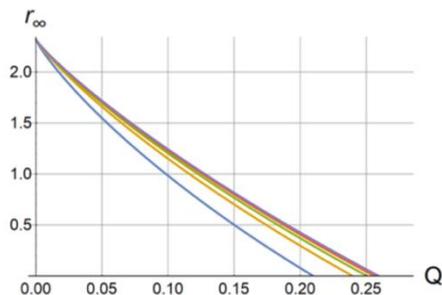
# Quantum communication

- **Quantum cryptography: study the performance (security) of QKD protocols**
- **Proof of advantage for increasing dimension and number of bases, realistic scenarios with imperfections**



See Poster 92

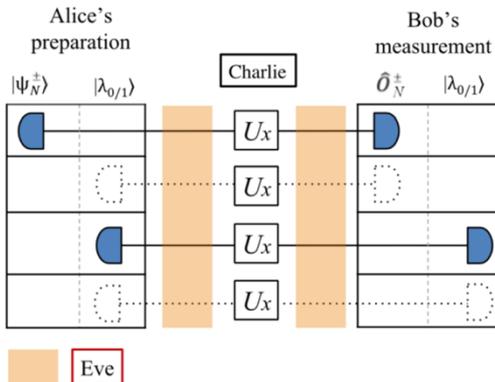
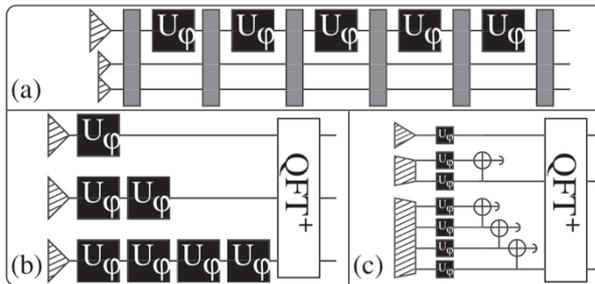
with G. Chesi



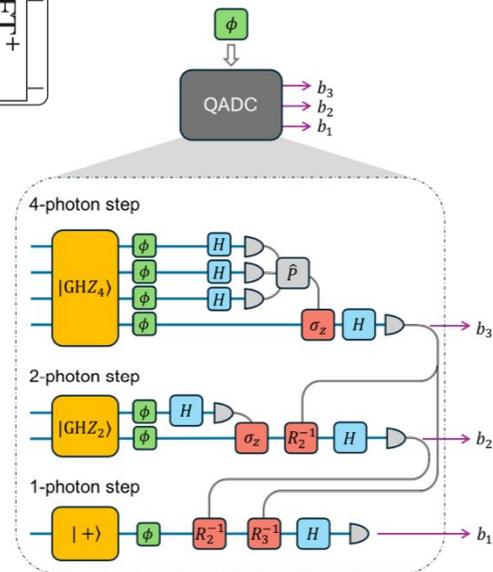
# Quantum metrology

Optimal estimation strategies:

- Digital quantum estimation
- Analog-to-digital converter (QADC)
- Protocols for multiphase estimation
- Cryptographic quantum metrology

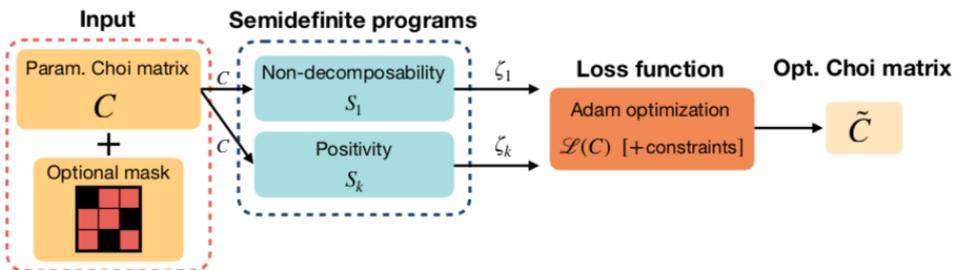
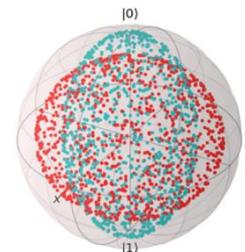
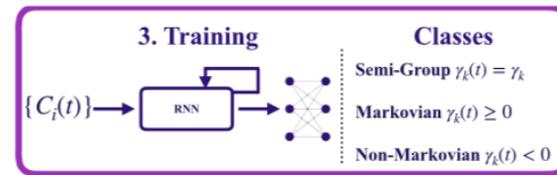
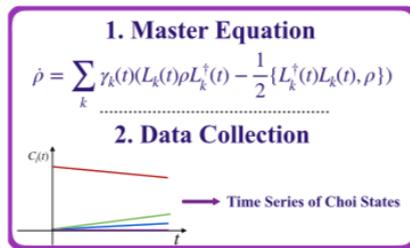


with Chesi, Maccone, Roncallo



# Open quantum systems and quantum operations

- Noise classification
- Detection of non-Markovian properties
- Learning properties of quantum channels (time-varying channels)
- Channel discrimination (resource features for optimal performance: entanglement/non stabiliserness...)
- Chasing non-decomposable positive maps (applications to entanglement detection)

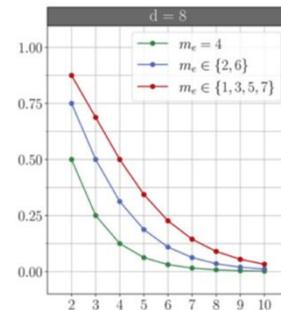
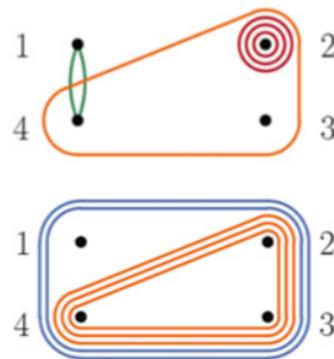
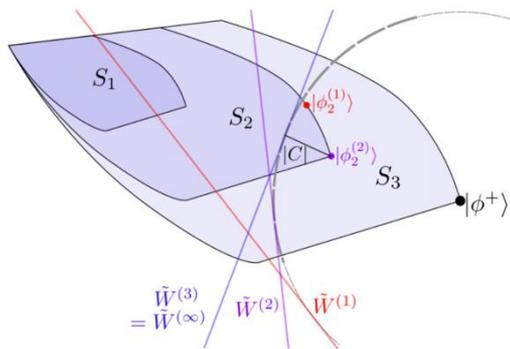
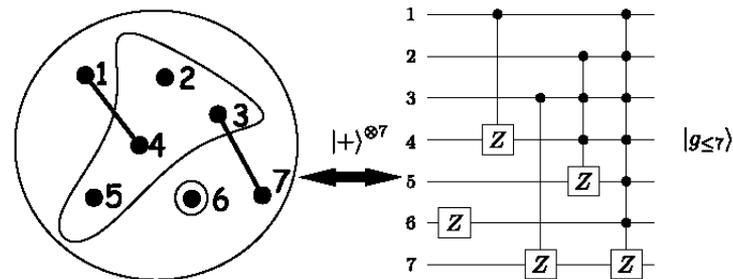


See Poster 66

with R. Morgillo, D. Poderini, M. Sacchi

# Entanglement properties of quantum states

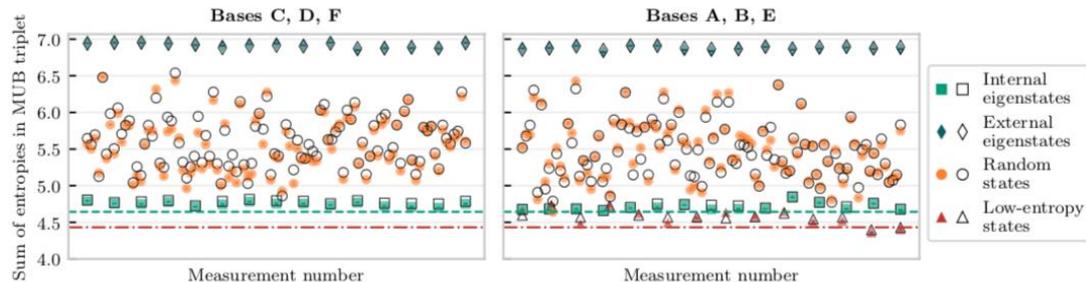
- Entanglement detection methods
- Multipartite systems: Hypergraph states
- Schmidt number witnesses in arbitrary dimension



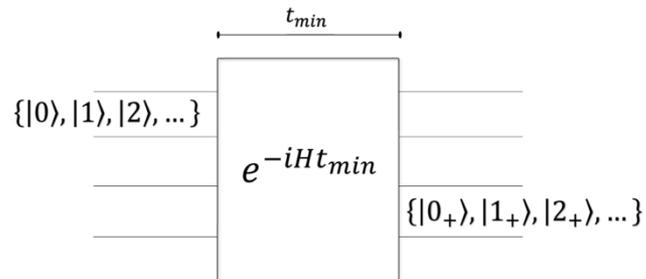
with G. Chesi, D. Poderini

# Uncertainty relations and quantum speed limits

- Entropic uncertainty relations: for complementary properties optimality can depend on the explicit choice of bases



- Q speed limits (ultimate bound for the time required to transform states): for change of basis they depend on the explicit form in  $d > 2$

