



Il Protone, questo sconosciuto – Parte I

Da cosa è composto il protone?

Nicolò Valle, Paolo Pedroni

11 dicembre 2018

Università di Pavia

Quali sono i costituenti ultimi della materia?

Quali sono le forze elementari che governano le loro interazioni?

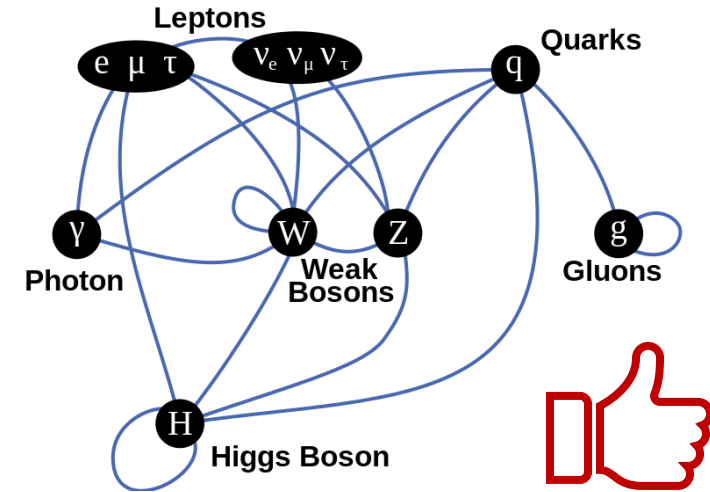
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Quali sono i possibili stati della materia?

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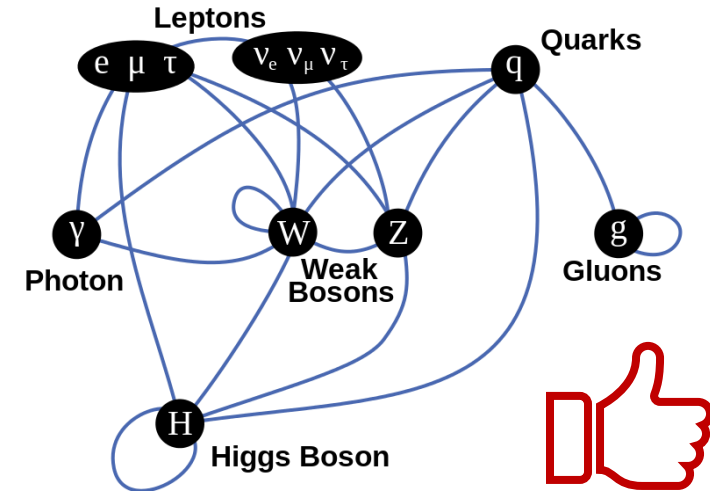
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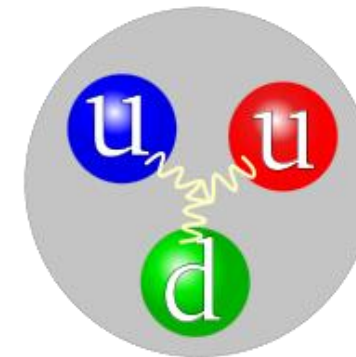
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Come è fatto il nucleone??



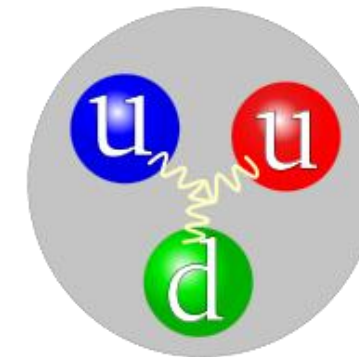
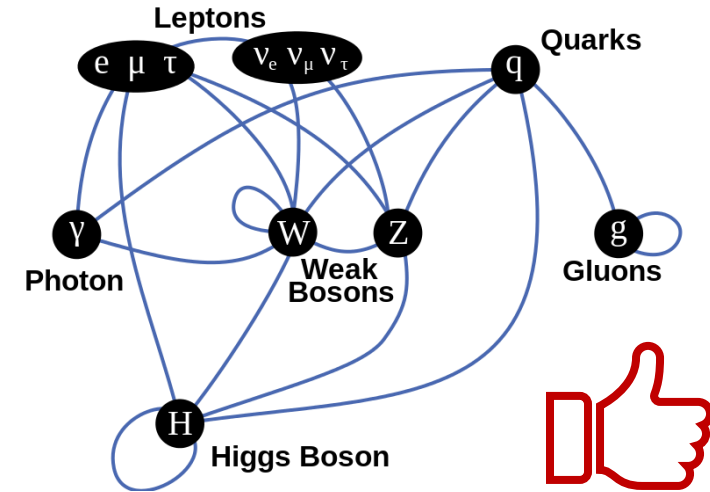
$$\begin{aligned} &2 \text{ MeV} \\ &+ \\ &2 \text{ MeV} \quad \neq 938 \text{ MeV} \\ &+ \\ &4 \text{ MeV} \end{aligned}$$

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$$\begin{aligned} &2 \text{ MeV} \\ &+ \\ &2 \text{ MeV} \quad \neq 938 \text{ MeV} \\ &+ \\ &4 \text{ MeV} \end{aligned}$$



10^{-10} m

ἄ-τομος

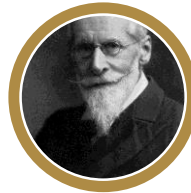
2000

1950

1900

1850

J.J. Thomson



W. Crookes



M. Curie



A. H. Becquerel



W.R. Röntgen

2000

1950

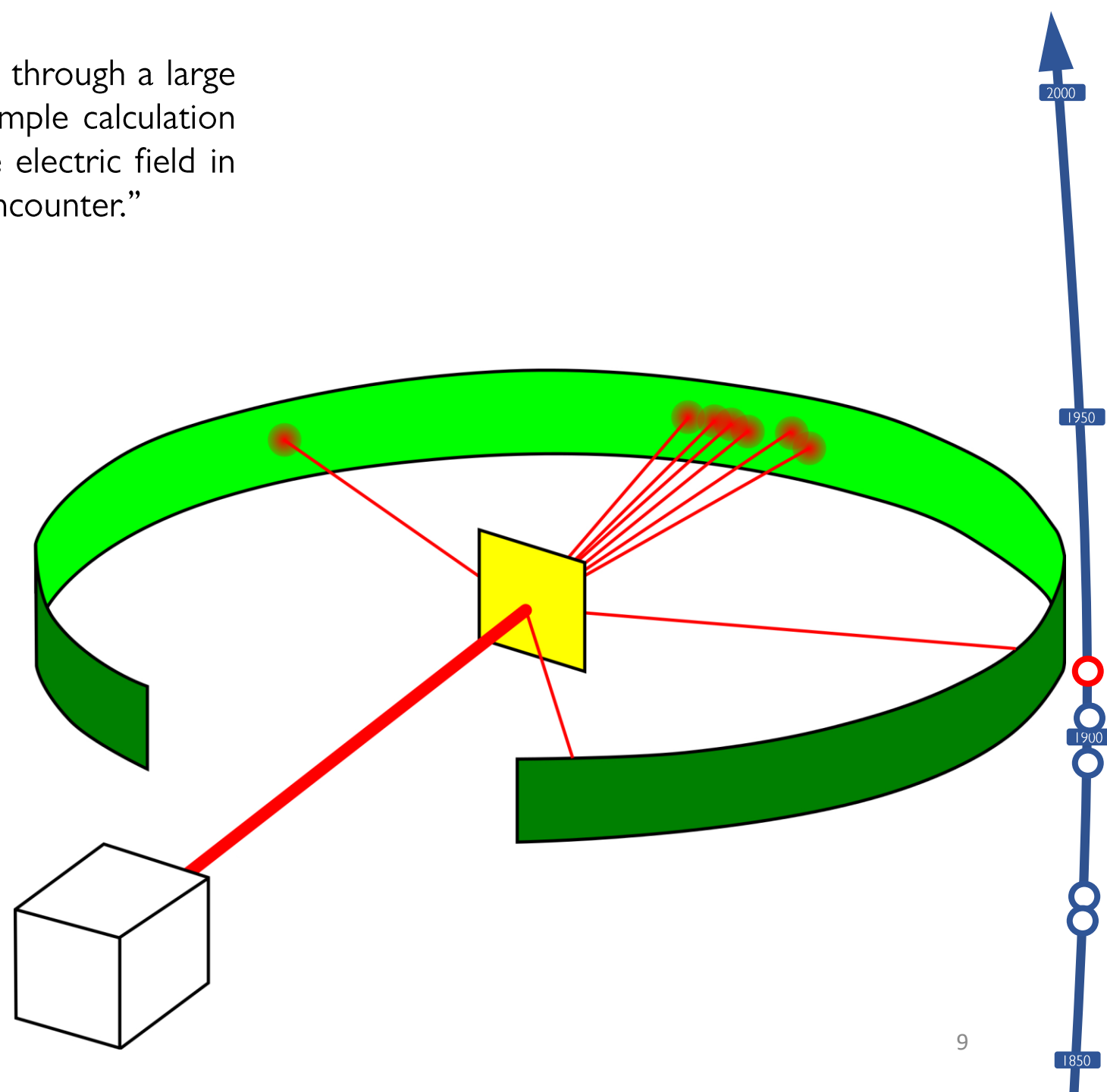
1900

8

1850

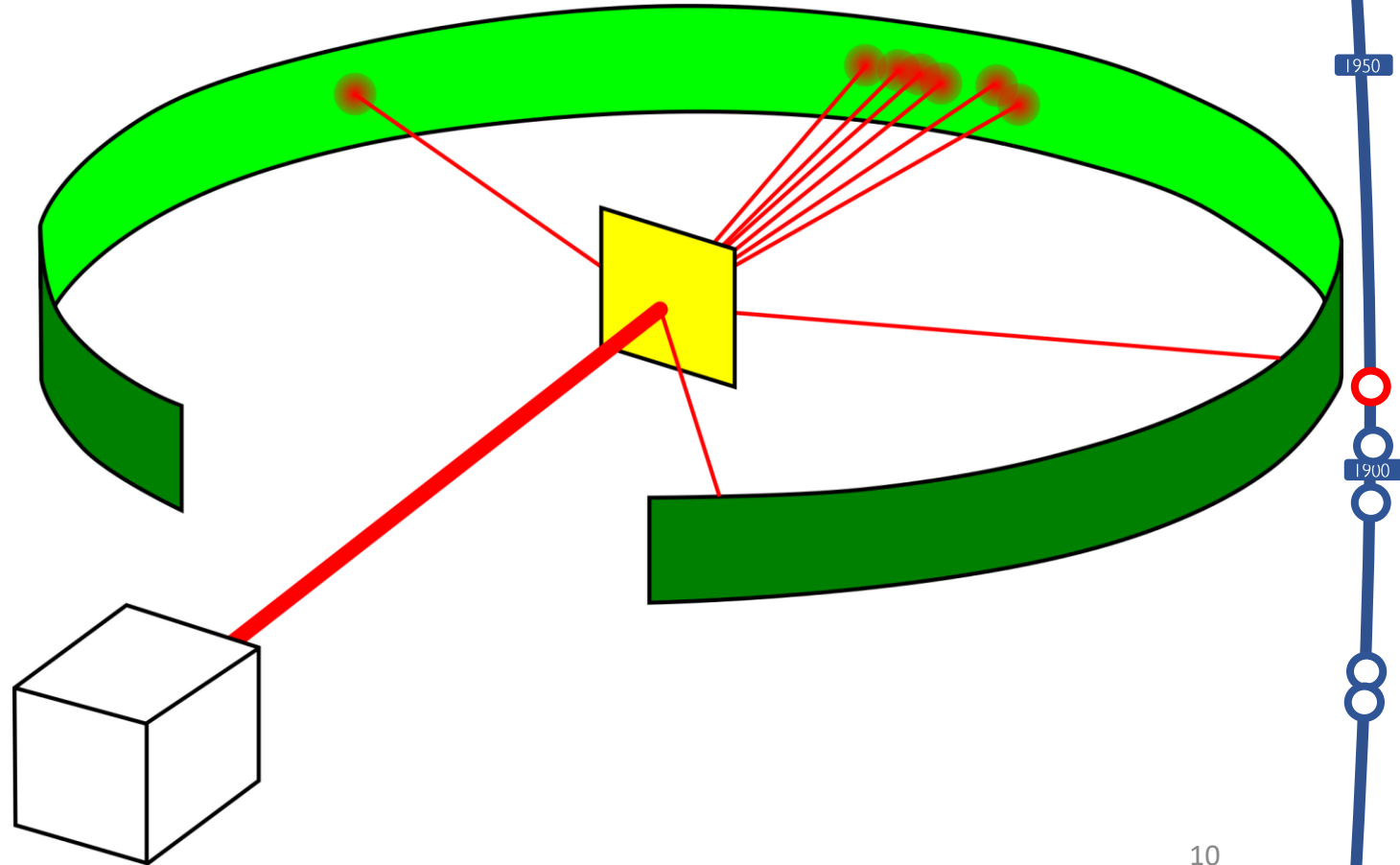
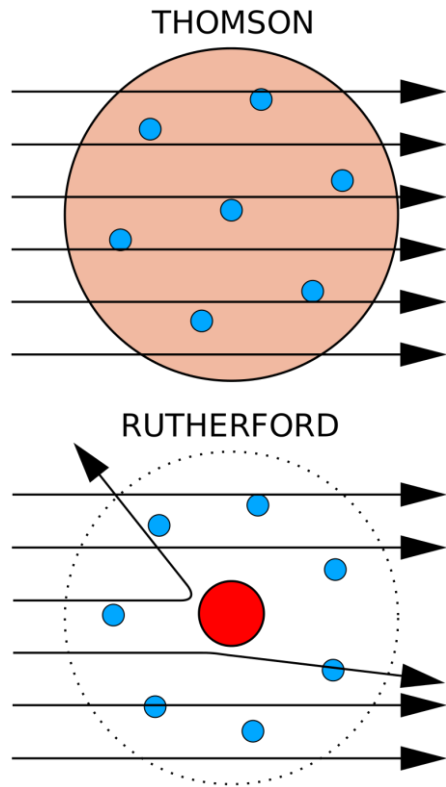
“It seems reasonable to suppose that the deflexion through a large angle is due to a single atomic encounter... A simple calculation shows that the atom must be a seat of an intense electric field in order to produce such a large deflexion at a single encounter.”

E. Rutherford, 1911



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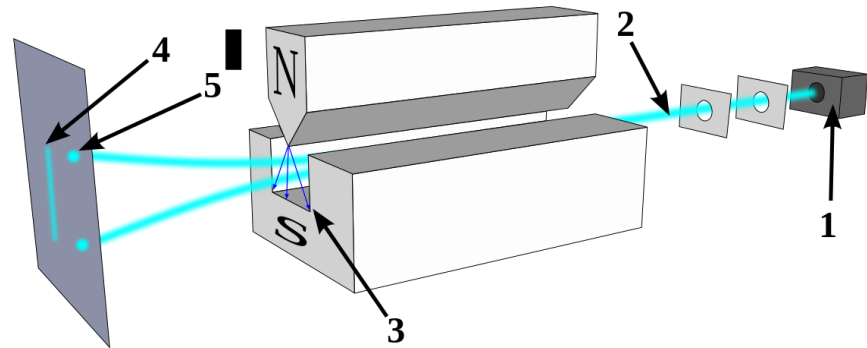
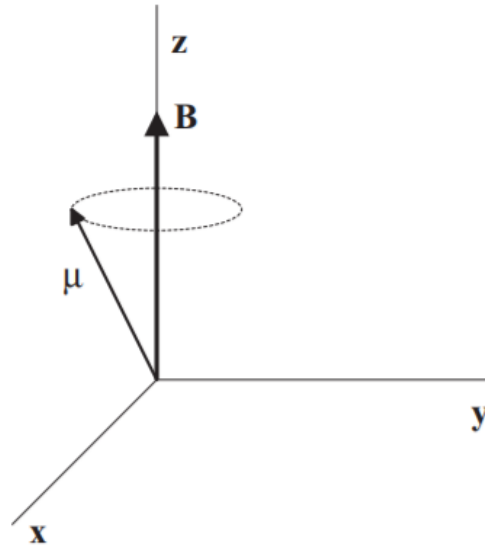
E. Rutherford, 1911



SPIN

Stern, Gerlach (1922)

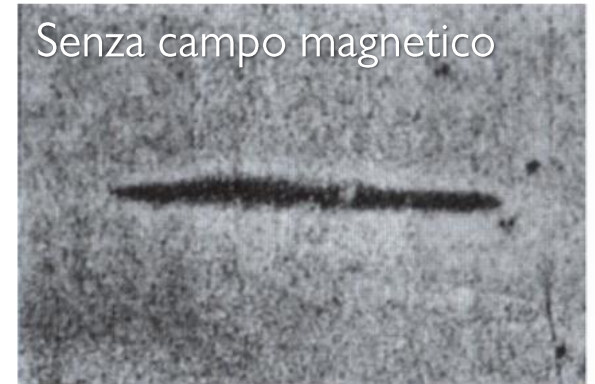
$$F = \mu_z \cdot \frac{\partial B}{\partial z}$$



$$\mu_{Ag} = \mu_B = \frac{e\hbar}{2m_e} = 9.27 \times 10^{-24} \text{ J T}^{-1} (\pm 10\%)$$



