

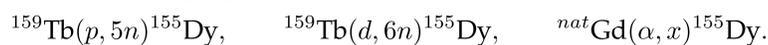


1. INTRODUCTION

Terbium: known as the *swiss-army knife* of Nuclear Medicine for its **four isotopes** useful both for imaging and therapy.

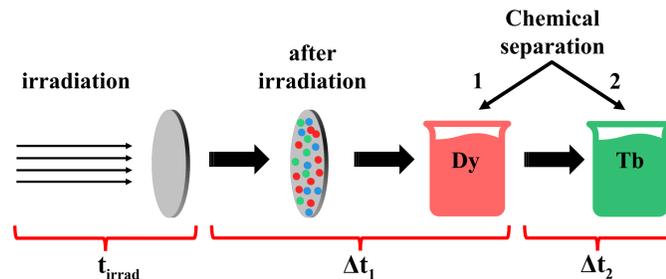


We focus here on ^{155}Tb ($T_{1/2} = 5.32$ d), **theranostic** radionuclide for Auger-electron therapy and SPECT imaging, with three cyclotron-based production routes:



These **reactions** are based on the intermediate **formation and decay of the progenitor $^{155}\text{Dy} \rightarrow ^{155}\text{Tb}$** and are ^{156}Tb -contaminant free, in contrast to **standard routes** that rely on direct ^{155}Tb production with the **undesired generation of ^{156}Tb** .

During the irradiation (t_{irrad}), multiple isotopes are produced (isotope of interest + contaminants). ^{155}Tb generation involves **two separation steps** (Dy extraction and subsequent Tb extraction) characterized by processing times Δt_1 and Δt_2 .



Goals: 1) to identify the reaction with the **highest yield and purity**; 2) to define the **optimal energies and processing times** for production.

2. METHODS

The study focused on two optimizations regarding: A) Dy-isotope production cross sections, B) irradiation and separation parameters to maximize ^{155}Tb yield and purity.

Theoretical calculations were performed with TALYS, including **rotational effects** for **deformed nuclei**, **linear binning** for continuum transitions, variations of **pre-equilibrium parameters**, **microscopic level-density models** with minimal parameter tuning for ^{153}Dy ($T_{1/2} = 6.4$ h). **These settings** are referred to as **TALYS modified**. We calculated the activity $A(t)$ of each nuclide and the isotopic (IP(t)) and radionuclidic purity (RNP(t)) of ^{155}Tb :

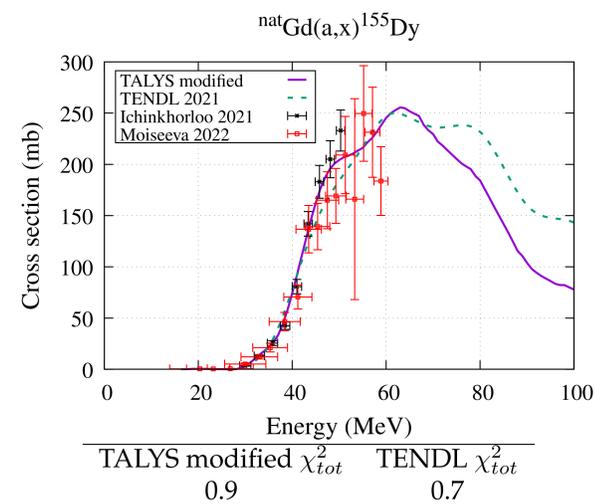
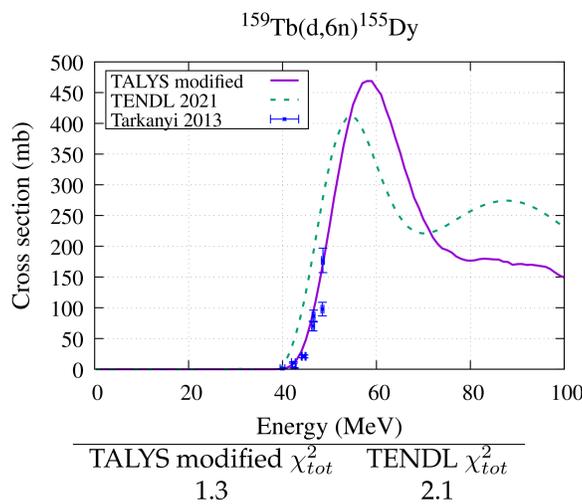
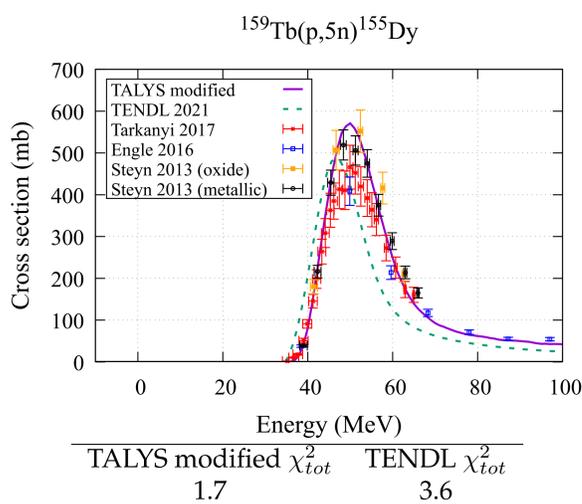
$$A_i(t) = \lambda_i N_i(t) \quad IP_{^{155}\text{Tb}}(t) = \frac{N_{^{155}\text{Tb}}}{\sum_i N_i(t)} \quad RNP_{^{155}\text{Tb}}(t) = \frac{A_{^{155}\text{Tb}}}{\sum_i A_i(t)}$$