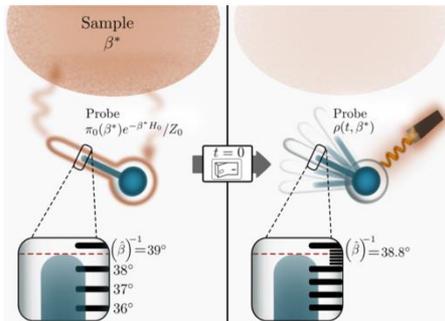


with Maccone, Chesi, Poderini

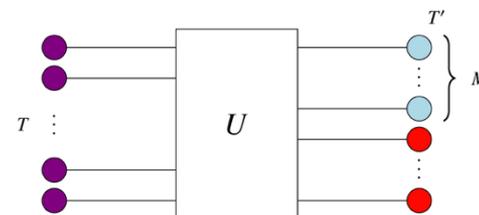
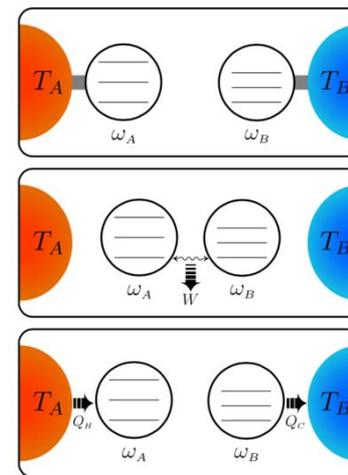
# Quantum thermodynamics

Study laws and concepts of thermodynamics including quantum effects and using quantum information tools

- Quantum thermal machines
- Quantum thermometry: external unitary driving as a resource to improve temperature precision

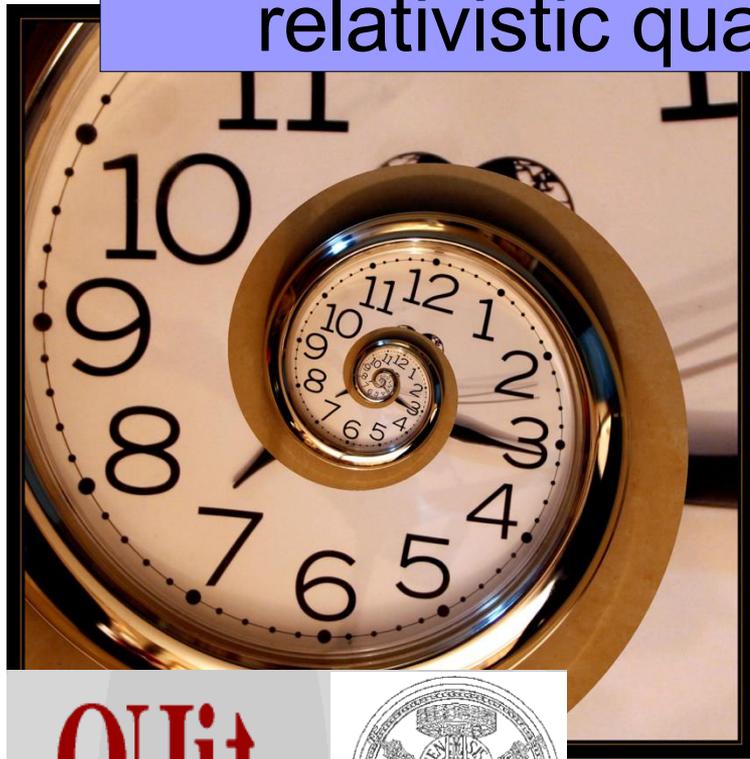


- Dynamical cooling



with Chesi, Guarnieri, Maccone, Sacchi, Tumbiolo

# Geometric Event-Based QM: relativistic quantum spacetime



Lorenzo Maccone

Dip. Fisica, INFN Sez. Pavia,  
Universita' di Pavia

Seth Lloyd

MIT

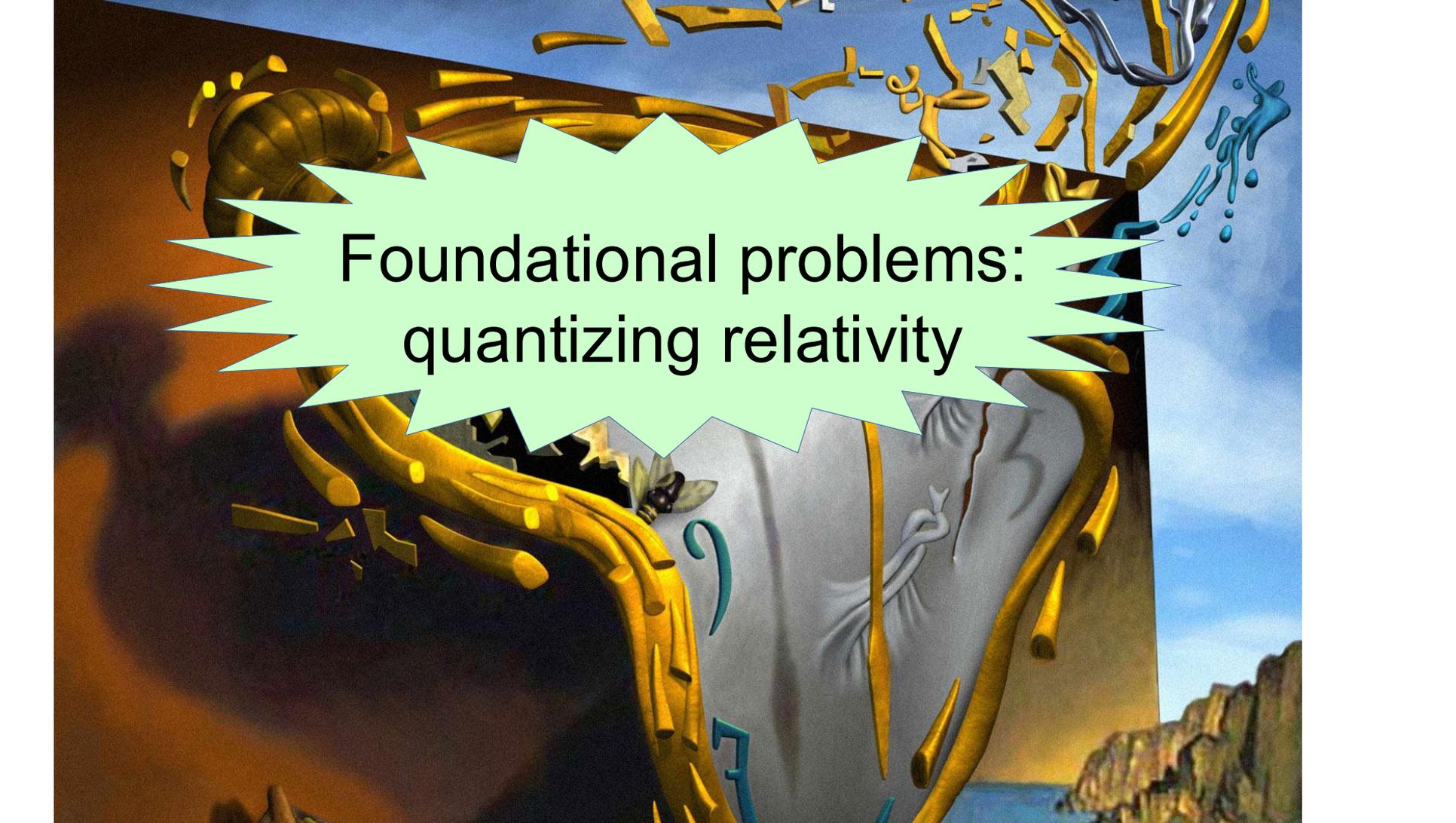
Vittorio Giovannetti

Scuola Normale Superiore, Pisa

**Q*U*it**  
quantum information  
theory group  
[www.qubit.it](http://www.qubit.it)



FQXi Foundation,  
“The physics of what happens”

The background is a vibrant, abstract 3D digital composition. It features a central white, stylized figure that appears to be a person or a deity, rendered in a soft, ethereal style. Surrounding this figure are numerous golden, metallic-looking shapes, including long, curved rods and smaller, fragmented pieces that seem to be floating or falling. There are also blue, liquid-like splashes and droplets scattered throughout the scene. The overall color palette is dominated by gold, white, and blue, with a dark, smoky brown area on the left side. A prominent feature is a large, jagged, light green starburst shape in the center, which contains the text. The lighting is dramatic, with strong highlights and deep shadows, creating a sense of depth and movement.

Foundational problems:  
quantizing relativity

What is the problem?



## What is the problem?

•QM → quantum systems

•GR → events

•



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(finite or infinite in space)

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What do  
YOU think?!

Which is the most  
fundamental concept?



## Two approaches:

- **General relativistic theory of QM**

Systems are more fundamental: GR is made of quantum fields

- **Quantum theory of GR**

Events are more fundamental:

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Explore the alternative!!



- Start with  
**SPECIAL** relativity

- Let's deal with GR in the future (much in the future!)