Senza campo magnetico



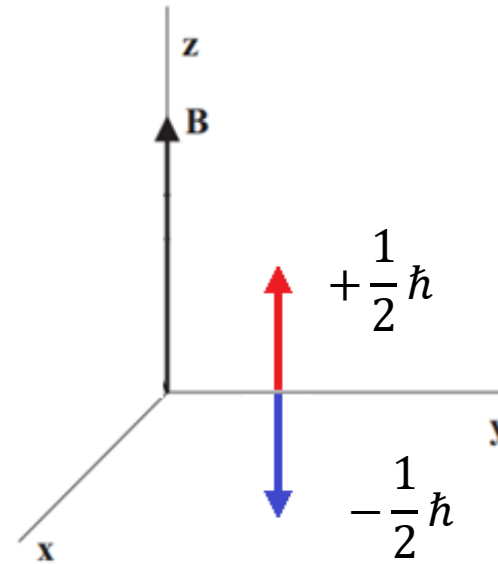
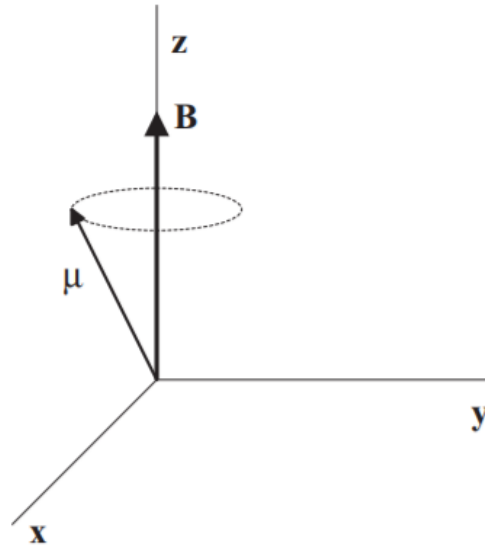
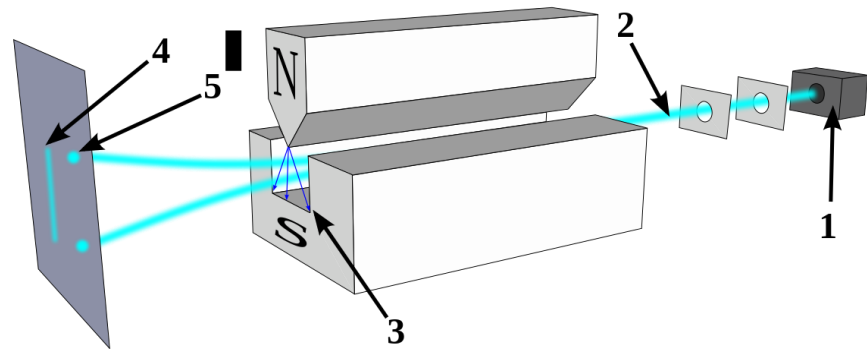
Con campo magnetico



SPIN

Stern, Gerlach (1922)

Uhlenbeck e Goudsmit (1925)



1950

1900

1850

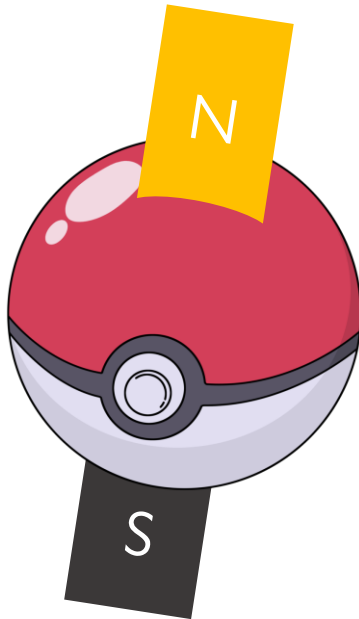
SPIN

Stern, Gerlach (1922)

Uhlenbeck e Goudsmit (1925)

Dirac (1928)

«The question remains as to why Nature should have chosen this particular model for the electron instead of being satisfied with the point-charge.»



$$E = \dots + \boxed{\frac{e\hbar}{2m}} B \cdot \sigma$$



SPIN

Stern, Gerlach (1922)

Uhlenbeck e Goudsmit (1925)

Dirac (1928)

«The question remains as to why Nature should have chosen this particular model for the electron instead of being satisfied with the point-charge.»

Stern, et al. *Magnetic moment of the Proton* (1933)

$$\mu_p = \frac{e\hbar}{2m_p} ?$$

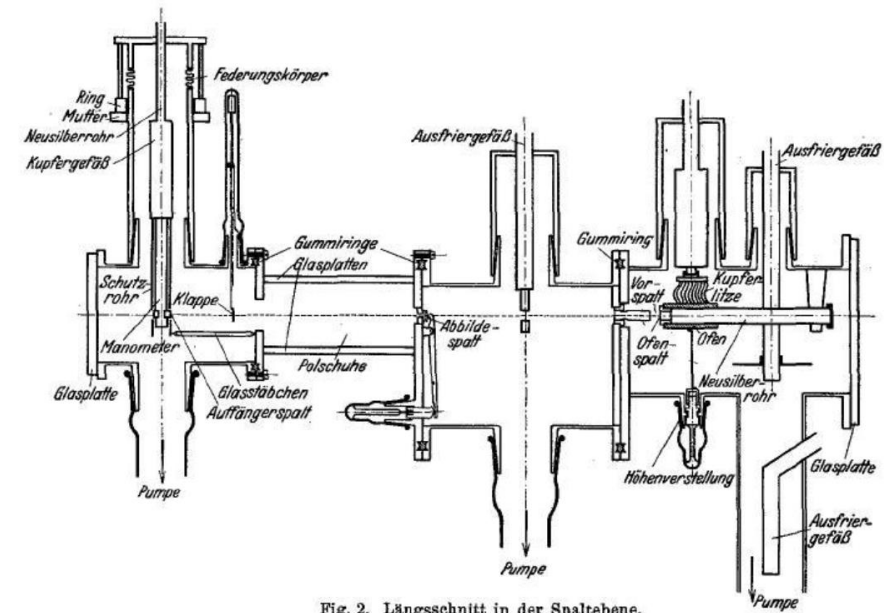


Fig. 2. Längsschnitt in der Spaltebene.

SPIN

Stern, Gerlach (1922)

Uhlenbeck e Goudsmit (1925)

Dirac (1928)

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Stern, et al. *Magnetic moment of the Proton* (1933)

$$\mu_p = \frac{e\hbar}{2m_p} (1 + k_p) \quad k_p = 1.5 \pm 10\%$$

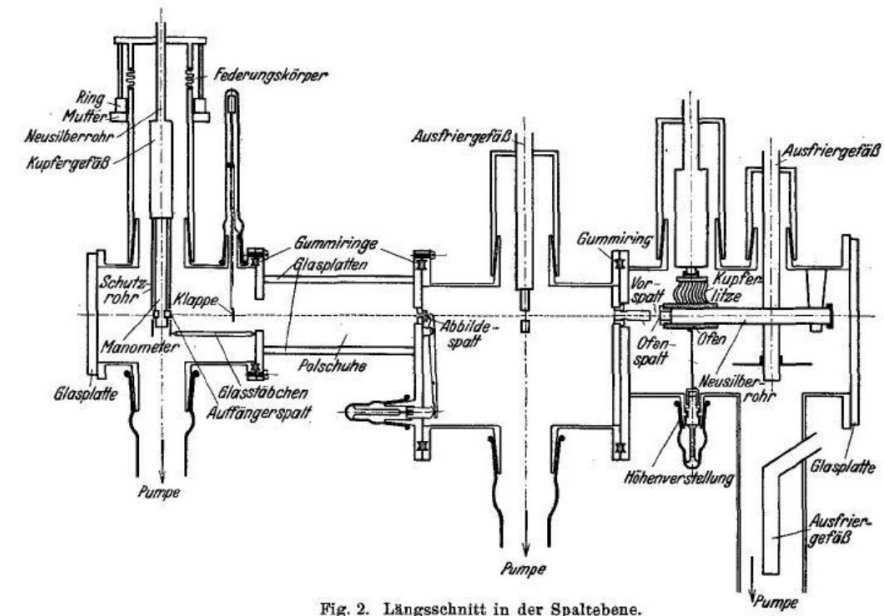



Fig. 2. Längsschnitt in der Spaltebene.

SPIN



Momento magnetico
anomalo



Particella
puntiforme



SPIN



Momento magnetico
anomalo



Particella
puntiforme

- I. Il protone non è elementare
e ha dimensione finita
→ *Fattori di forma*

2000

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SPIN



Momento magnetico
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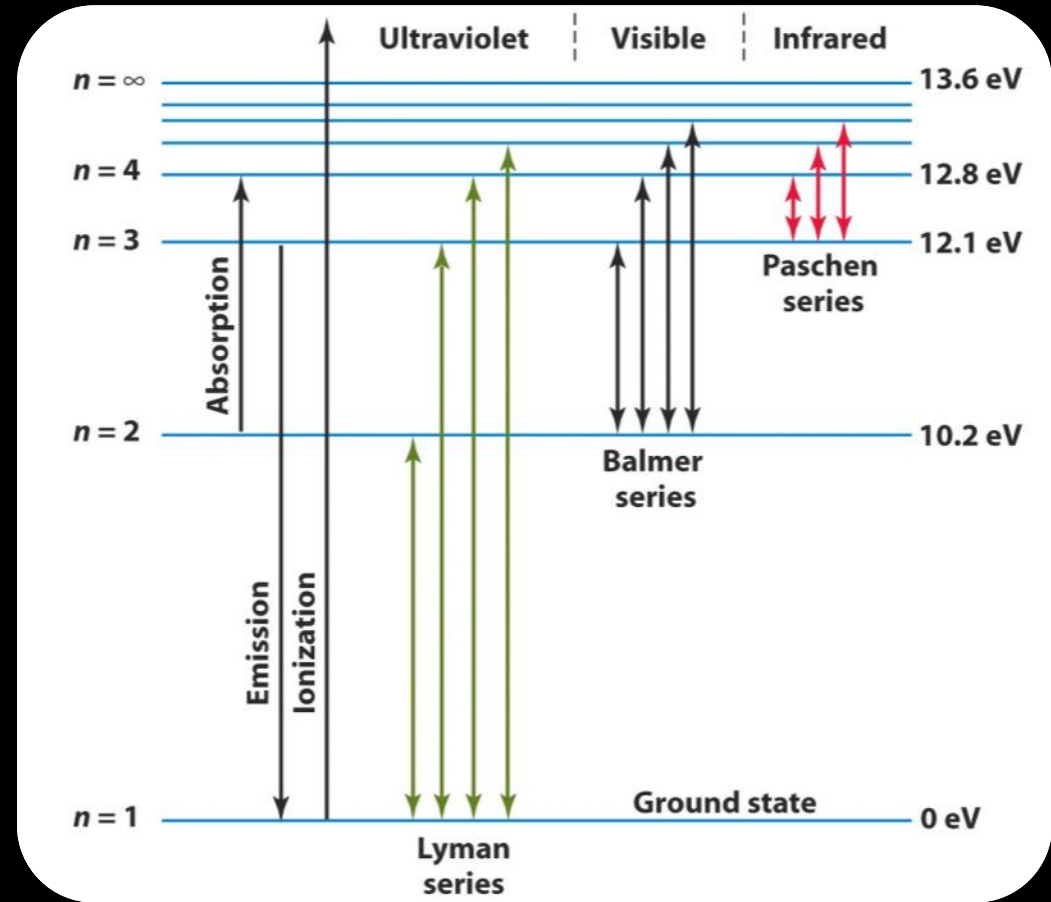


Particella
puntiforme

1. Il protone non è elementare
e ha dimensione finita
→ *Fattori di forma*
2. Deve possedere uno
spettro di eccitazione
→ *Stati eccitati*

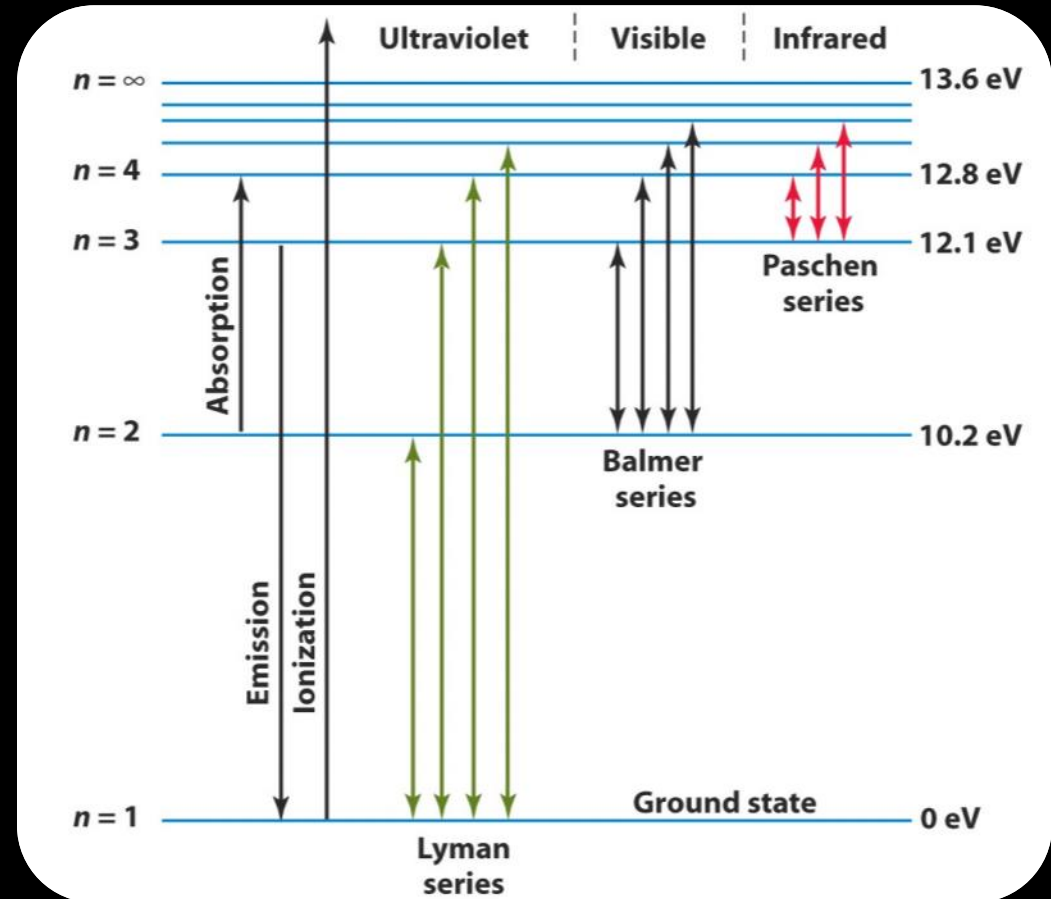
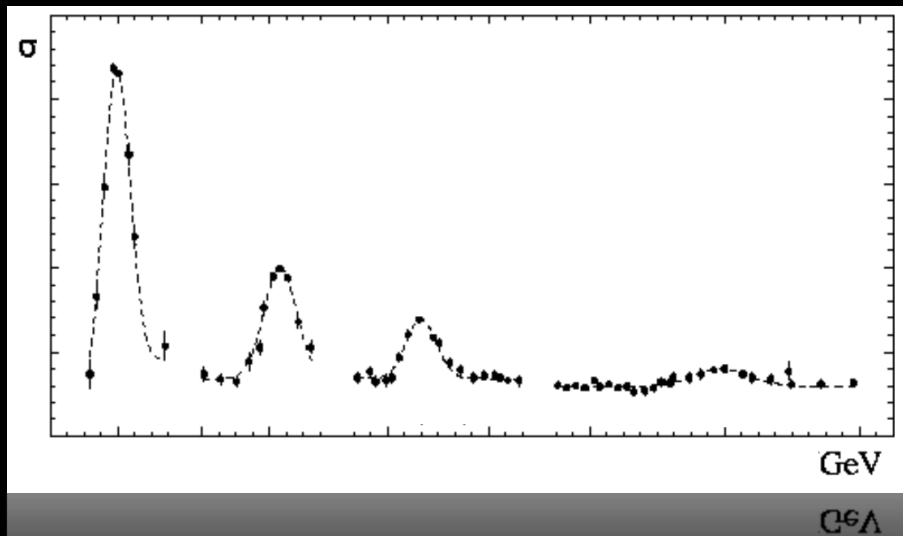


Energia



$$\sigma(\gamma p \rightarrow f) = \frac{n_f}{n_\gamma} \frac{1}{\rho_p \Delta z}$$