To identify the most promising reaction, we evaluated the **integral saturation yield**:

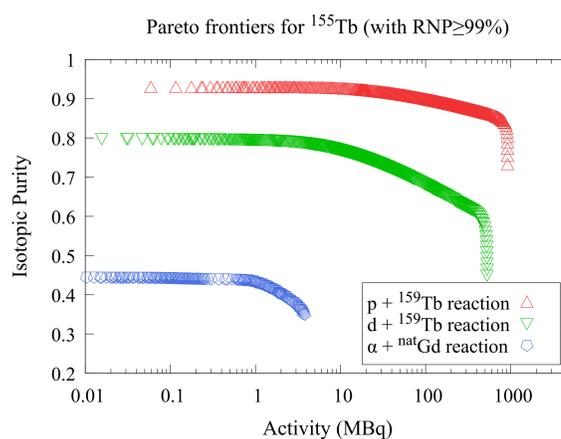
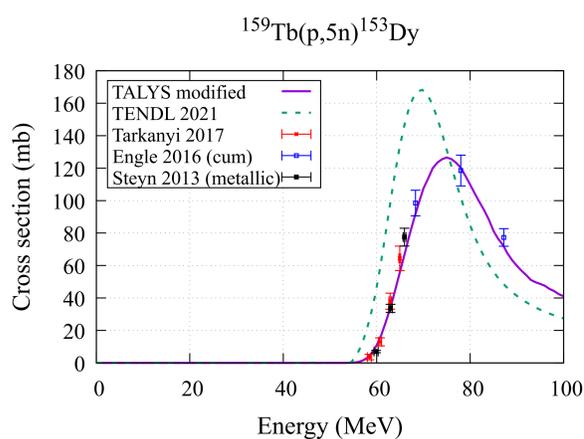
$$a_{\text{sat}}^{\text{int}} = \lim_{\substack{t_{\text{irrad}} \rightarrow +\infty \\ \Delta t_1 \rightarrow 0}} \frac{A_{^{155}\text{Tb}}(t)}{I_0}$$

To address the second goal, we performed a **multi-objective optimization**, computing the **Pareto frontier** between ^{155}Tb integral production (IP) and activity (A), with the constraint $\text{RNP} \geq 0.99$, as recommended by the European Pharmacopoeia.

3. SELECTED RESULTS



Top: better description is achieved with the calculations presented in Methods for all the three reactions with respect to the standard TENDL library. **Optimization** achieved especially for **contaminants**, as ^{153}Dy shown below (**bottom left**), and validated with **total chi-square calculation** (considering all the Dy channels): **improvements** of **53%** for protons, **38%** for deuterons and **22%** for α reactions.



reaction	p	d	α
$E_{\text{in}}-E_{\text{th}}$ (MeV)	60–35	67–38	53–12
Δx (mm)	4.6	3.5	0.55
$a_{\text{sat}}^{\text{int}}$ (MBq/ μA)	1891	1139	19
IP	0.7	0.41	0.07
RNP	0.997	0.992	0.98

Comparison of the three reactions by means of the saturation integral yield defined in the Methods section. The **proton-induced reaction is the most promising** route, providing the highest activity and purity levels.

Middle figure: Pareto frontier for the three reactions. Set of equally valid solutions that simultaneously maximize activity and isotopic purity, while also satisfying the required radionuclidic-purity constraint. The figure highlights **higher production of contaminants** in reactions with **deuterons** and **α -particles**. Additionally, **lower activities** are the result of lower cross section values.

4. CONCLUSIONS

Theoretically consistent and strong representation of the cross sections of ^{155}Tb and contaminants for all the reactions. Additionally we **optimized the activities and purities**, identifying the reaction with protons as the most promising. We developed a **robust framework** with **dedicated codes** available for further studies on the field. **Tools already applied with success** to other IAEA recommended isotopes, such as ^{67}Cu , ^{47}Sc and ^{52g}Mn .