- QM uses **time conditioned quantities**
- 



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- $|\psi(t)\rangle$  States (Schroedinger picture)

- $X(t)$  Observables (Heis. picture)



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**CANNOT** be relativistically covariant

(covariance="formulas look the same in all reference frames")



## Wait?!? What about QFT?

- QFT uses a couple of tricks to recover covariance:

1) use observables in the Heisenberg picture with covariant spacetime dependence, e.g.

$$a^\dagger e^{-ix^\mu p_\mu}$$

2) Use a state that is invariant for Lorentz transforms, e.g the vacuum  $|0\rangle$



# Our approach: Geometric Event-Based QM

**GEB**



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• quantum events  $\rightarrow$  fundamental

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GEB



- **quantum events**  $\rightarrow$  **fundamental**
- quantum systems  $\rightarrow$  derived: a **quantum state for a succession of events** in  $q$  spacetime



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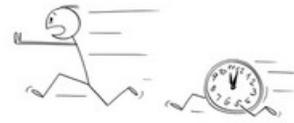
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Poincare' algebra:

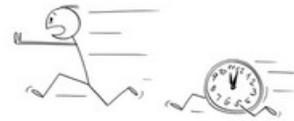
$$\begin{aligned} [M^{\mu\nu}, P^\rho] &= -i(\eta^{\mu\rho} P^\nu - \eta^{\nu\rho} P^\mu), \\ [M^{\mu\nu}, M^{\rho\sigma}] &= i(\eta^{\nu\rho} M^{\mu\sigma} - \eta^{\mu\rho} M^{\nu\sigma} \\ &\quad - \eta^{\mu\sigma} M^{\rho\nu} + \eta^{\nu\sigma} M^{\rho\mu}) \end{aligned}$$

# A universe with a single event



$$|\Phi\rangle = \int d^4x \Phi(\bar{x}) |\bar{x}\rangle = \int d^4p \tilde{\Phi}(\bar{p}) |\bar{p}\rangle$$

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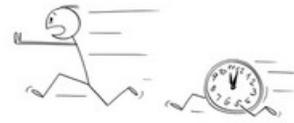
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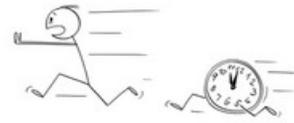
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Physical states are the ones that satisfy some constraints (e.g. PW WdW).

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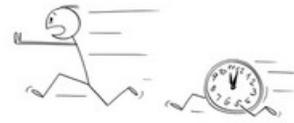


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Born rule in QM is **CONDITIONED**

$$p(\vec{x}|\psi, t) = |\langle \vec{x}_S|\psi_S(t)\rangle|^2 = |\langle \vec{x}_H(t)|\psi_H\rangle|^2$$

Probability that the particle is at position  $\vec{x}$

*given* that the time is t!!!

QM

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QM probabilities are NOT covariant  
GEB probabilities ARE covariant

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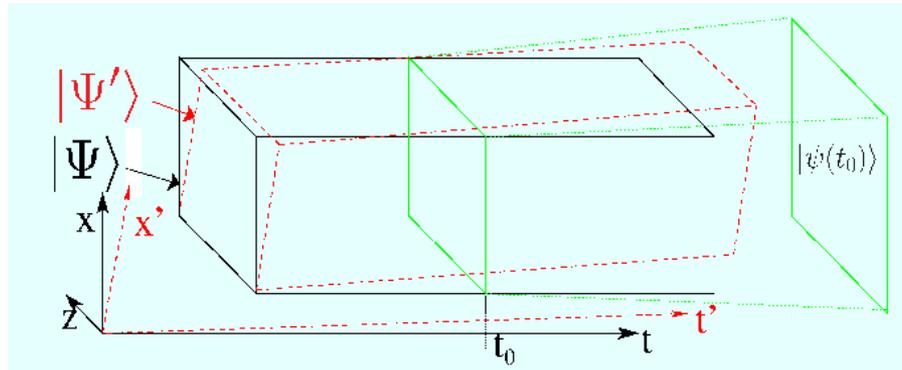
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QM

# LORENTZ TRANSFORMS IN GEB

Just a **unitary transformation on the GEB state** (Wigner's prescription on how to describe symmetries of a theory)

$$|\Phi'\rangle = U_\Lambda |\Phi\rangle$$



# Multiple events: tensor products!

(if fixed number of events n)

$$|\Phi^{[n]}\rangle = \sum \int d^1x_1 \cdots d^1x_n \Phi^{[n]}(\bar{x}_1, \sigma_1; \cdots; \bar{x}_n, \sigma_n) |\bar{x}_1, \sigma_1; \cdots; \bar{x}_n, \sigma_n\rangle$$

**EACH EVENT WITH ITS  
OWN TIME!!!!**

(cfr Dirac's multiparticle-multitime)

$$P^{[n]}(\bar{x}_1, \sigma_1; \cdots; \bar{x}_n, \sigma_n) = |\Phi^{[n]}(\bar{x}_1, \sigma_1; \cdots; \bar{x}_n, \sigma_n)|^2$$

Joint probability for the n events to happen  
in spt positions  $x_1, \dots, x_n$

# Fock space

$$= \frac{1}{\sqrt{n!}} \sum_{\sigma_1, \dots, \sigma_n} \int d^4x_1 \cdots d^4x_n \Phi^{[n]}(\bar{x}_1, \sigma_1; \dots; \bar{x}_n, \sigma_n) a_{\bar{x}_1, \sigma_1}^\dagger \cdots a_{\bar{x}_n, \sigma_n}^\dagger |0\rangle_4$$

## Commutators:

$$\text{Bose: } [a_{\bar{x}, \sigma}, a_{\bar{x}', \sigma'}^\dagger] = \delta_{\sigma, \sigma'} \delta^{(4)}(\bar{x} - \bar{x}'), \quad [a_{\bar{x}, \sigma}, a_{\bar{x}', \sigma'}] = 0,$$

$$\text{Fermi: } \{a_{\bar{x}, \sigma}, a_{\bar{x}', \sigma'}^\dagger\} = \delta_{\sigma, \sigma'} \delta^{(4)}(\bar{x} - \bar{x}'), \quad \{a_{\bar{x}, \sigma}, a_{\bar{x}', \sigma'}\} = 0$$

Bosonic events  $\longrightarrow$

Bosons

Fermionic events  $\longrightarrow$

Fermions





Use **constraints** (as in the quantum time P&W, WdW, etc.)!

## Use constraints

Klein-Gordon eq. constraint in Fock sp:

$$K_{\text{KG}^+}^{(\text{Fock})} := \int d^4p \left[ \Theta(p^0) \bar{\underline{p}} \cdot \underline{p} - m^2 \right]^2 a_{\underline{p}}^\dagger a_{\bar{\underline{p}}}$$

Similarly for the Dirac eq. constraint.

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GEB is an **alternative** in the sense “a different way to obtain the same results”

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WHY?

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WHY?

To get a better ontology?  
To go further than QFT can go?



# Conclusions

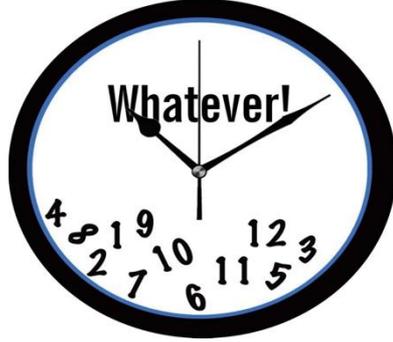


## Conclusions



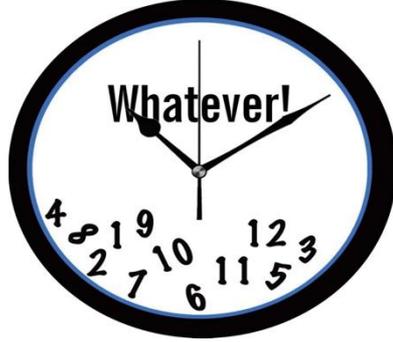
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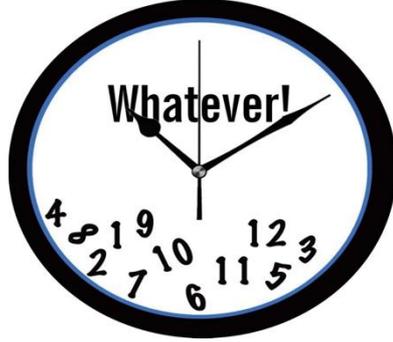
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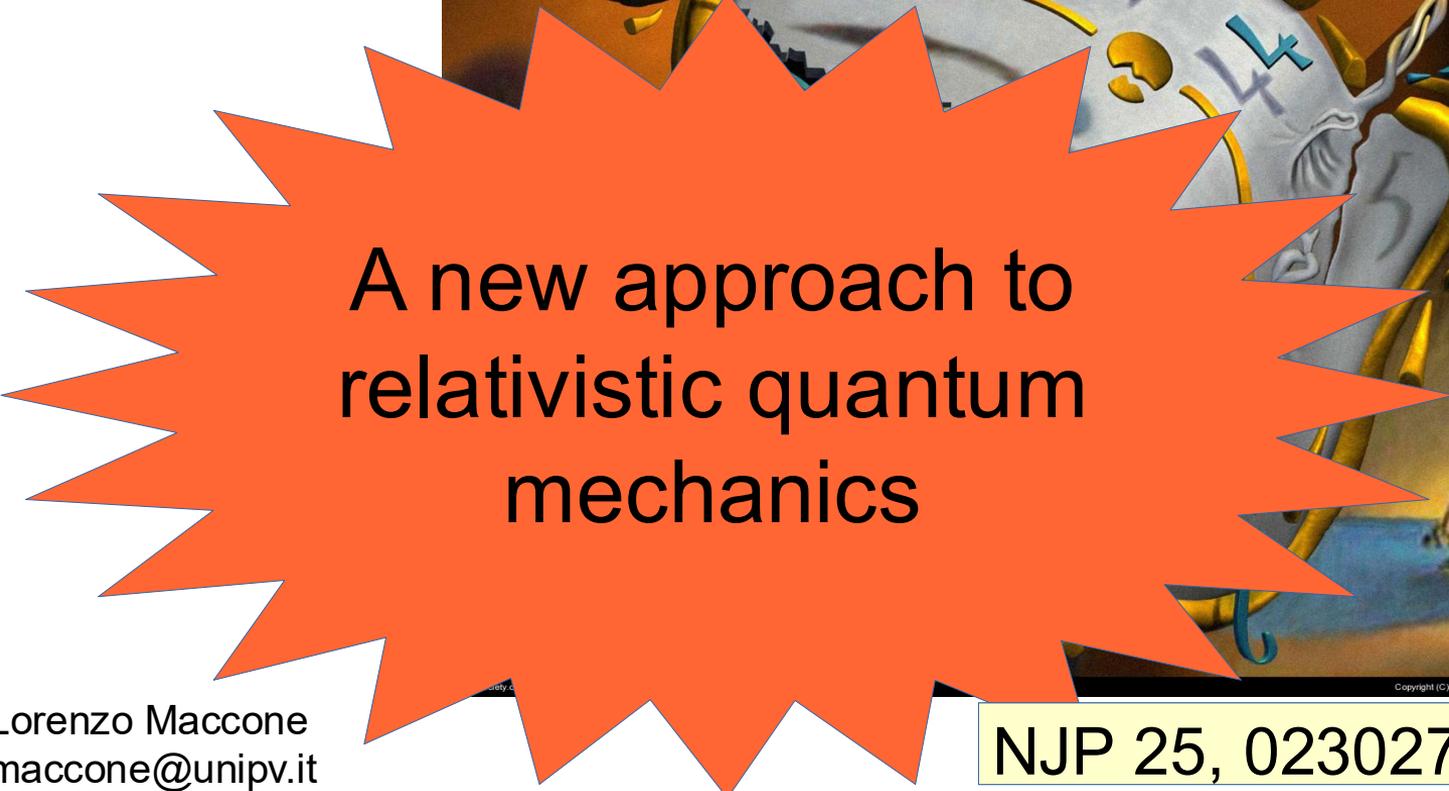