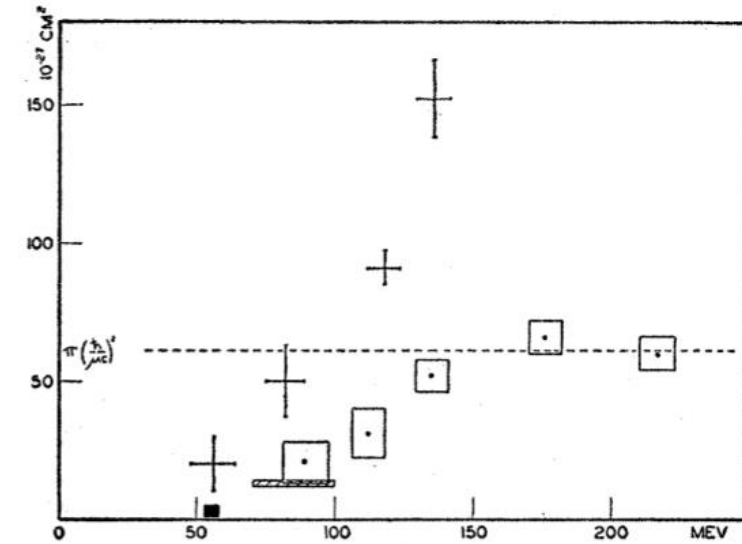
Energia



Scattering con pioni

Fermi (1952)

1. $\pi^+ p \rightarrow \pi^+ p$
2. $\pi^- p \rightarrow \pi^0 n$
3. $\pi^- p \rightarrow \pi^- p$



Scattering con pioni

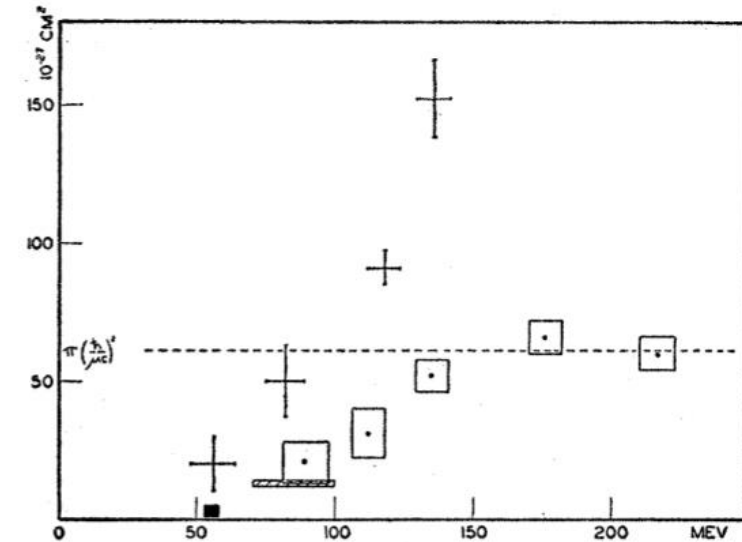
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Brueckner: risonanza con spin 3/2 e isospin 3/2

→ Rapporto sezioni d'urto 9 : 2 : 1

→ Distribuzione angolare $\propto \cos^2 \vartheta$



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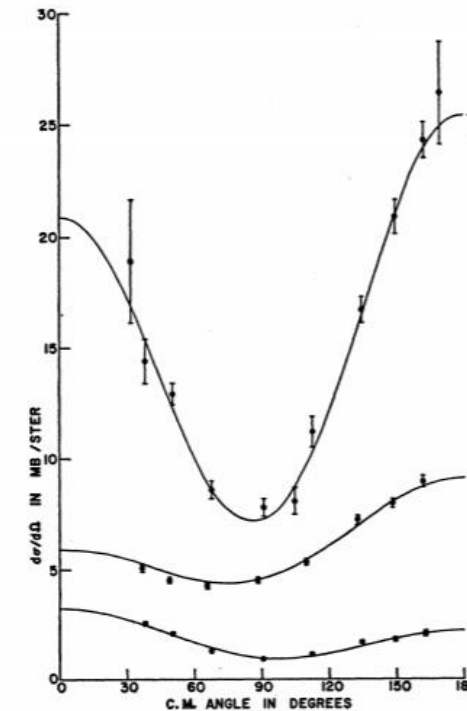
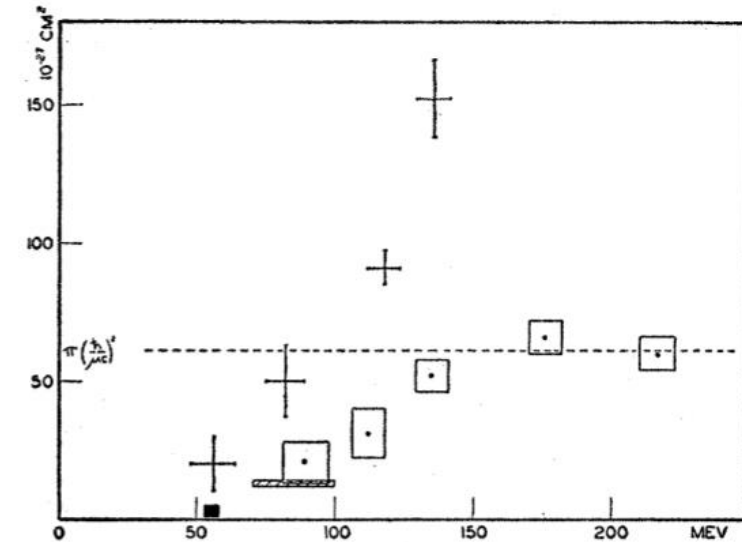
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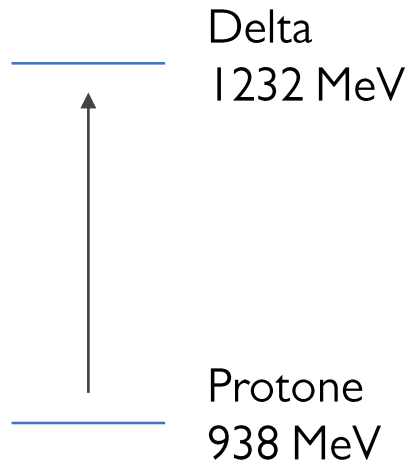
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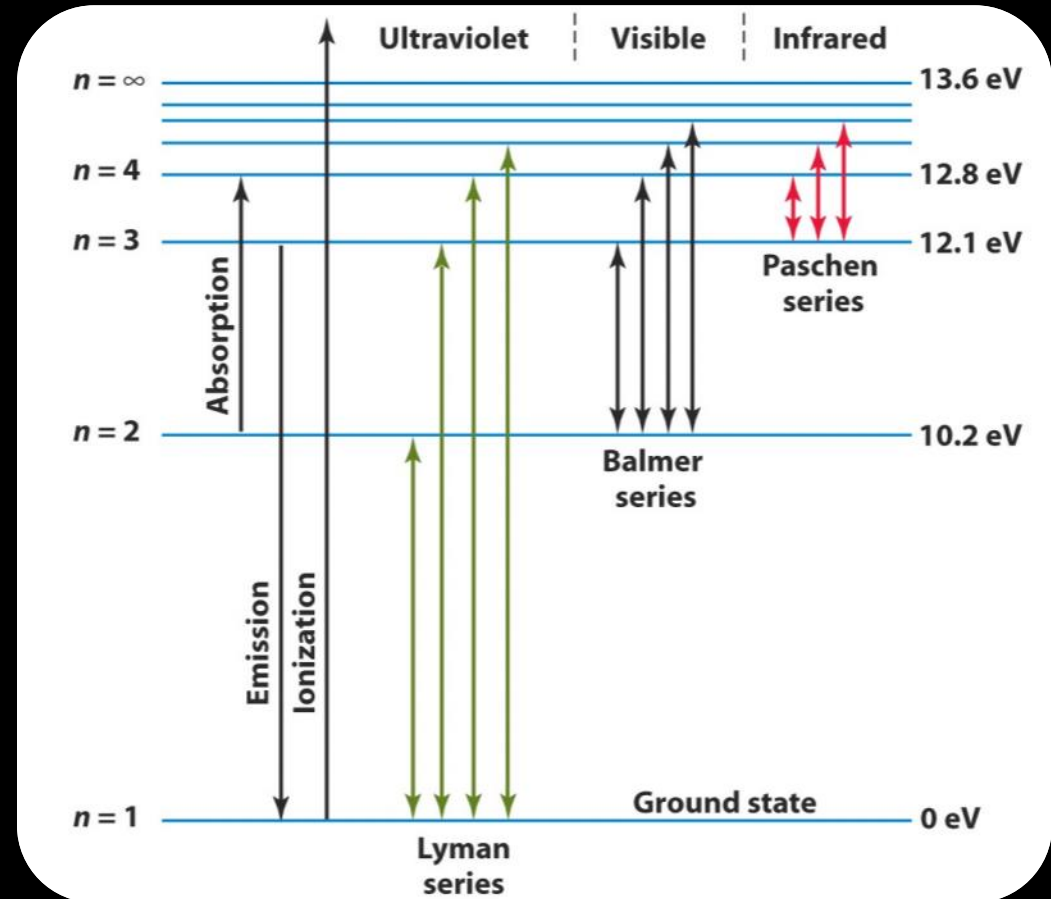
Ashkin et al, *Pion-Proton Scattering at 150 and 170 Mev* (1955)

Primo stato eccitato: $\Delta(1232)$

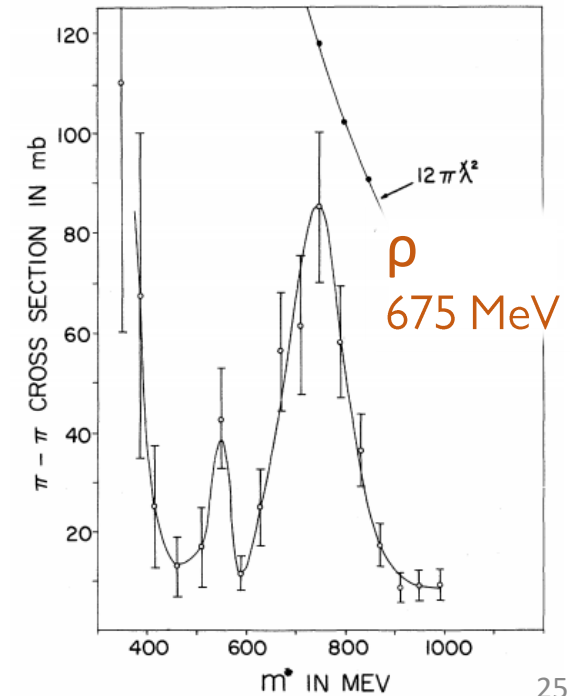
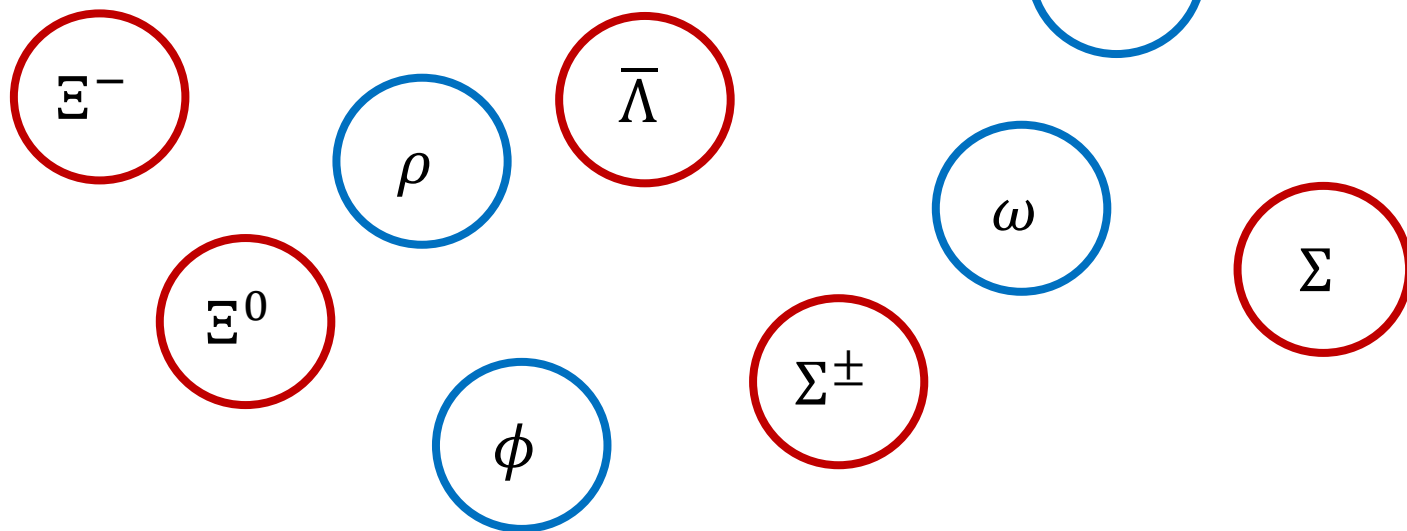
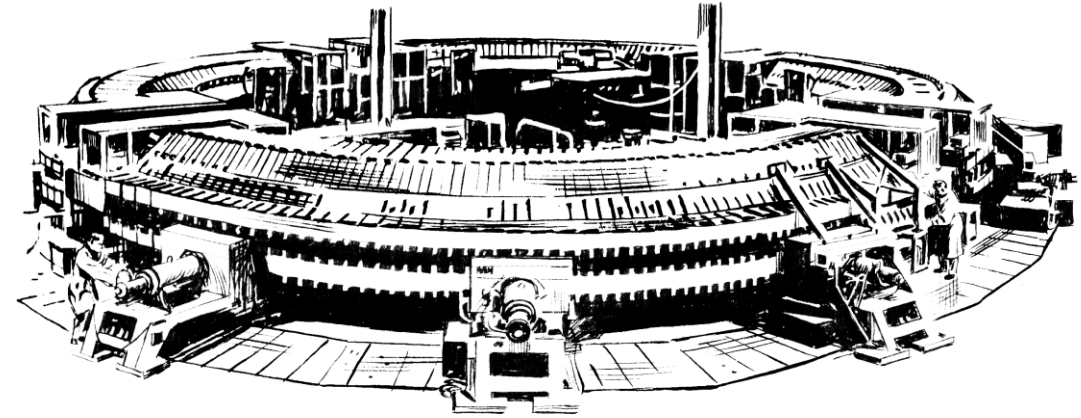
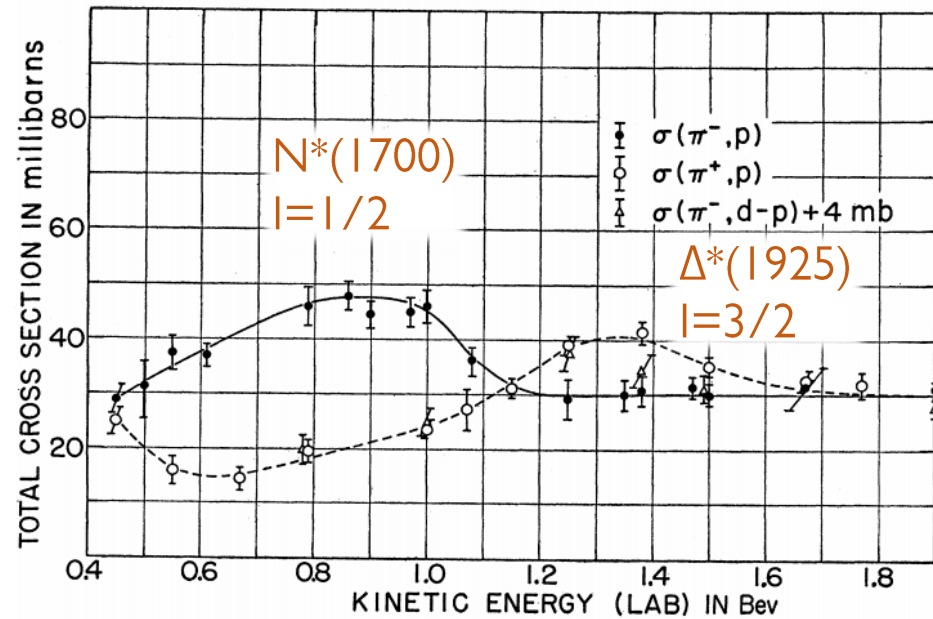




Energy



Risonanze



Data on Elementary Particles and Resonant States (1964)