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- GEB: new approach to relativistic QM
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- QFT from GEB: KG and Dirac



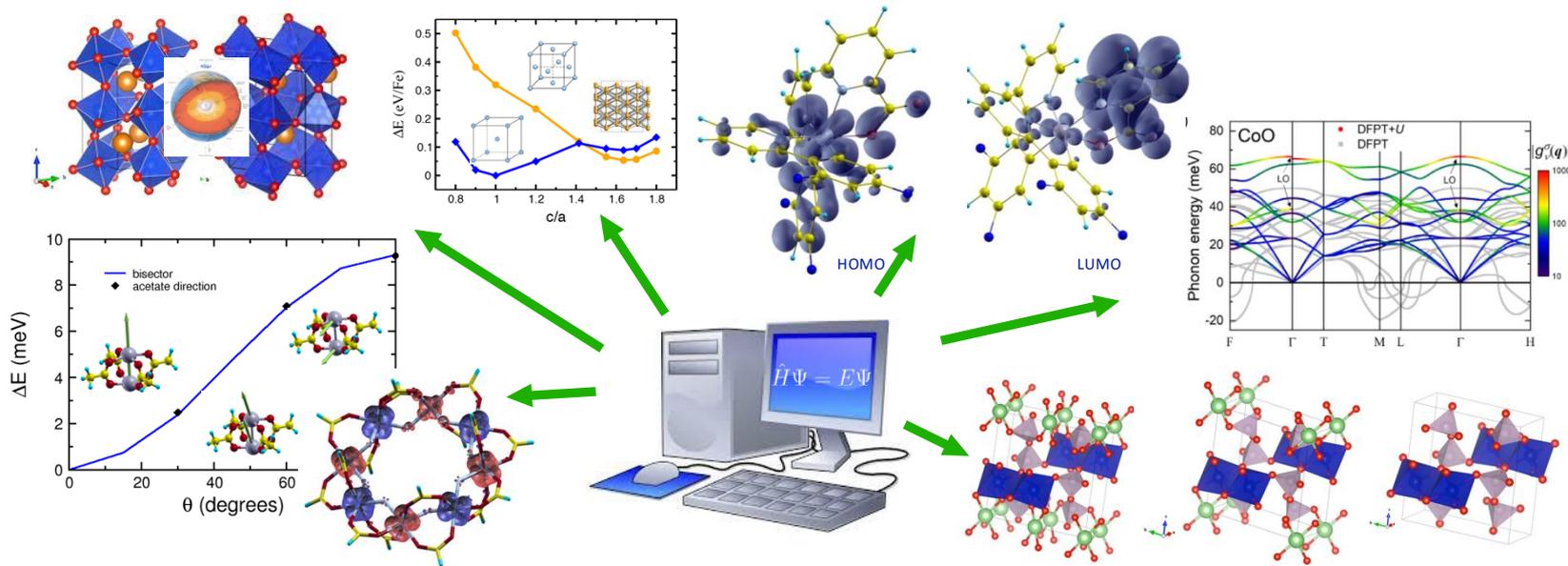
A new approach to  
relativistic quantum  
mechanics

# Modelling of materials from first-principles

## current members



## former members



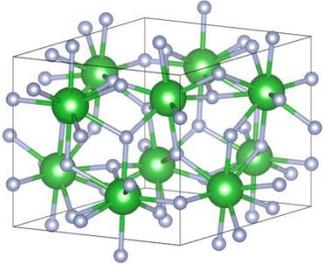
# Modelling of materials from first-principles



**Objective: to comprehend and predict the physical properties of systems from the solution of the electronic problem**

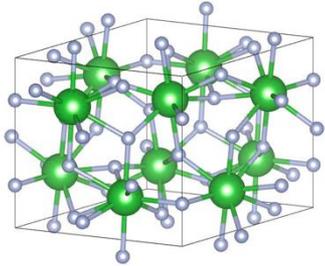
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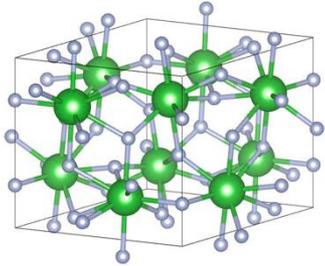
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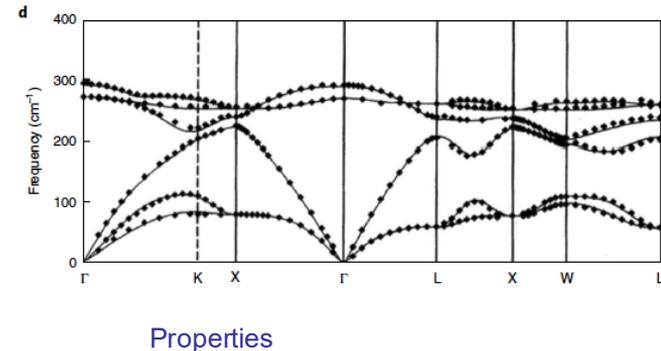
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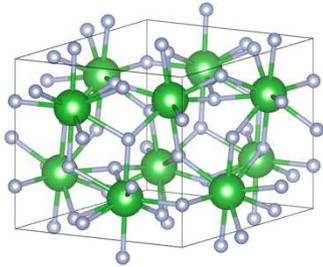


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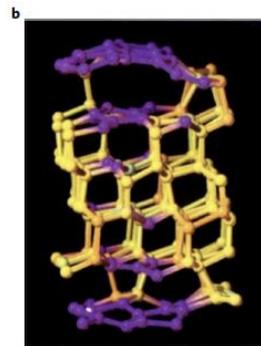
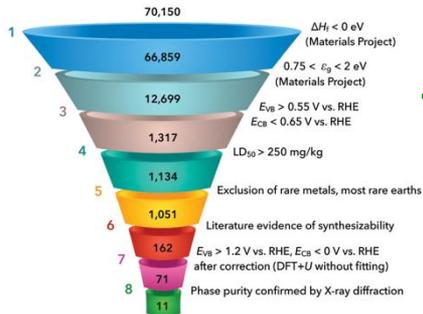
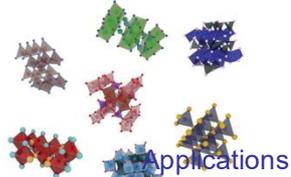


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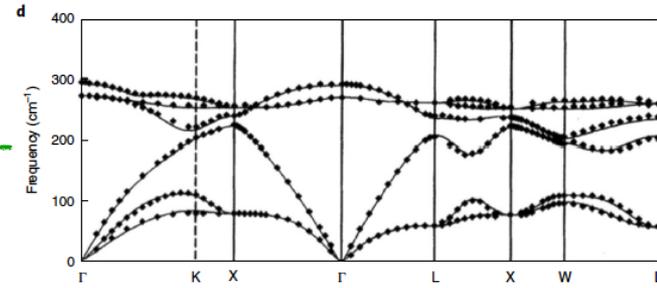
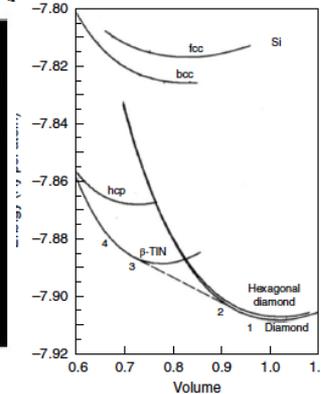
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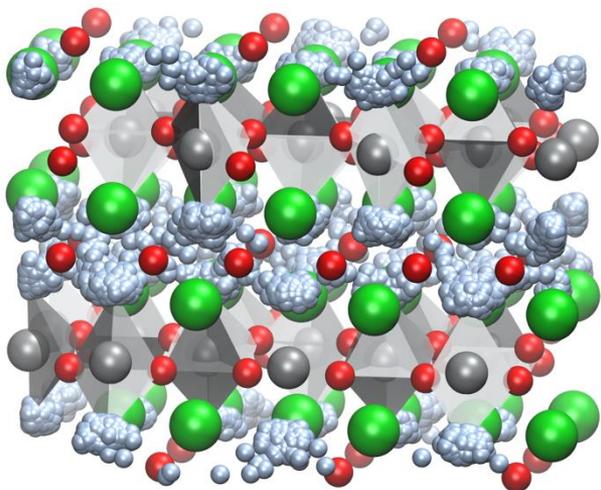
Behavior