2000

1950

1900

1850

Mesons

	Mass (MeV)	$I(J^{PG})CA$ — = estab.	Symb.	Γ (MeV)	M^2 (BeV ²)	Important decays				
						Partial modes	Frac- tion %	Q (MeV)	p or Pmax (MeV/c)	
η	548.7 ± 0.5	$0(0^{++})C^+A^-$	η_p	<10	0.301	See table S				
ω	782.8 ± 0.5 Xscale = 1.8	$0(1^{--})C^-A^-$	η_Y	9.4 ± 1.7	0.613	$\pi^+\pi^-\pi^0$ $\pi^+\pi^-\pi^0$ neutral($\pi^0\gamma$) $\pi^+\pi^-\gamma$ $e^+e^-\gamma$ $\mu^+\mu^-$	86 <1 11 $\pm$ 1 3.2 $\pm$ 1 <0.3 <0.5	369 504 648 504 782 572	327 366 380 366 391 377	
$\eta 2\pi$	959 ± 2	$0(0^{++}, 1^{++}, \dots)C^+A^-$	η	<12	0.920	$\eta 2\pi$ 2π 3π 4π 6π $\pi\pi\gamma$	large <20 <30 <3 <3 ?	131 680 540 400 121 680	232 459 427 372 189 459	
Conceivably strongly decaying $1(J^{P++})C^-$ or electromagnetic decay of $G = -1$ meson										
$K_1 K_1$	~ 1000	May be just large KK scattering length, see listings of data cards.								
ϕ	1019.5 ± 0.3 Xscale = 1.7	$0(1^{--})C^-A^+$	η_Y	3.1 ± 0.6	1.040	$K_1 K_2$ $K^+ K^-$ $\pi\pi$ $\pi^0 + 3\pi$ $\pi^0 \gamma$	41 $\pm$ 6 59 $\pm$ 6 <8 <10 ?	23 32 740 117 885	109 126 490 188 501	
Suppressed by $A=+1$ approximation										
f	1253 ± 20	$0(2^{++})C^+A^+$	η_a^{II}	100 ± 25	1.571	$\pi\pi$ 4π KK	large 8 $\pm$ 6 ?	974 695 265	611 547 386	
$KK\pi$	1410	$\leq 1(0^{++}, 1^{++}, \dots)C^+A^-$	η	60		$K^* K$ $KK\pi$ 2π KK 3π	large small ? ? ?	25 283 1131 422 991	126 421 691 503 670	
If we guess $I=0$, then $G=+1$										
$\pi^\pm$	139.6	$1(0^{--})C_n^+A^-$	π_β			See table S				
π^0	135.0	$1(0^{--})C_n^+A^-$								
ρ	763 ± 4	$1(1^{++})C_n^+A^+$	π_Y	106 ± 5	0.582	2π 4π	100 small	483 204	355 241	
Xscale=1.5										
A_1	1090 ± 7	$\geq 1(0^{--})C_n^+A^-$	π	125 ± 25		$\rho\pi$ KK	~ 100 <5	188 G-forbidden for odd l if $I=1$	251	
May be just large $\rho\pi$ scattering length Only recently separated from A_2										
B^+	1215 ± 18	$1(1^{++}, 2^{--})C_n^+A^+$	π_δ	122 ± 17	1.476	$\omega\pi$ $\pi\pi$ KK 4π	~ 100 <30 <10 <50	293 I forbidden for even l G forbidden for even l 657	335 335 525	
Xscale = 1.9										
A_2	1340	$1(2^{+-})C_n^+A^+$	π_a^{II}	80		$\rho\pi$ KK $\eta\pi$	~ 70 $\sim 30 \pm 7$ seen	408 816 622	418 562 529	
Only recently separated from $A_1(1090)$										
$K^\pm$	493.8	$1/2(0^-)A^-$	K_β		0.244	See table S				
K^0	498.0	$1/2(0^-)A^-$								
κ	725	Existence not yet definitely established								
K^*	891 ± 1	$1/2(1^-)A^+$	K_Y	50 ± 2	0.794	$K\pi$ $K\pi\pi$ $\pi\pi$	~ 100 <0.2 <0.2	258 118 27	288 215 82	
Xscale=1.3										
K_C	1215 ± 15	$\leq 3/2(1^+)A^-$	K	60 ± 10	1.476	$K\rho$ $K^*\pi$	strong ?	-30 184	<0 253	

A. H. Rosenfeld, A. Barbaro-Galtieri, W. H. Barkas, P. L. Bastien, J. Kirz, M. Roos
UCRL-8030 - Part I. June 1964.

Baryons

	Beam πp (MeV) or Kp (MeV/c)	$I(J^P)$ — = estab.	Sym- bol	Mass (MeV)	Γ (MeV)	Mass ² (BeV ²)	Important Decays			
							Partial mode	Frac- tion (%)	Q (MeV)	p or Pmax (MeV/c)
p		$1/2(1/2^+)$	N_a	938.2 939.6		0.88 0.88	See table S			
n		$1/2(1/2^+)$	N_a	~ 1480	~ 240	2.19	πN	~ 50	402	426
$N_{1/2}^*$ (1480)	550 πp (MeV)	$1/2(1/2^+)$	N_a	~ 1480	~ 240	2.19	πN	~ 50	402	426
$N_{1/2}^*$ (1512)	600 πp	$1/2(3/2^-)$	N_Y	1518 ± 10	125 ± 12	2.30	πN $N\pi\pi$	~ 80	440 301	454 408
$N_{1/2}^*$ (1688)	900 πp	$1/2(5/2^+)$	N_a^{II}	1688	100	2.85	πN $N\pi\pi$	~ 80	610 471	572 538
$N_{1/2}^*$ (2190)	1935 πp	$1/2(9/2^+)$??	$N_a^{III} (?)$	2190	~ 200	4.80	πN ΔK	~ 30	1112 577	888 710
$N_{1/2}^*$ (2700)	3265 πp	$1/2$	N	2700	~ 100	7.29	ηN πN	large ~ 6	1213 1622	1115 1182
$N_{3/2}^*$ (1238)	198 πp	$3/2(3/2^+)$	Δ_0	1236 ± 2	125	1.53	πN	100	160	233
$N_{3/2}^*$ (1920)	1347 πp	$3/2(7/2^+)$	Δ_0^{II}	1924	170	3.70	πN ΣK	34	842 237	722 430
$N_{3/2}^*$ (2360)	2350 πp	$3/2(11/2^+)$??	$\Delta_0^{III} (?)$	2360	~ 200	5.57	πN	~ 10	1282	988
Λ		$0(1/2^+)$	Λ_a	1115.4		1.24	See table S			
Σ		$1(1/2^+)$	Σ_a	+1189.4 -1197.1 1192.4		1.41 1.43 1.42	See table S			
Σ^* (1405)	<0 Kp	$0(1/2^-)$	Λ_β	1405	50	1.97	$\Sigma\pi$ $\Lambda\pi\pi$	100 <1	76 10	151 69
Σ^* (1520)	395 Kp (MeV/c)	$0(3/2^-)$	Λ_Y	1518.9 ± 1.5	16 ± 2	2.31	$\Sigma\pi$ KN $\Lambda\pi\pi$	55 $\pm$ 7 29 $\pm$ 4 16 $\pm$ 2	190 87 124	266 243 251
Σ^* (1815)	1040 Kp	$0(5/2^+)$	Λ_a^{II}	1815	70	3.29	KN $\Sigma\pi$ $\Lambda\pi\pi$ $\Lambda\eta$	80 <10 <15 ?	383 486 420 151	541 504 515 344
Σ		$1(1/2^+)$	Σ_a	+1189.4 -1197.1 1192.4		1.41 1.43 1.42	See table S			
Σ^* (1385)	<0 Kp	$1(3/2^+)$	Σ_0	1382.1 ± 9	53 ± 2	1.91	$\Lambda\pi$ $\Sigma\pi$	96 $\pm$ 4 9 $\pm$ 4	127 55	205 124
Xscale=1.5 Xscale=2.4										
Σ^* (1660)	715 Kp	1	Σ	1660 ± 10	44 ± 5	2.76	KN $\Sigma\pi$ $\Lambda\pi$ $\Sigma\pi\pi$ $\Lambda\pi\pi$	~ 16 ~ 32 ~ 6 ~ 33 ~ 23	225 328 405 188 265	406 383 439 321 389
Σ^* (1765)	940 Kp	$1(5/2^-)$	Σ	1765 ± 10	60 ± 10	3.12	KN $\Lambda\pi$ $\Sigma\pi$	60 510 Not yet resolved from $\Sigma^*(1815)$	343 547	502 517
Only recently resolved from $\Sigma^*(1815)$										
Ξ		$1/2(1/2^+)$	Ξ_a	-1321 1314		1.75 1.73	See table S			
Ξ^* (1530)		$1/2(3/2^+)$	Ξ_0	1529.1 ± 1.0	7.5 ± 1.7	2.34	$\Xi\pi$	~ 100	73	148
Ξ^* (1810)		$1/2$	Ξ	1810 ± 20	~ 70	3.27	$\Xi^0\pi$ $\Lambda^0 K$ $\Xi\pi$ ΣK	~ 45 ~ 45 <10 <10	141 197 354 127	225 386 406 307
Ω		$0(3/2^+)$	Ω_0	1675 ± 3		2.84	See table S			

A. H. Rosenfeld, A. Barbaro-Galtieri, W. H. Barkas, P. L. Bastien, J. Kirz, M. Roos
UCRL-8030 - Part I. June 1964.

- Gell-Mann e Ne'eman, 1961. Simmetria SU(3)