Properties

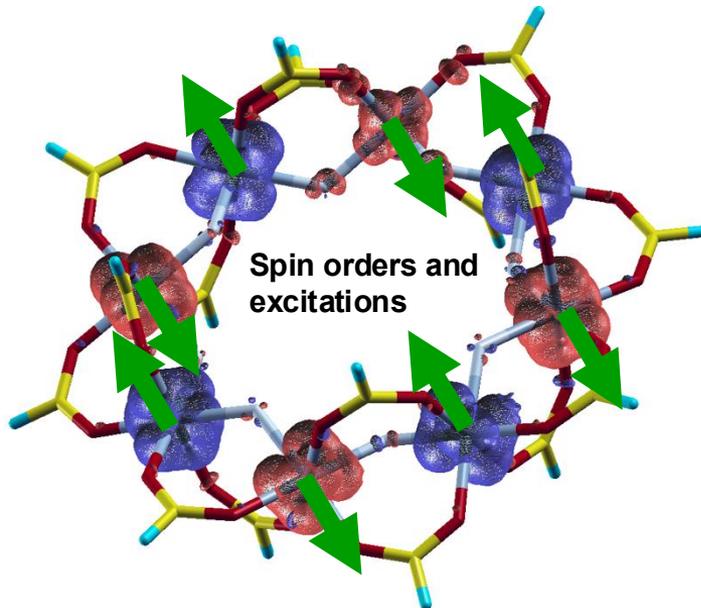
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## Main projects under development



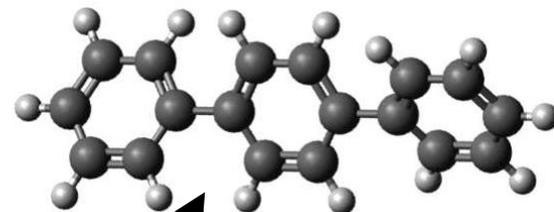
Phase stability and ion diffusion

Fluoride-ion batteries

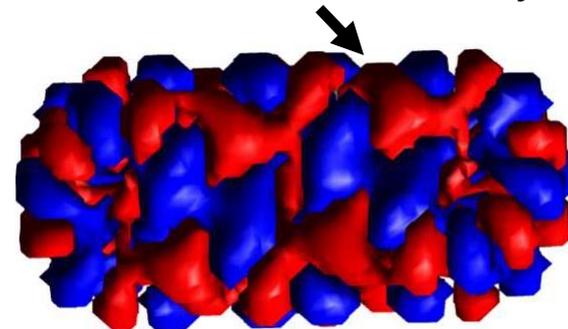


Spin orders and  
excitations

Molecular magnets



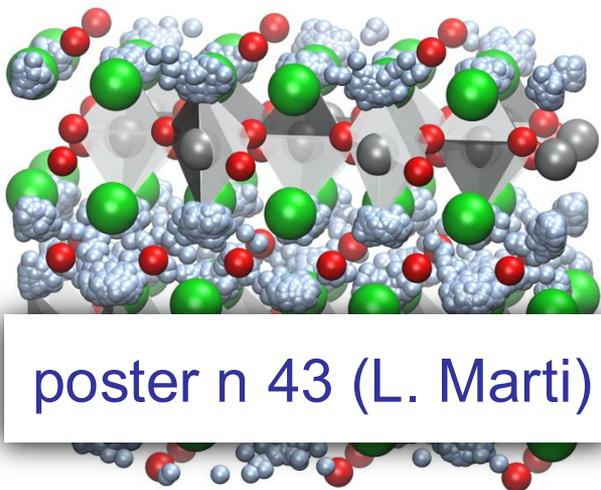
Structural vs electronic chirality



Spin-polarisation in  
chiral systems

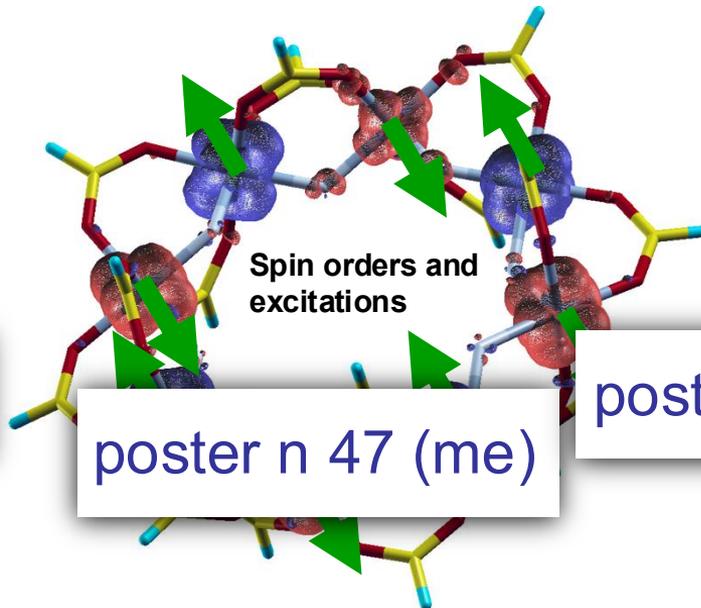
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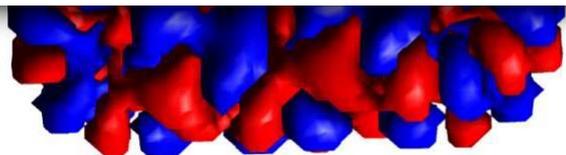
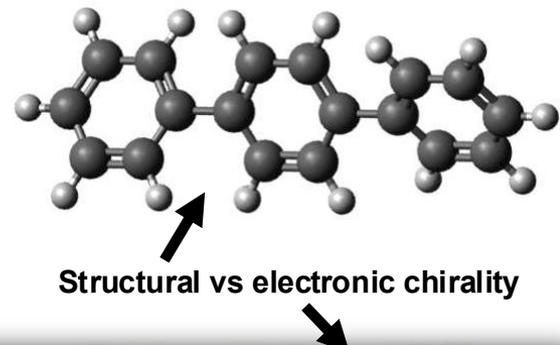


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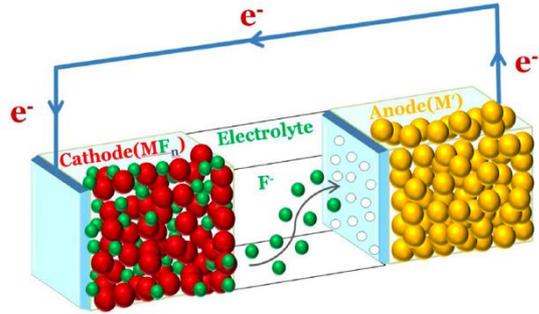
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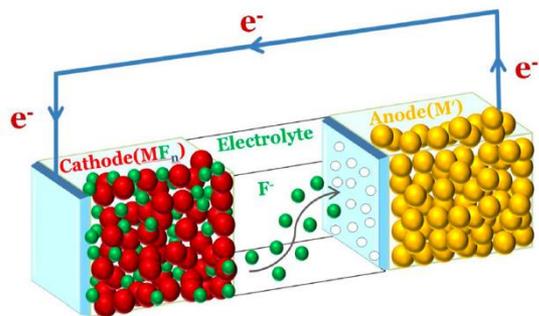
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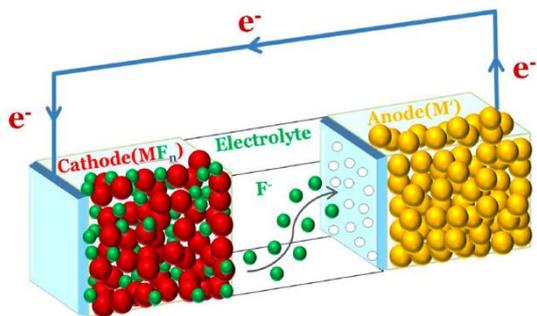


Research needed on all components

- Electrochemical stability
- Intercalation energetics (voltage)
- Diffusivity of charge carriers
- Phase recognition

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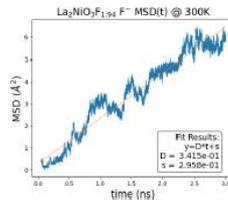
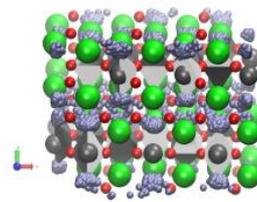
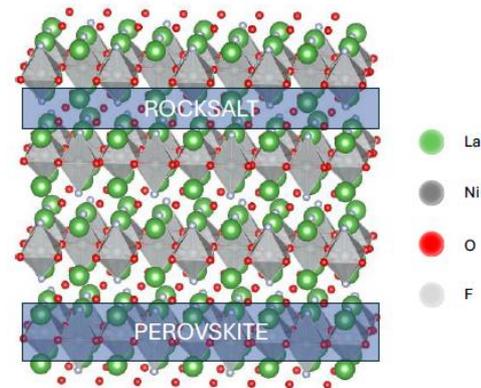
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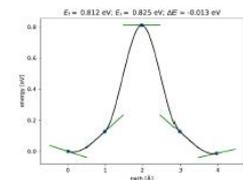
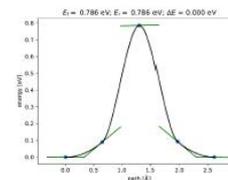
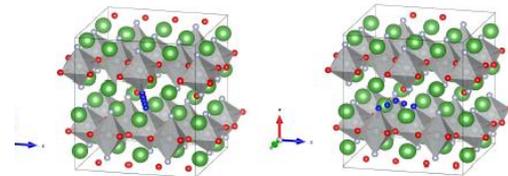
Research needed on all components