- Gell-Mann e Zweig, 1964

3 particelle elementari
per costruire tutti i barioni e i mesoni

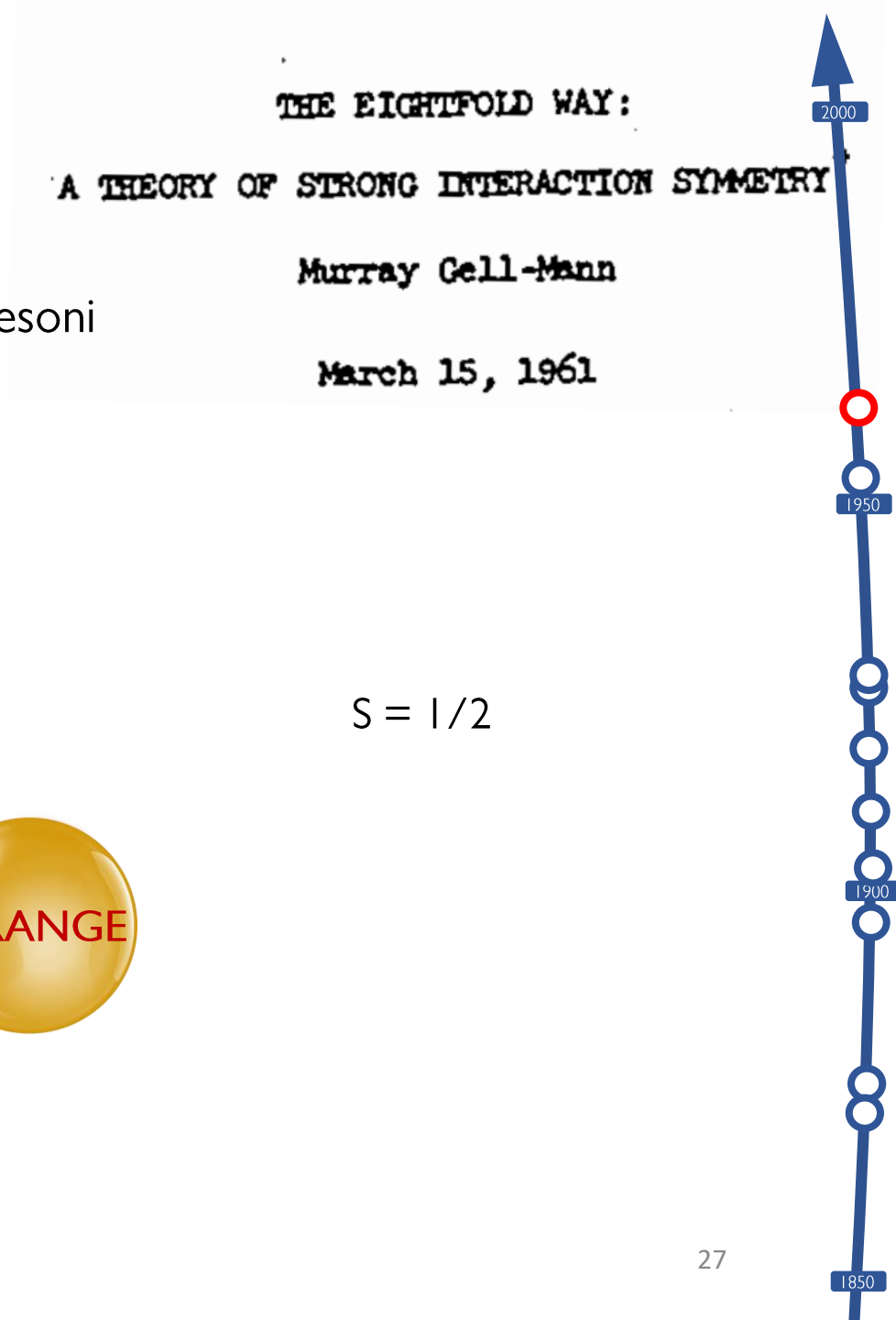
$$Q = +2/3$$



$$Q = -1/3$$



$$S = 1/2$$



- Gell-Mann e Ne'eman, 1961. Simmetria $SU(3)$

- Gell-Mann e Zweig, 1964

3 particelle elementari
per costruire tutti i barioni e i mesoni



udd



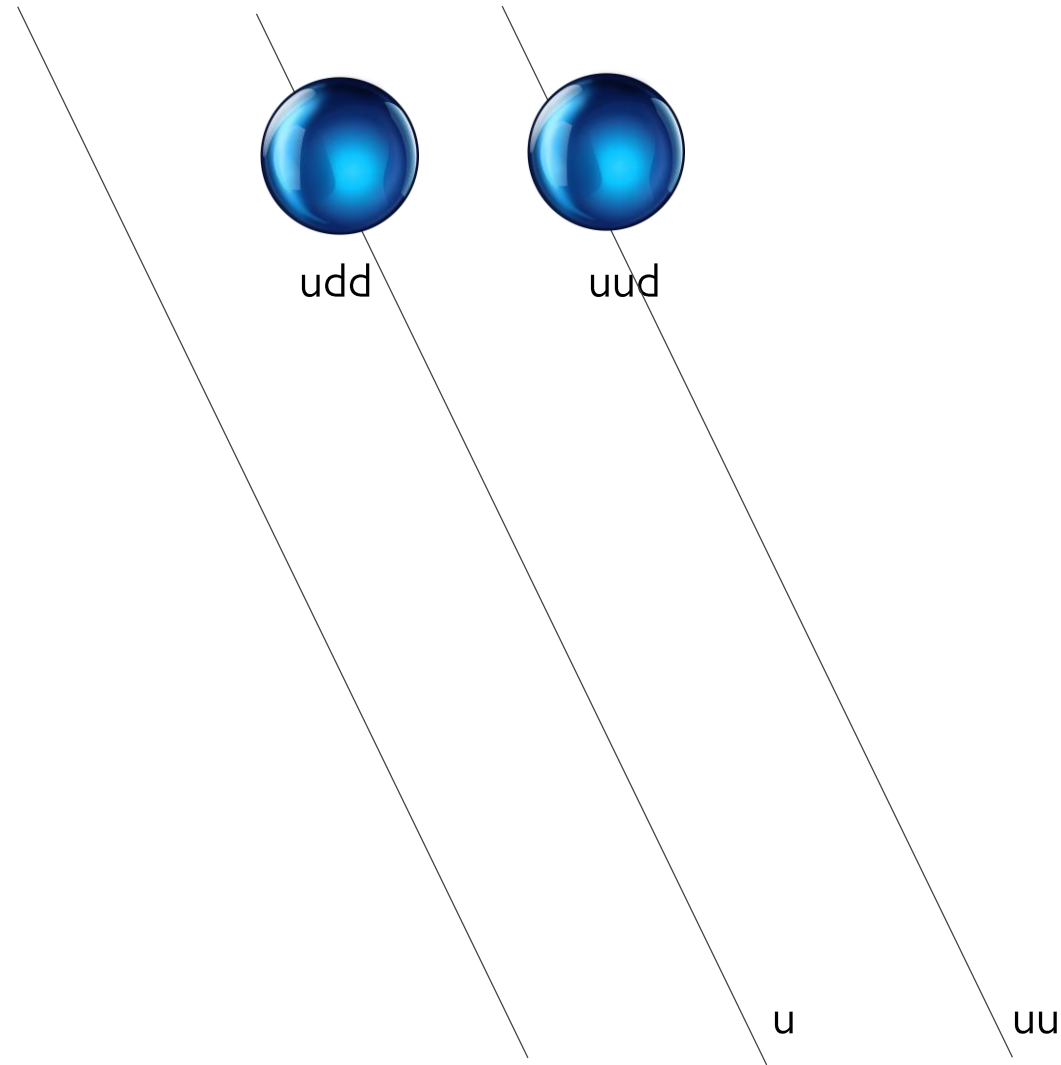
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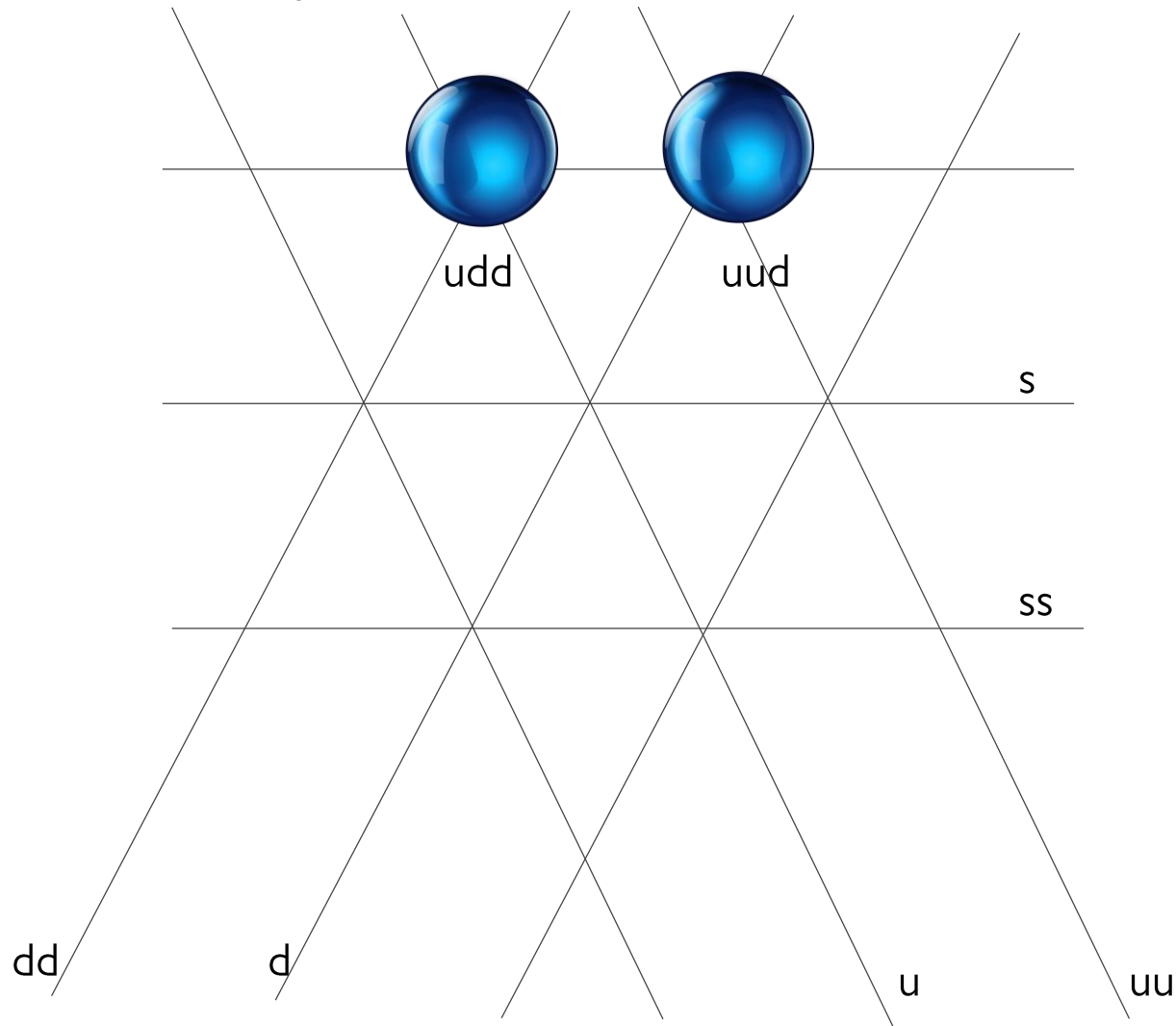
3 particelle elementari
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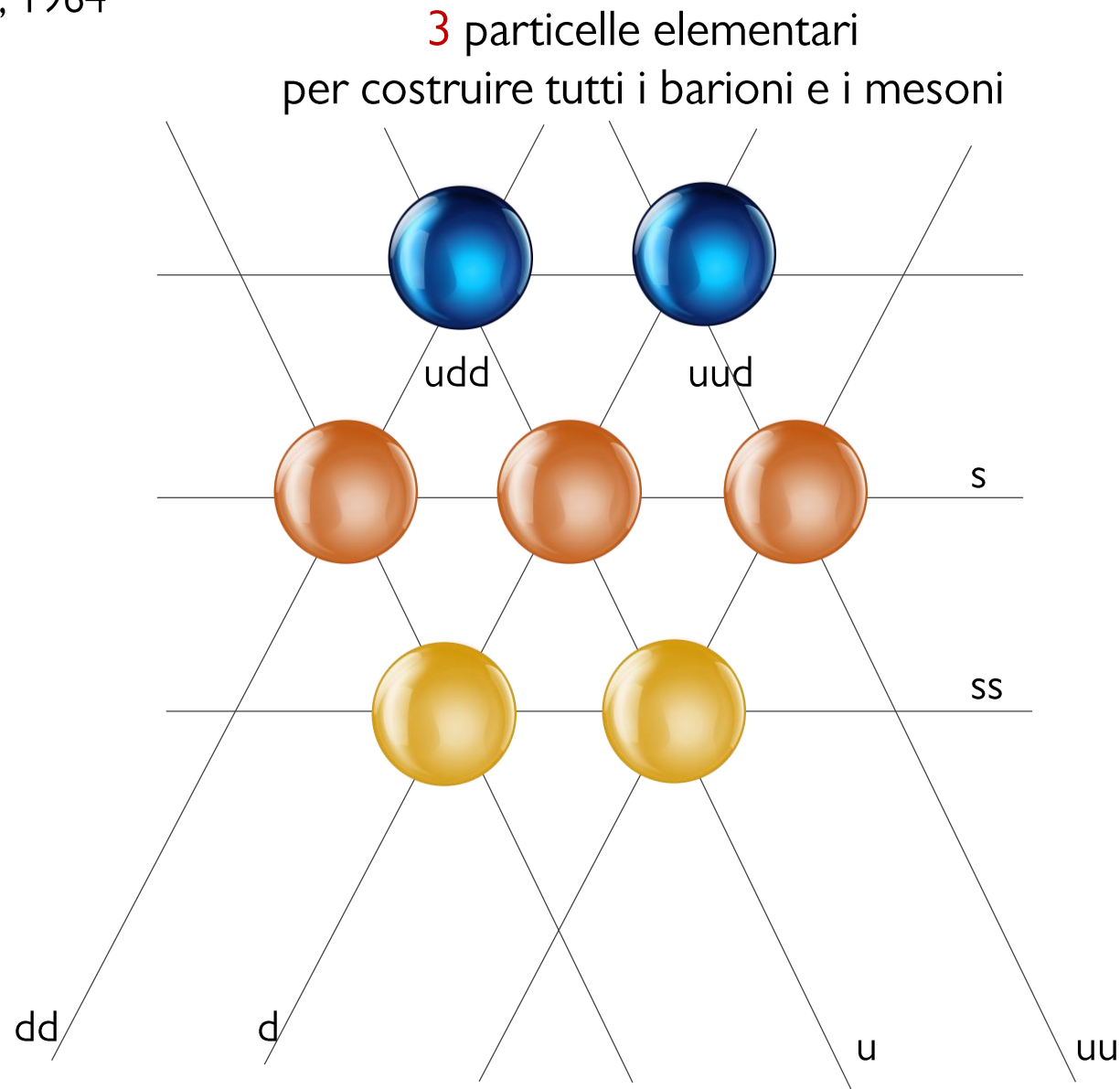
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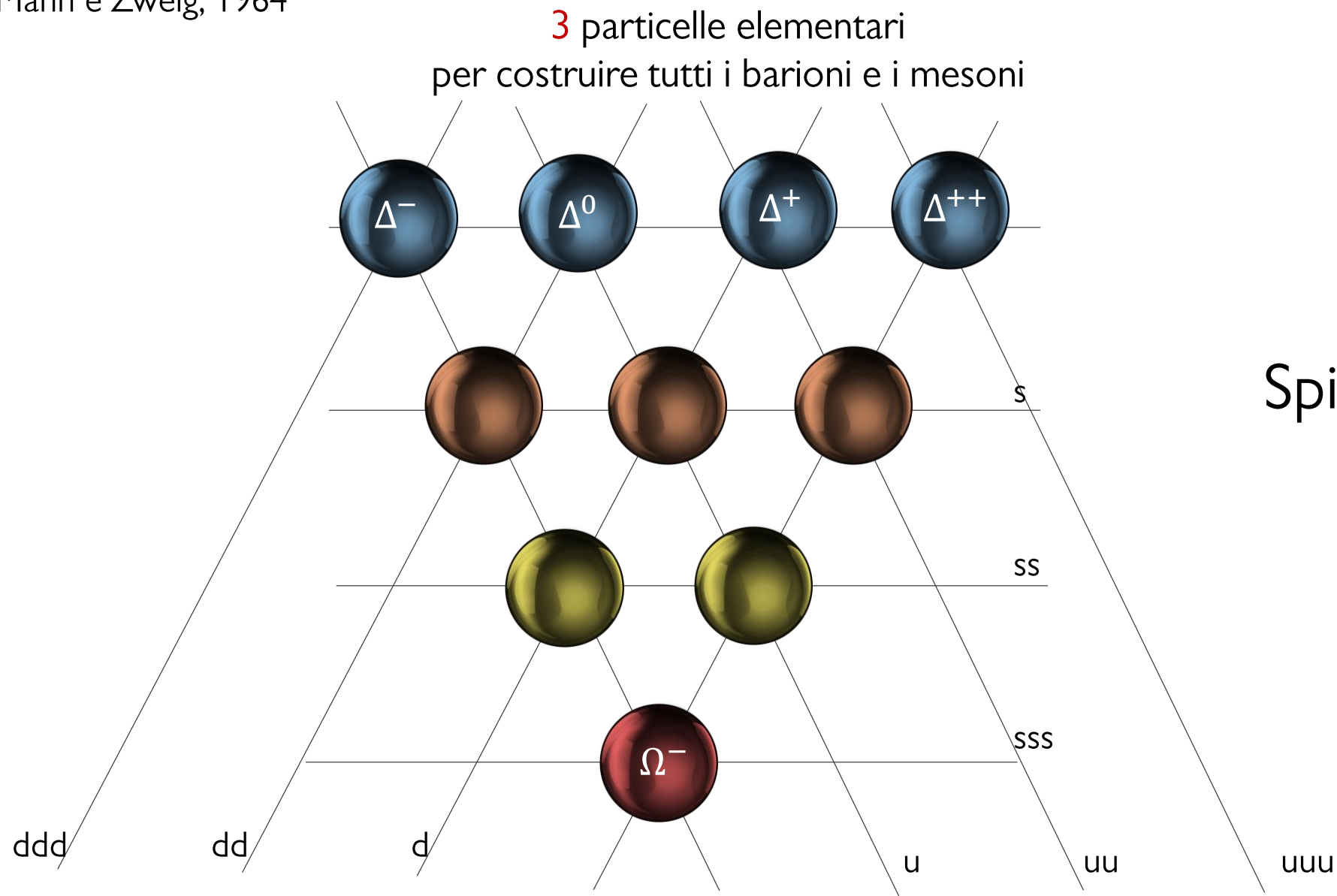
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Spin = $1/2$

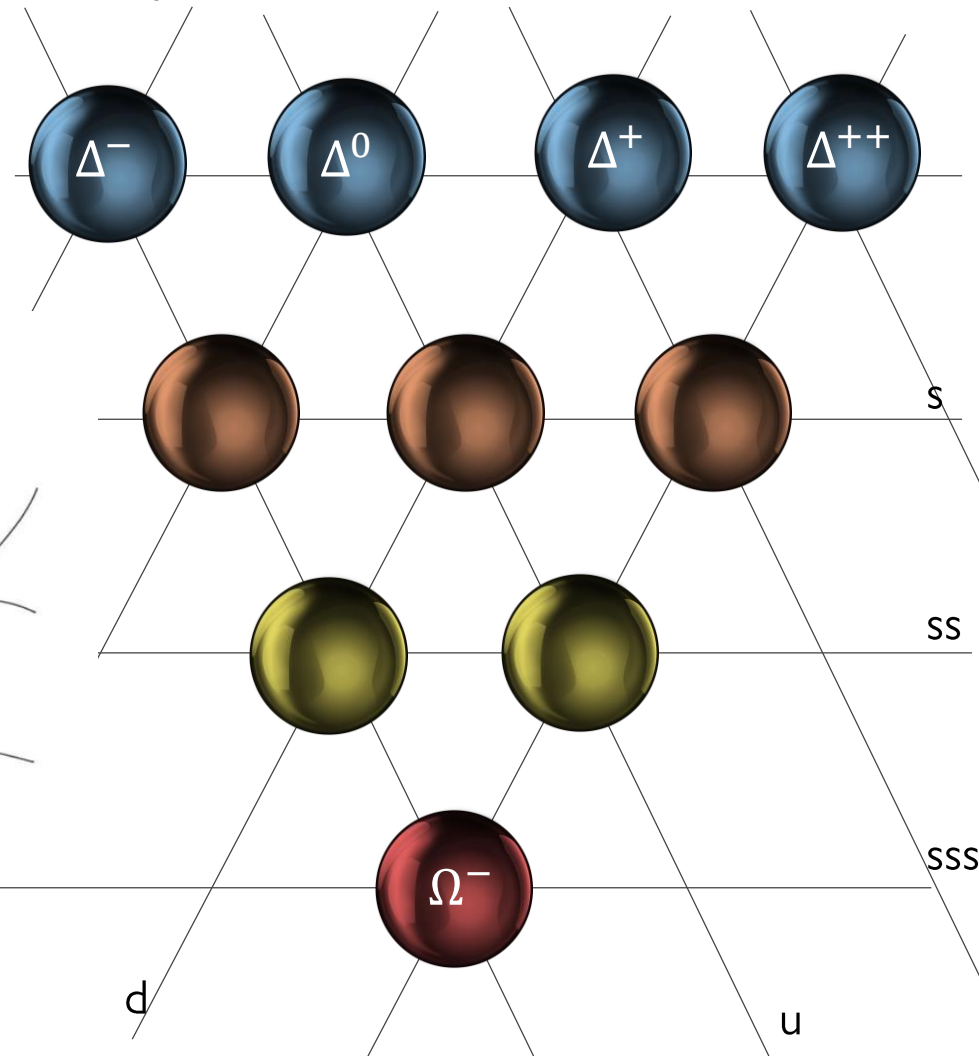


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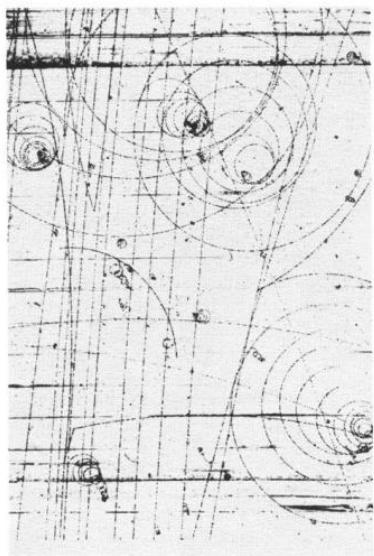


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- Gell-Mann e Zweig, 1964

3 particelle elementari
per costruire tutti i barioni e i mesoni



Spin=3/2



Barnes et al,
1964

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“...the idea that mesons and baryons are made primarily of quarks is hard to believe..”

M. Gell-Mann, 1966

“Additional data are necessary and very welcome to destroy the picture of elementary constituents.”

J. Bjorken, 1967

“I think Professor Bjorken and I constructed the sum rules in the hope of destroying the quark model.”

K. Gottfrid, 1967

“Of course the whole quark idea is ill founded.”

J.J. Kokkedee, 1969

2000



1950

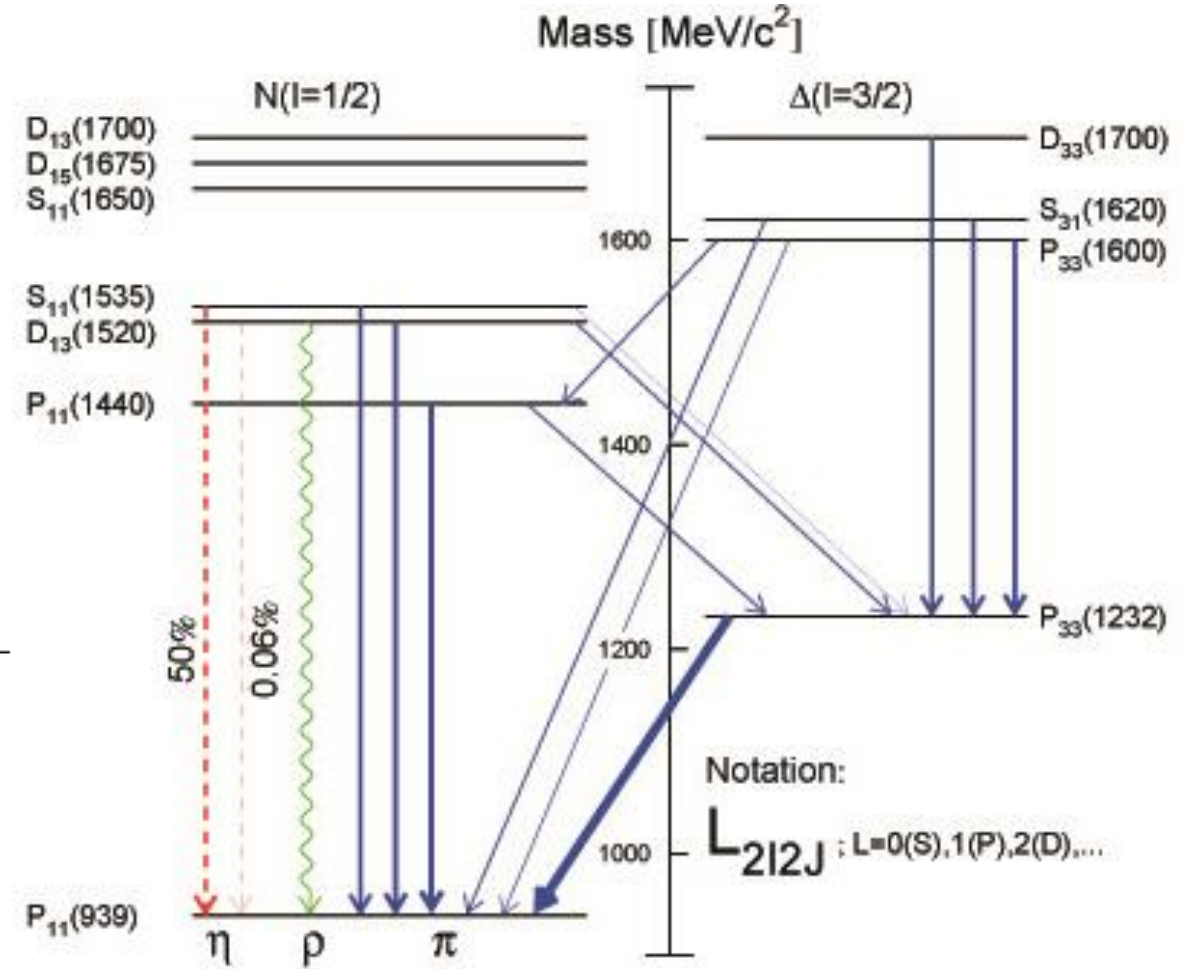
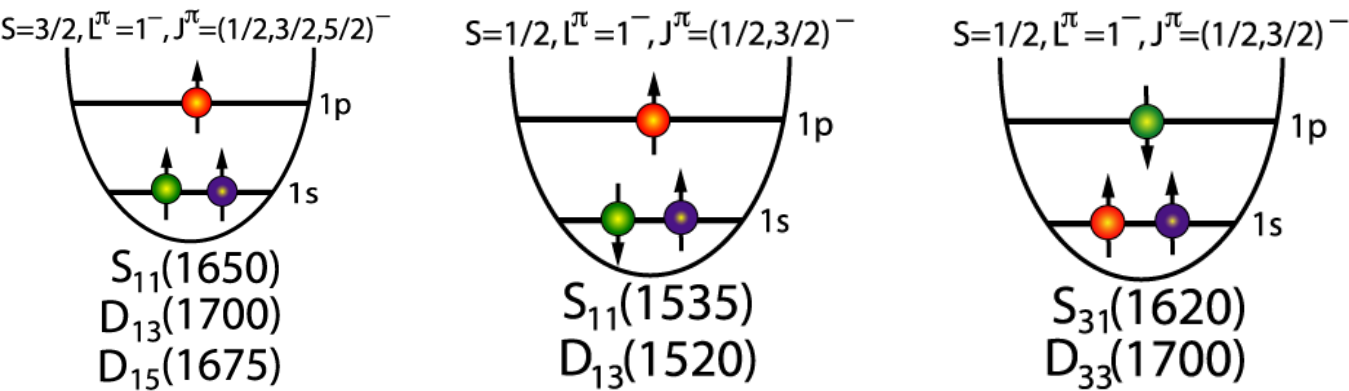
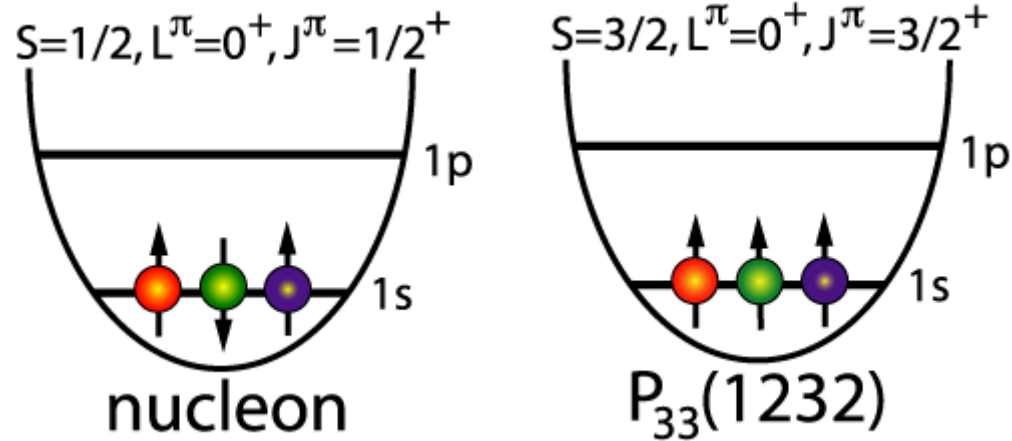


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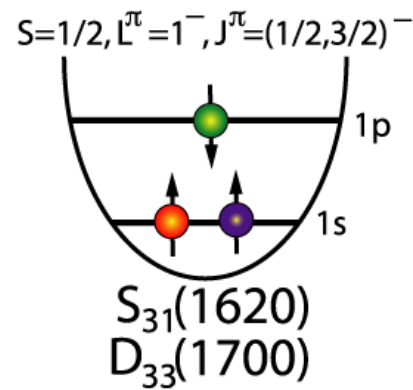
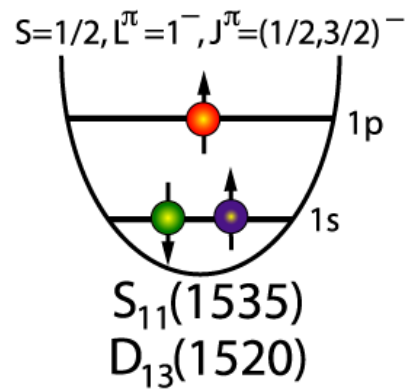
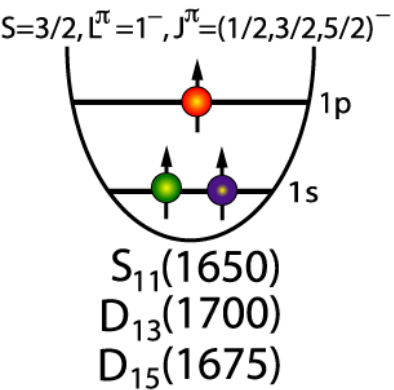
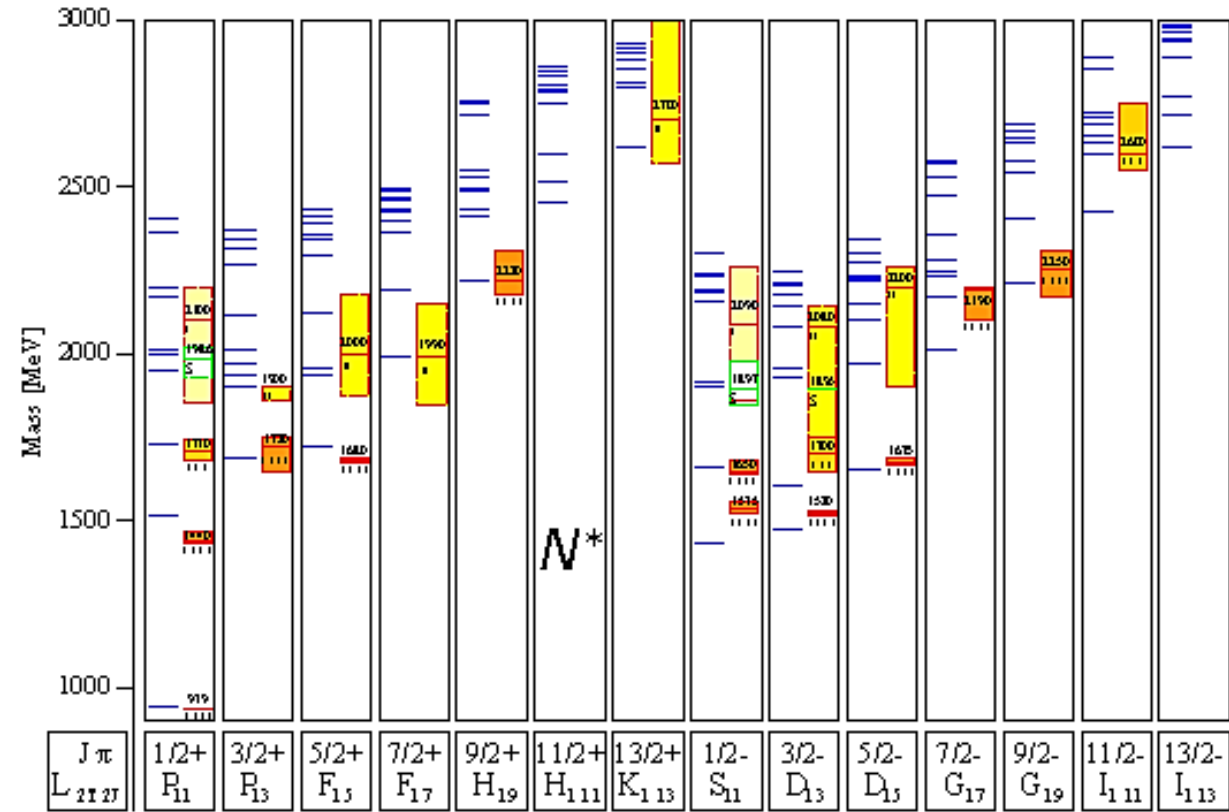
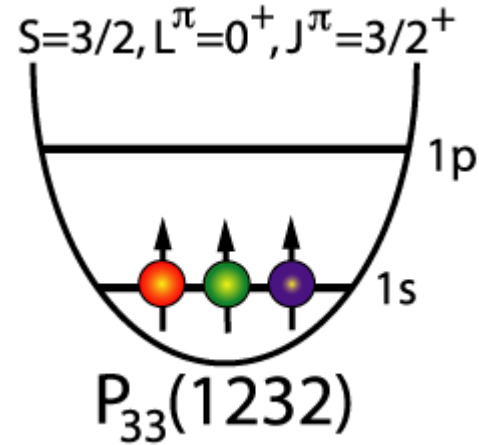
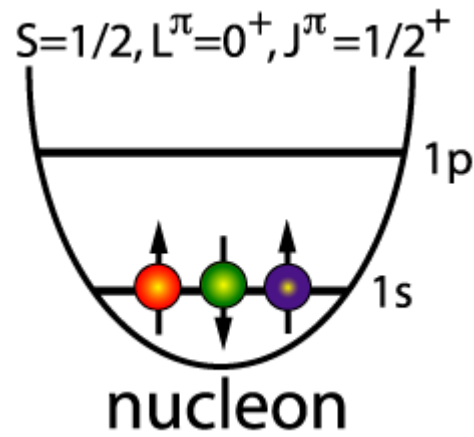


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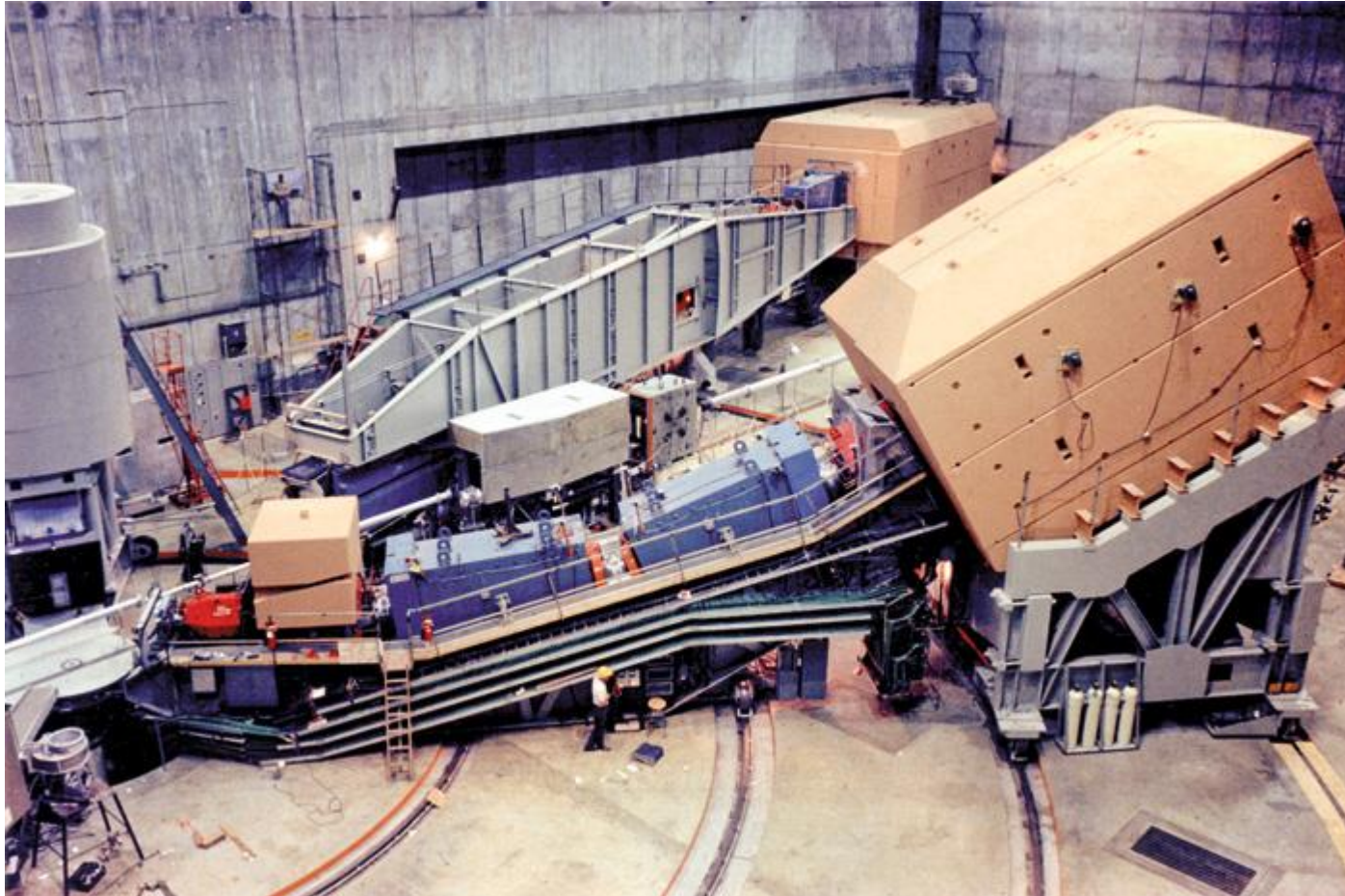
Risonanze