- Electrochemical stability
- Intercalation energetics (voltage)
- Diffusivity of charge carriers
- Phase recognition

Cathode:  $\text{LaNiO}_3\text{F}_{2-x}$



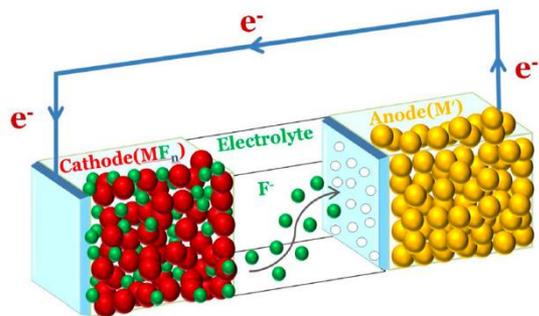
Diffusion of F from  
molecular dynamics



Potential energy barriers along  
diffusion paths

# Fluoride-ion batteries

(In collaboration with P. Galinetto, M. C. Mozzati, C. Tealdi)

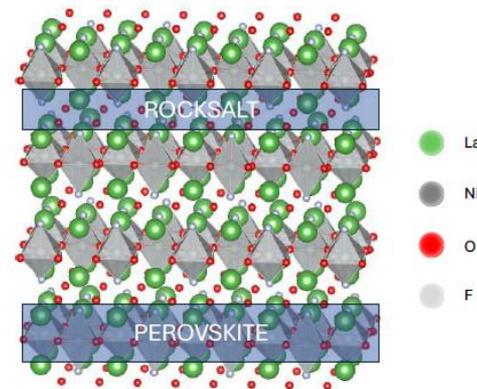


Elettrolita

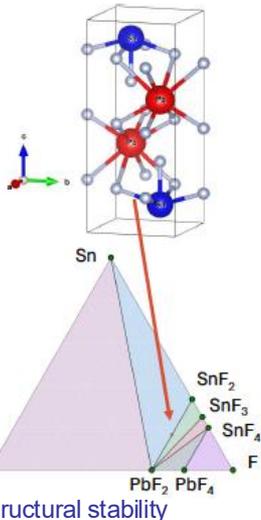
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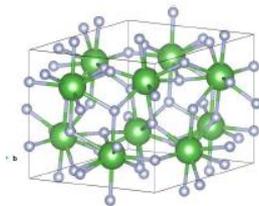
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$\text{PbSnF}_4$

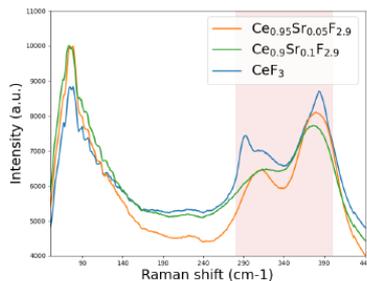


$\text{CeF}_3$

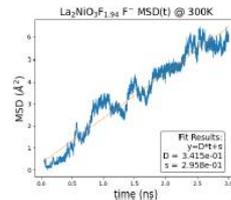
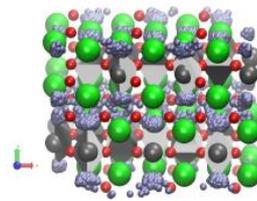


Irrep	Frequency (cm <sup>-1</sup> )	A <sub>1g</sub>	232.3
E <sub>g</sub>	76.8	E <sub>g</sub>	295.4
E <sub>g</sub>	112.4	A <sub>1g</sub>	299.9
A <sub>1g</sub>	121.2	E <sub>g</sub>	304.9
E <sub>g</sub>	144.7	E <sub>g</sub>	315.7
E <sub>g</sub>	159.0	E <sub>g</sub>	367.0
E <sub>g</sub>	200.3	E <sub>g</sub>	373.2
A <sub>1g</sub>	210.5	A <sub>1g</sub>	393.0
E <sub>g</sub>	220.0	E <sub>g</sub>	443.3

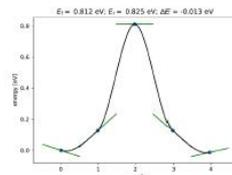
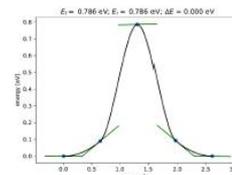
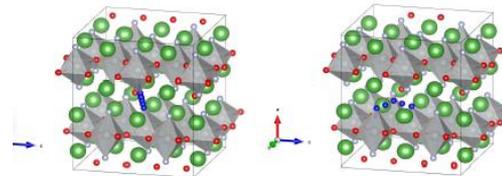
$$\Gamma_{\text{Raman}} = 5A_{1g} + 12E_g$$



Raman spectroscopy (exp and calc) for phase recognition and characterisation

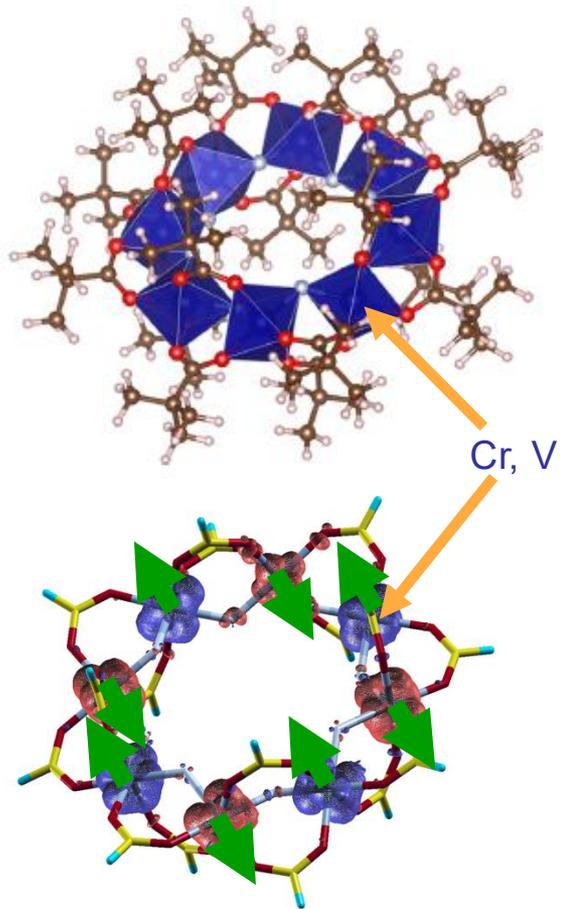


Diffusion of F from molecular dynamics



Potential energy barriers along diffusion paths

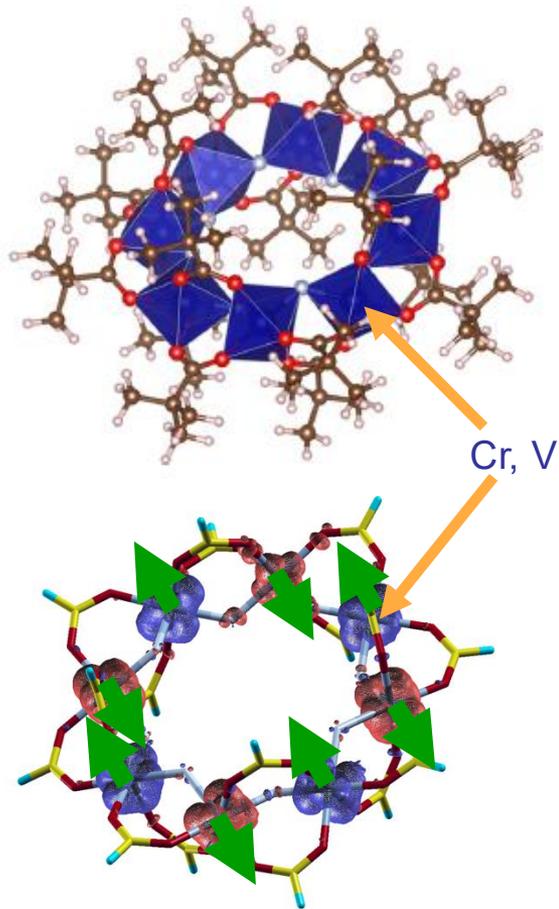
# Molecular magnets



# Molecular magnets

Magnetic orders and spin excitations in Cr<sub>8</sub> and V<sub>8</sub> from the exact diagonalization of model spin Hamiltonians:

$$\hat{H}_{spin} = \hat{H}_{ex} + \hat{H}_{bq} + \hat{H}_{dm}$$

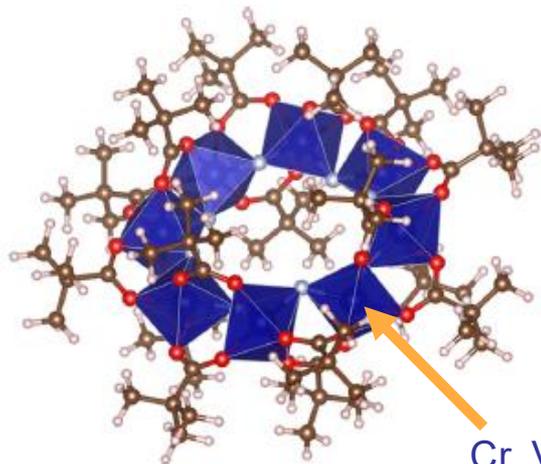


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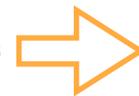
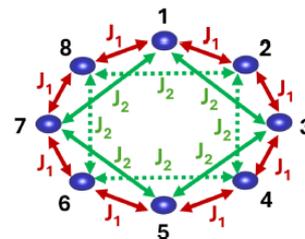
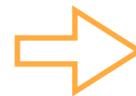
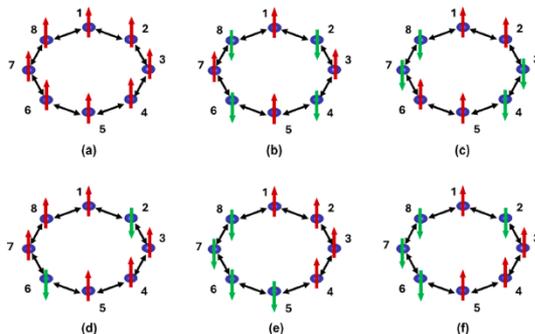
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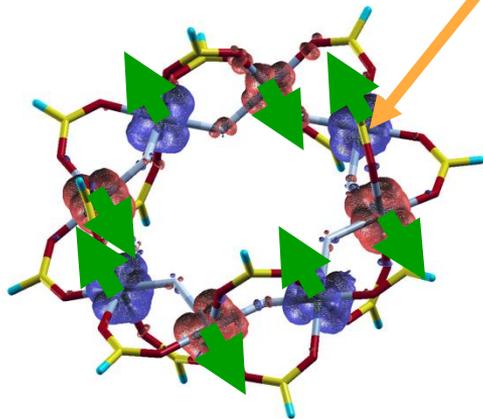
Computational strategy:  $E_{DFT}^{\alpha} = \langle \Psi_{\alpha} | \hat{H}_{spin} | \Psi_{\alpha} \rangle$



Cr, V



$\hat{H}_{spin}$

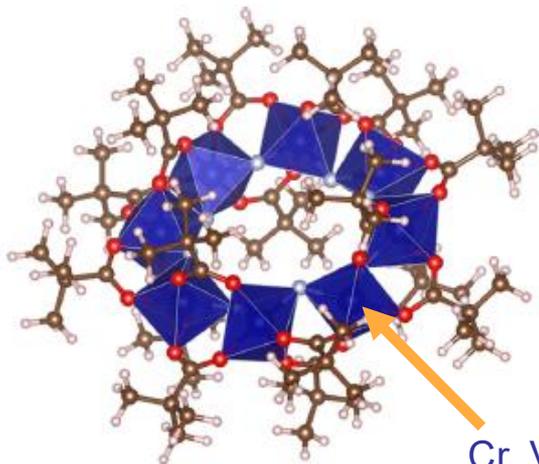


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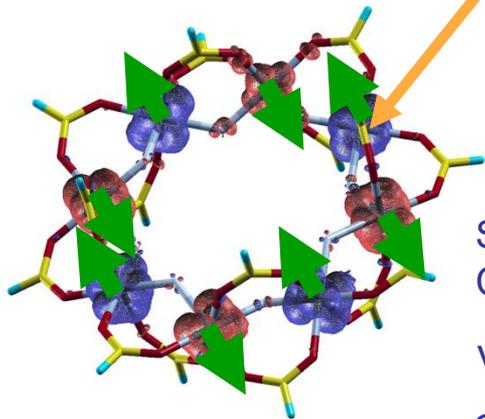
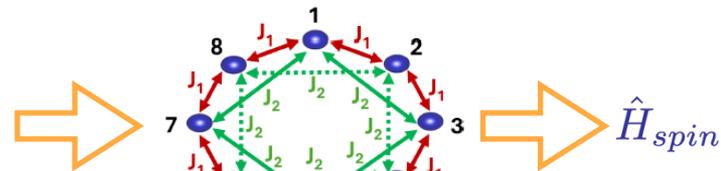
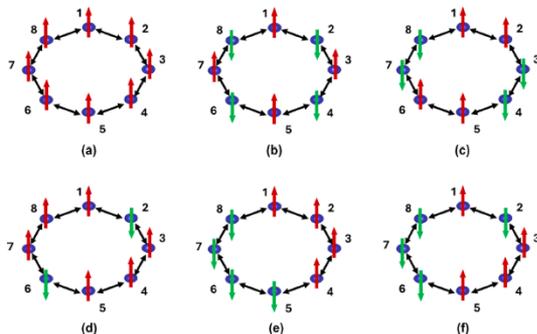
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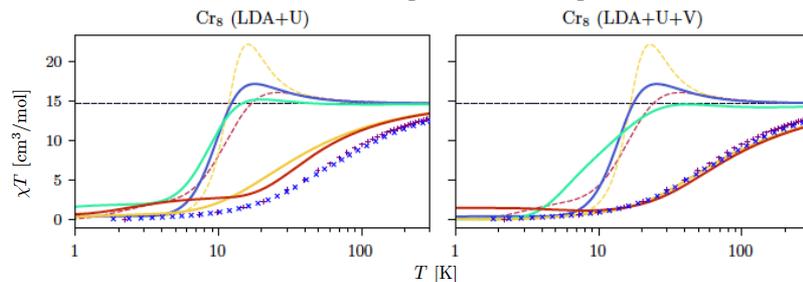


Significant differences between Cr<sub>8</sub> and V<sub>8</sub>:

V<sub>8</sub> ferromagnetic

Cr<sub>8</sub> antiferromagnetic

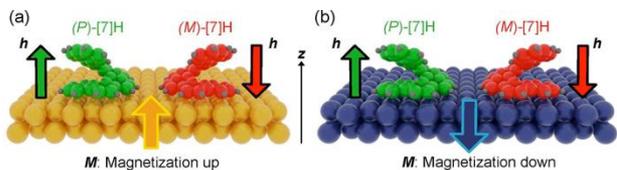
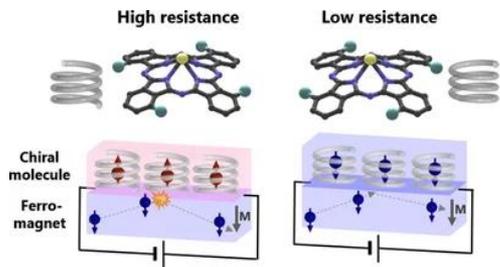
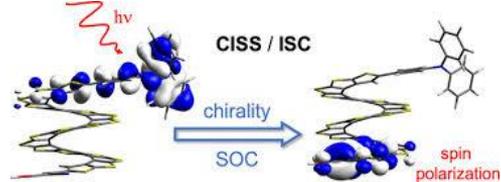
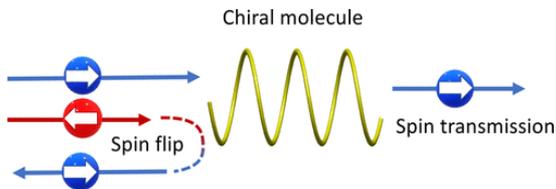
$$\chi_{zz} = \mu_0 \beta \left[ \langle \hat{m}_z^2 \rangle - \langle \hat{m}_z \rangle^2 \right]$$



# Spin and chirality

Chirality-induced spin selectivity (CISS): can we explain it?

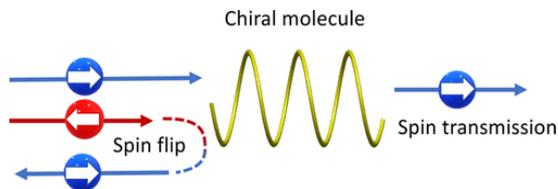
CISS phenomenology



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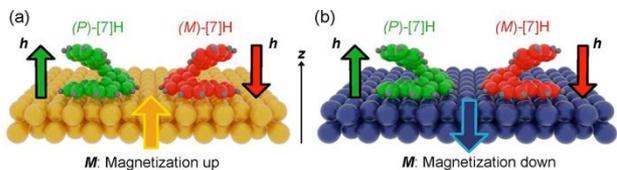
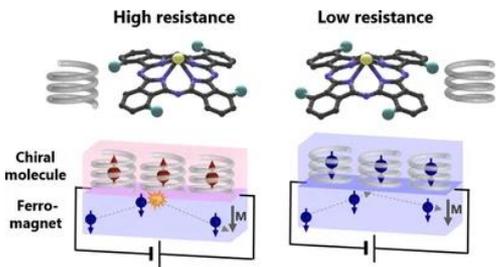
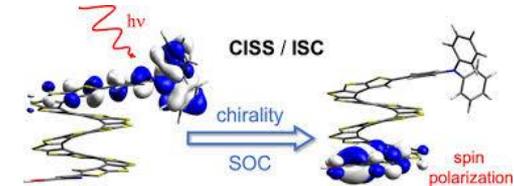
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CISS phenomenology



A new descriptor: electron chirality  $\chi(\mathbf{r}) = \sum_{\mu\nu} \psi_{\mu}^*(\mathbf{r}) \gamma_{\mu\nu}^5 \psi_{\nu}(\mathbf{r})$