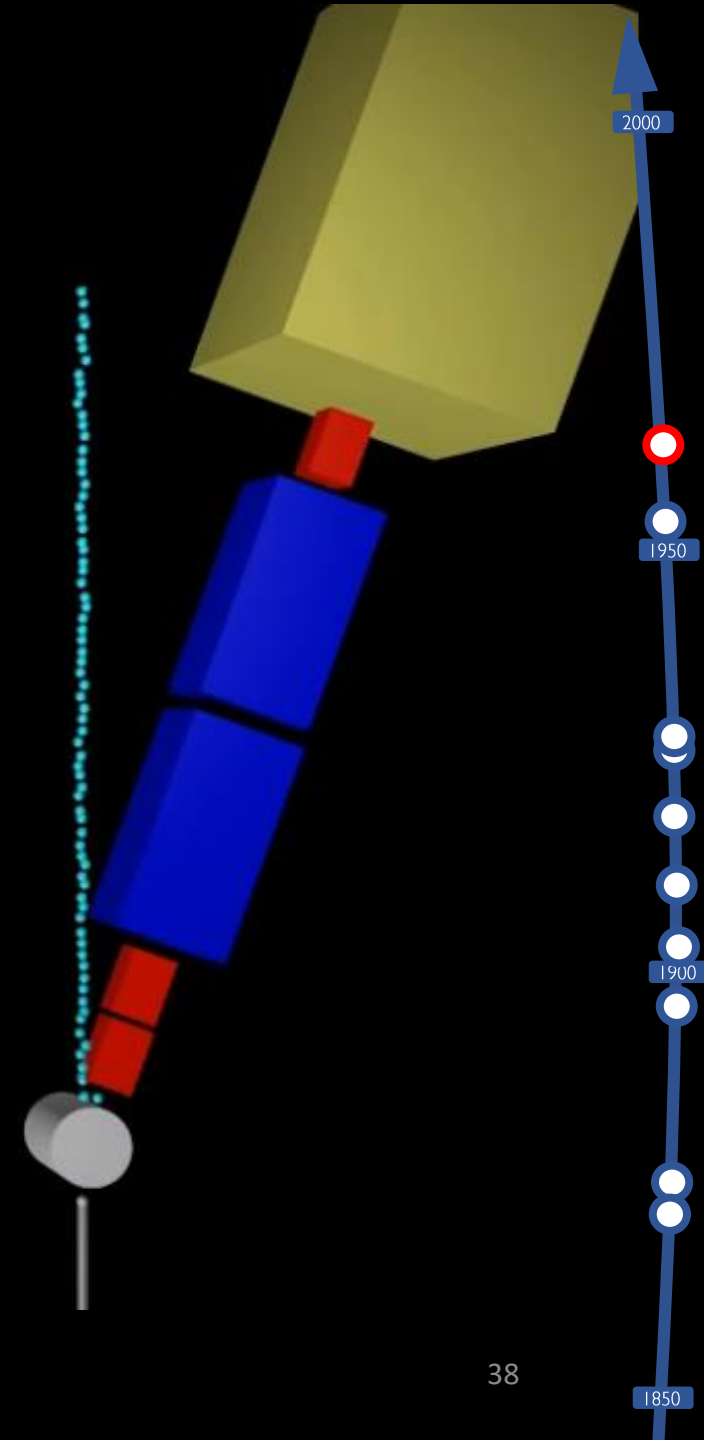
Risonanze



Gli esperimenti a SLAC

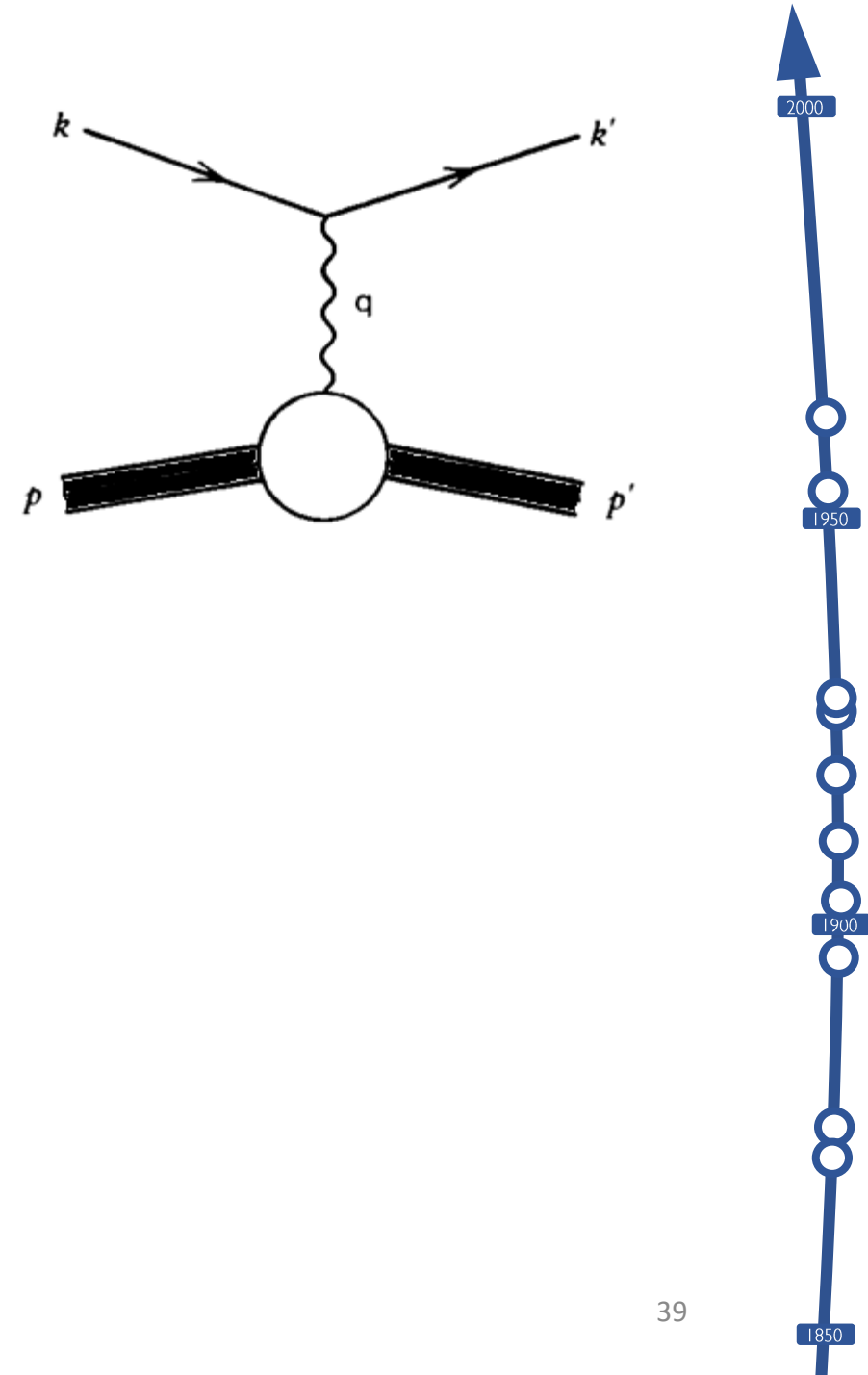


Gli esperimenti a SLAC



Gli esperimenti a SLAC

1968-1973, Scattering elastico... protone "soft"



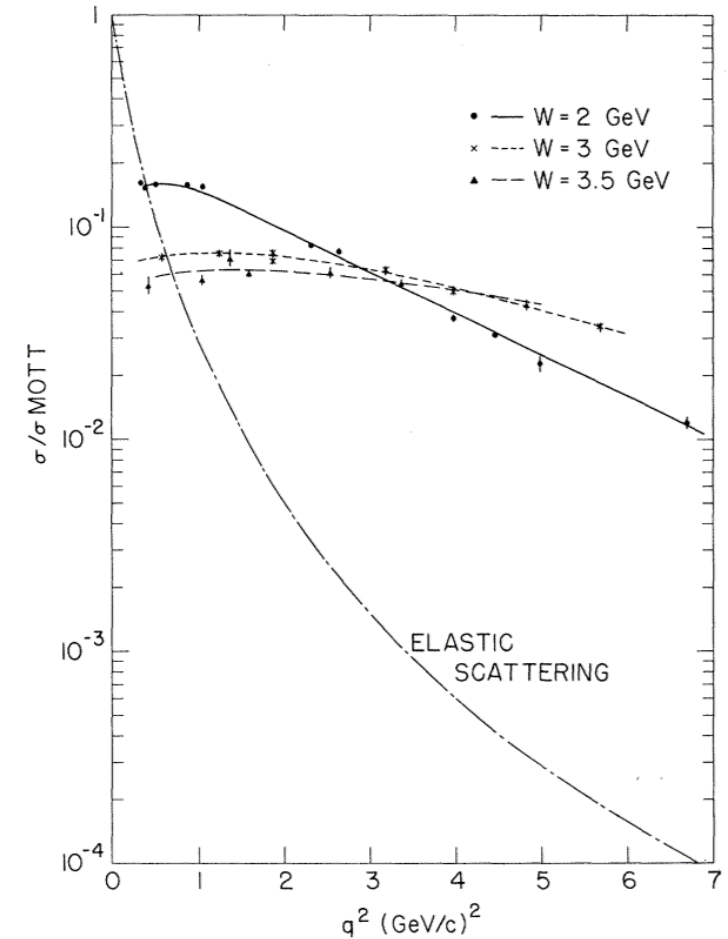
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Primi esperimenti di scattering anelastico, SLAC-MIT (1967)

$$e + p \rightarrow e + Altro$$

$E = 20 \text{ GeV}$ (10^{10} volte luce ordinaria, $\lambda = hc/E$)



Gli esperimenti a SLAC

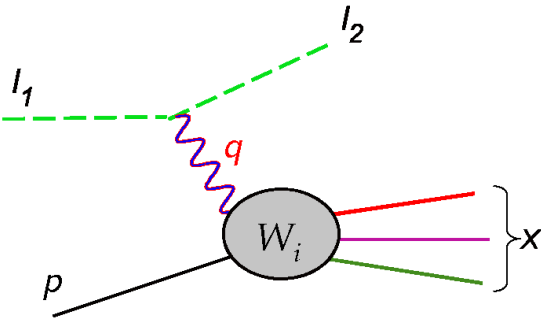
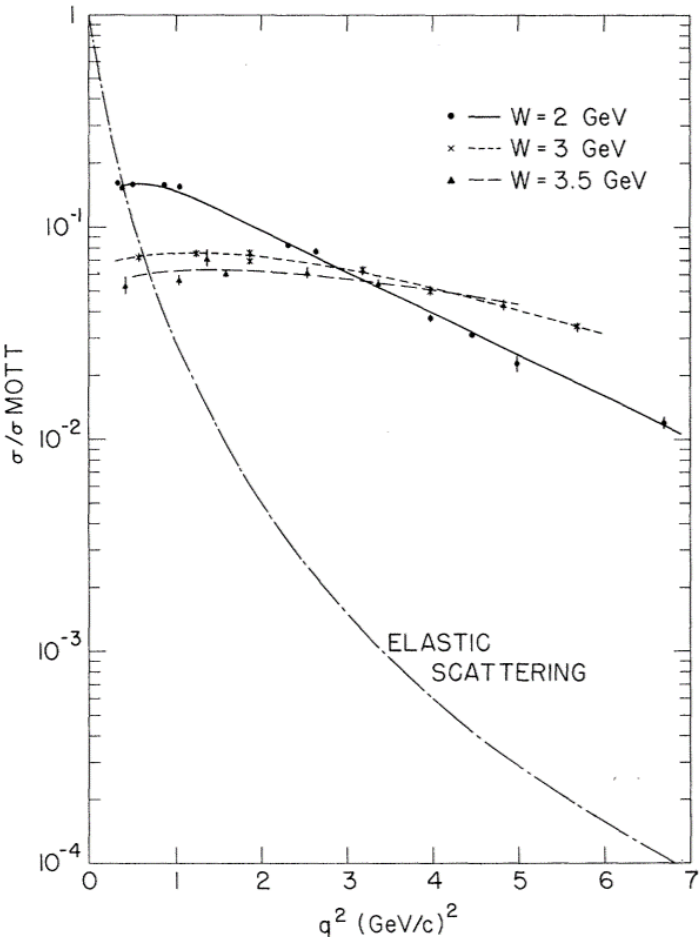
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Q [GeV]	λ [fm]	bersaglio
0.02	10	Nuclei
0.1	2	
0.2	1	Nucleoni
>1	< 0.2	Strutture più interne



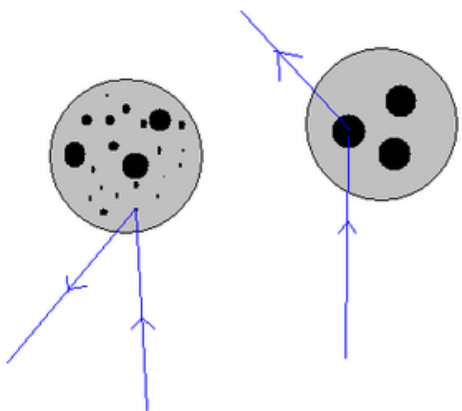
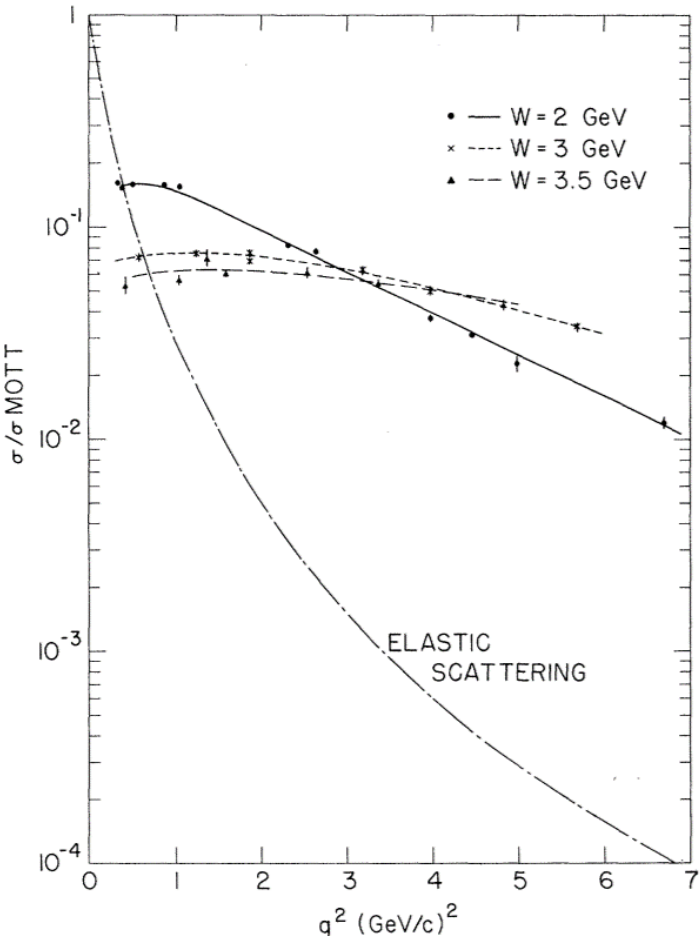
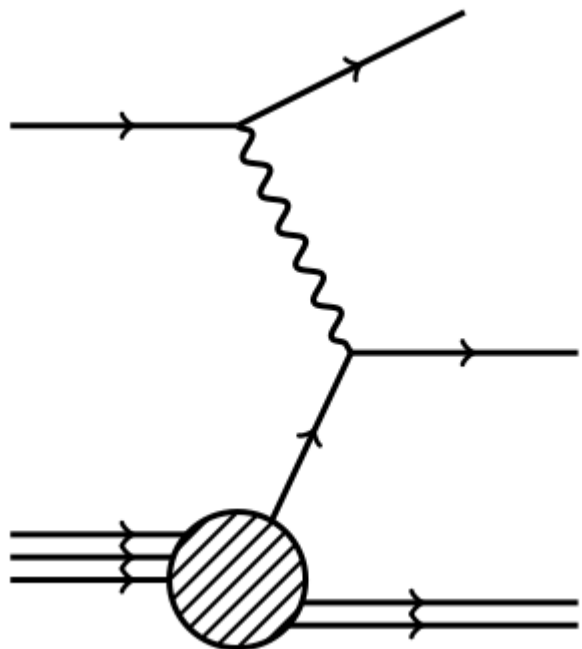
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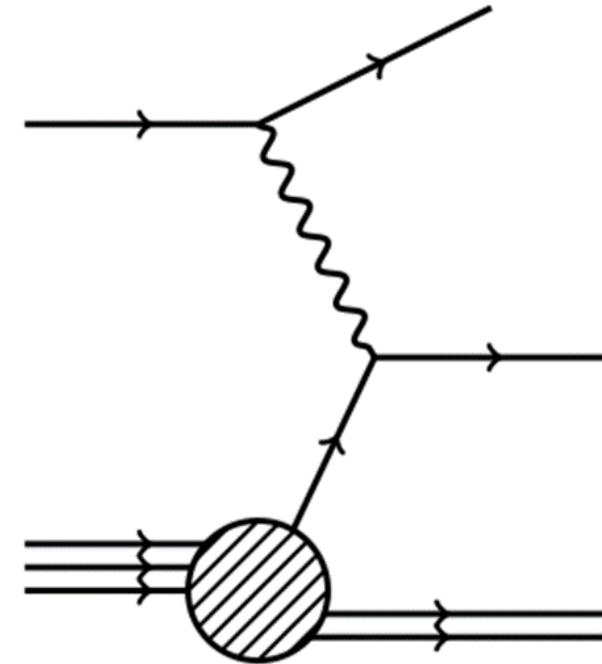
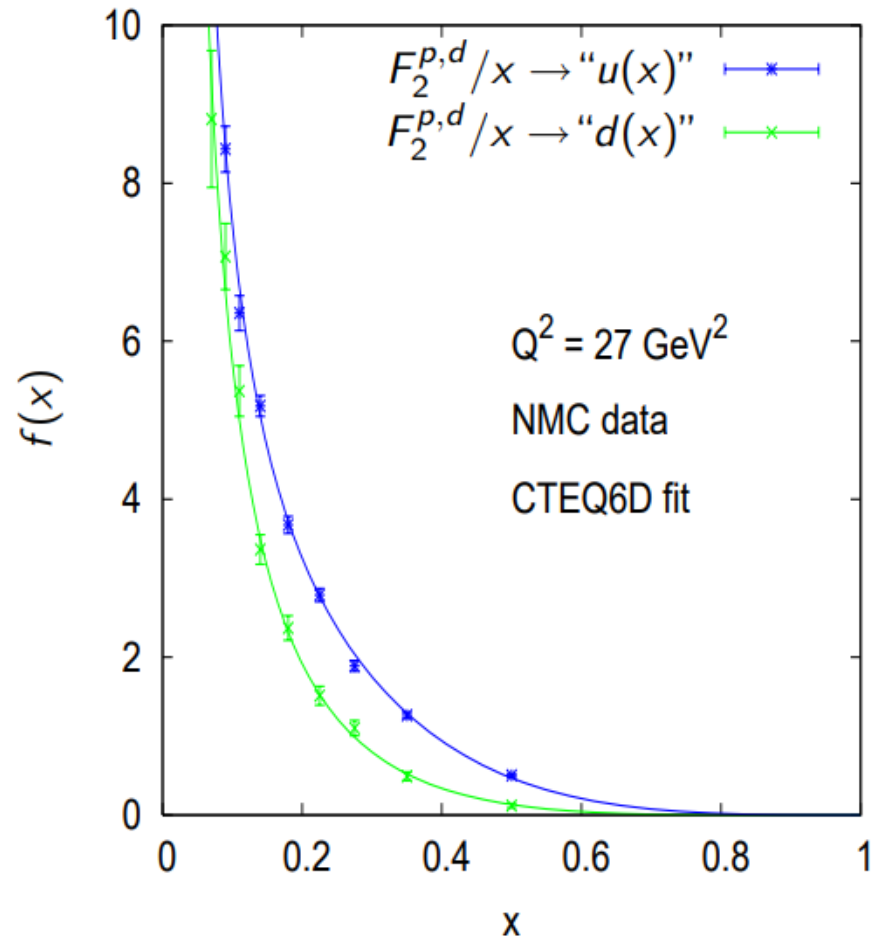
Bjorken, 1968. Scaling,