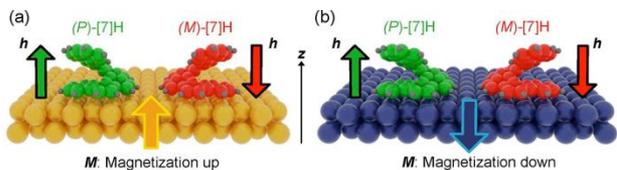
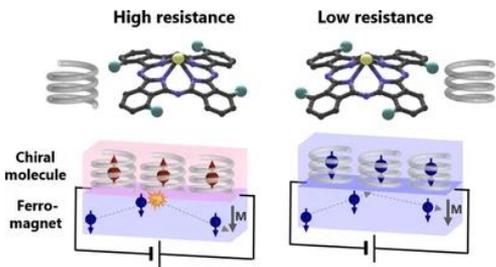
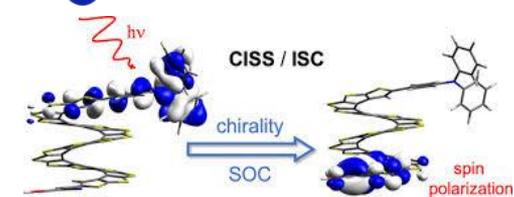
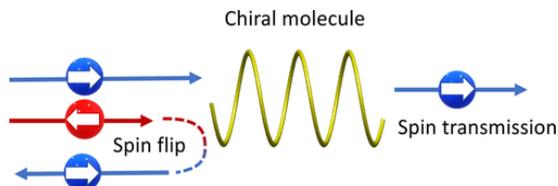
Where:  $\gamma^5 = i\gamma^0\gamma^1\gamma^2\gamma^3 \approx \boldsymbol{\sigma} \cdot \mathbf{p}$  (massless particles or WRL)



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DFT su eq. di Dirac:

Molecules of tunable chirality: ethane, trichloroethane and triphenil

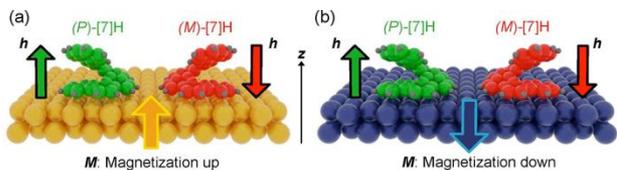
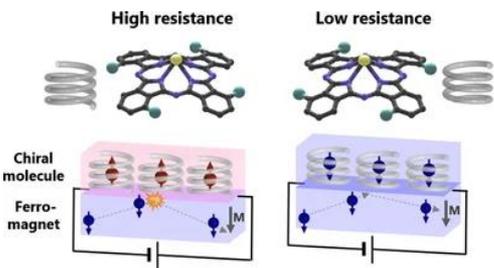
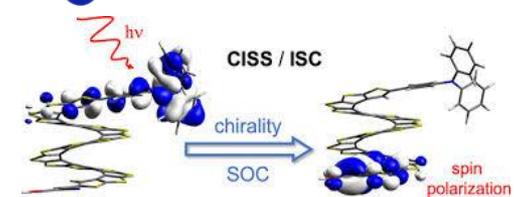
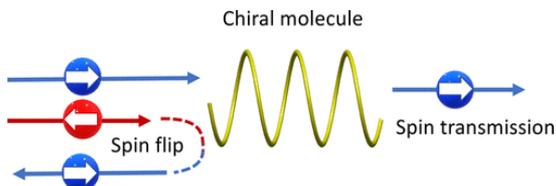


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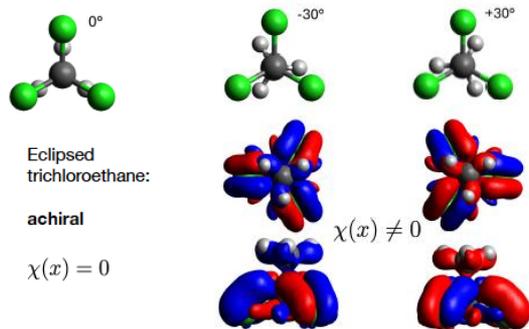
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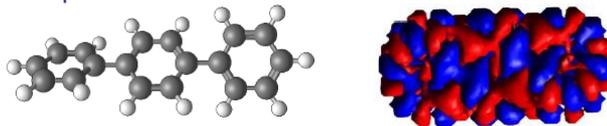
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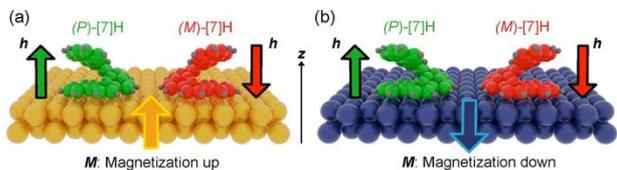
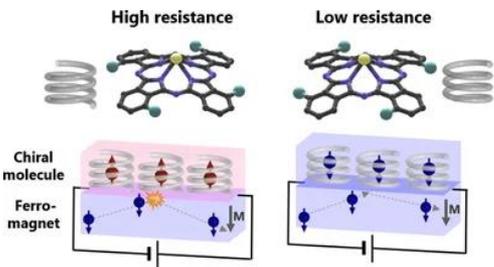
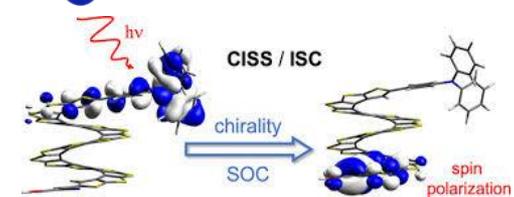
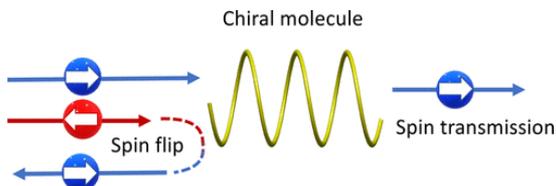
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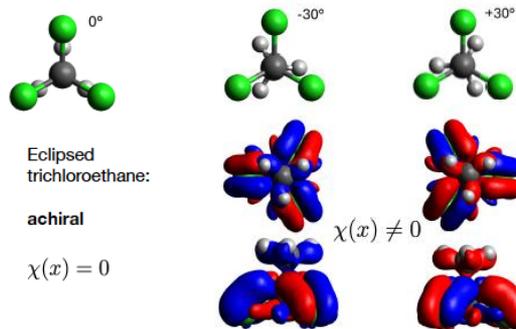


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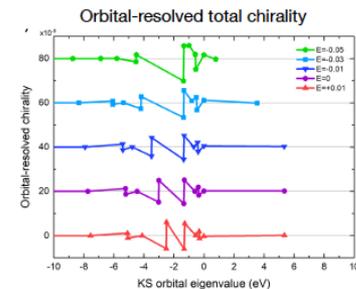
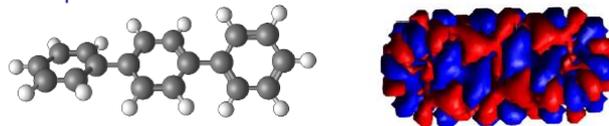
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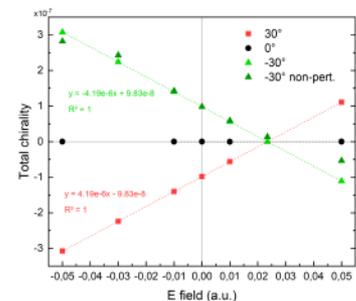
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chiral triphenil



Response to electric fields



# Modelling the modelling engine

Main computational tool: density functional theory (DFT):

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## Examples of difficult cases:

Strong electronic correlations

Excited states

Superconductivity

Out-of-equilibrium conditions

Topological materials

Non-collinear magnetism and  
Spin frustration

Spontaneous symmetry breaking

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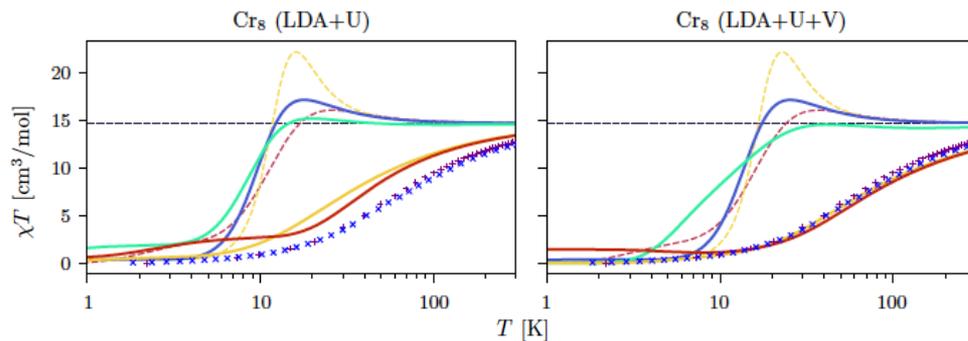
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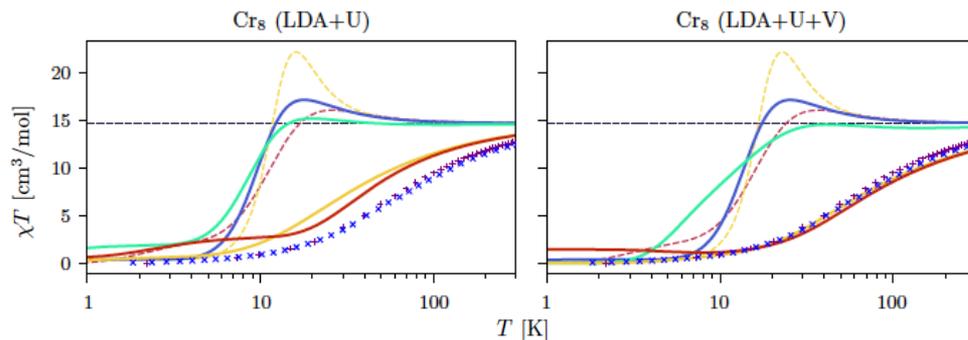
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## Much theoretical work still needed

Gauge fields formalism

Dependence on (spin) currents

Non-hermitian terms

Etc...