Feynman, 1969. Partoni



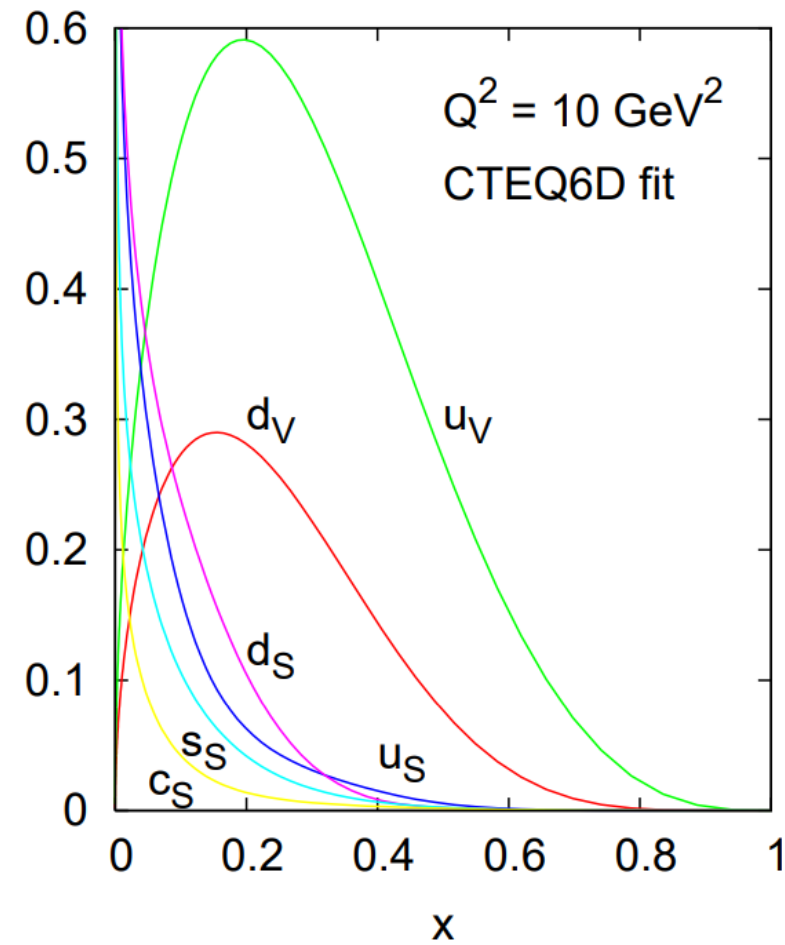
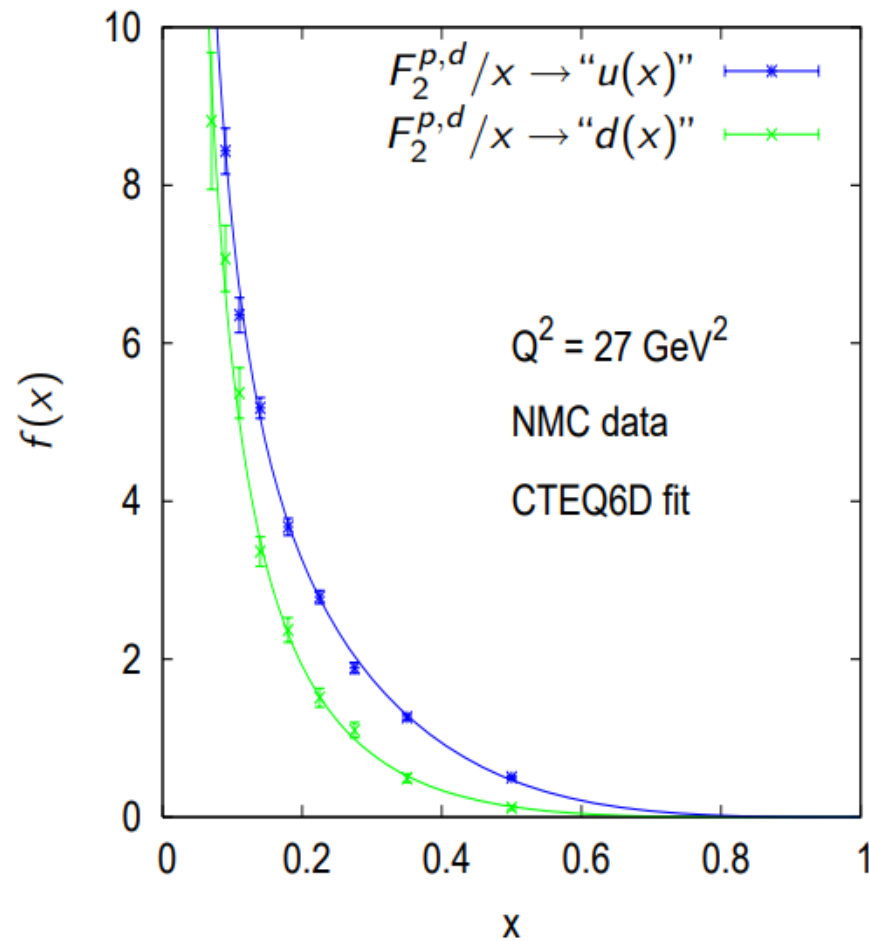
Partoni

$$\sigma(k) \sim \sum_i \int dx f_i(x) \sigma_{el}(xk)$$



Partoni

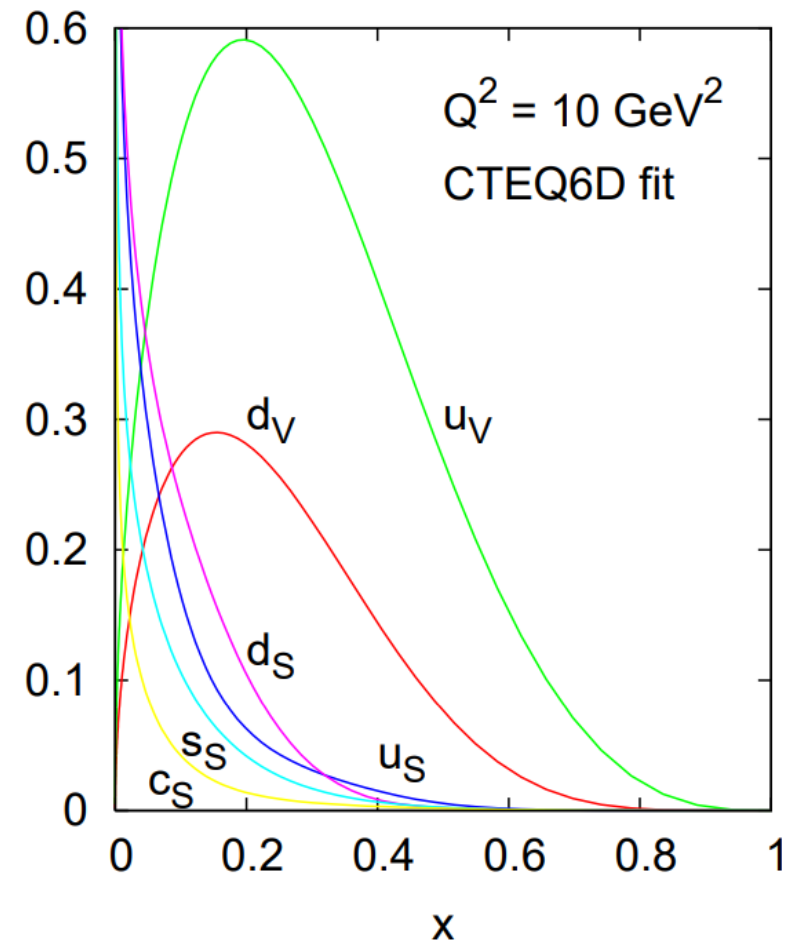
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Partoni

$$\sigma(k) \sim \sum_i \int dx f_i(x) \sigma_{el}(xk)$$

$$\sum_i \int dx x f_i(x) = 1 \quad ?$$

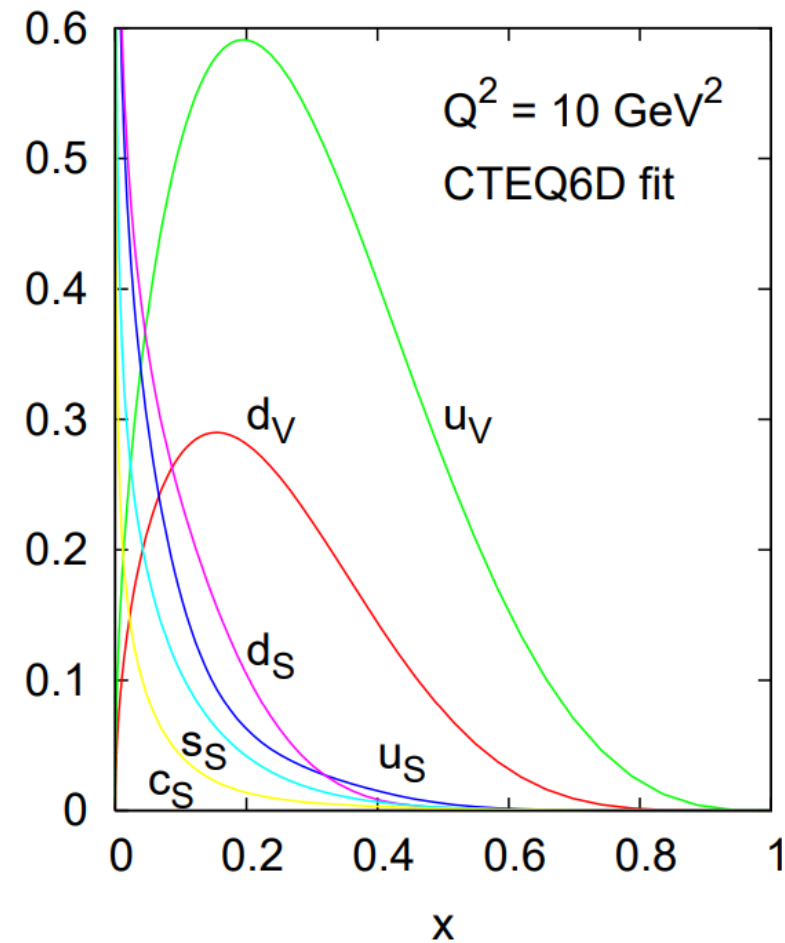


Partoni

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q_i	momentum
d_V	0.11
u_V	0.26
d_S	0.06
u_S	0.05
s_S	0.03
c_S	0.01
total	0.54

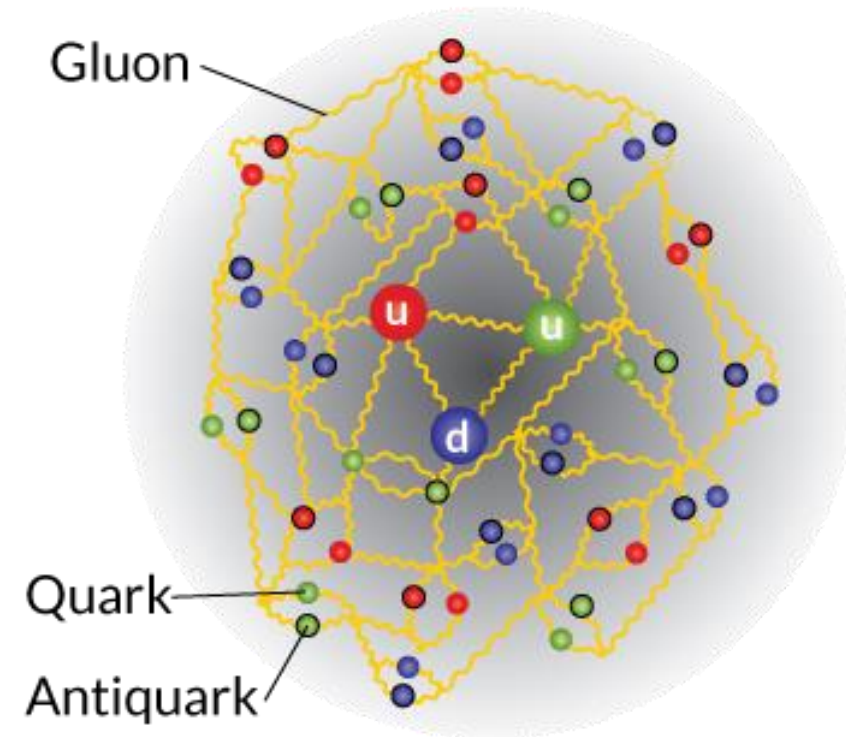


Partoni

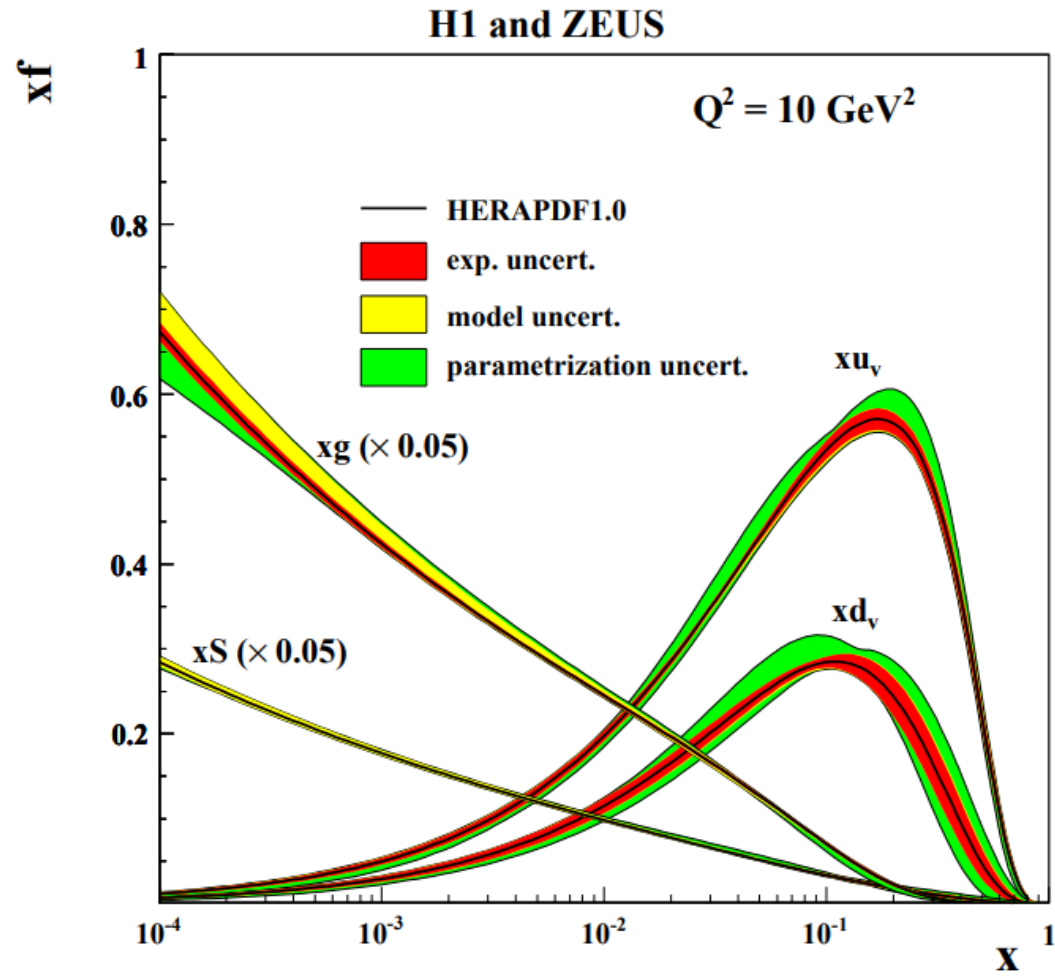
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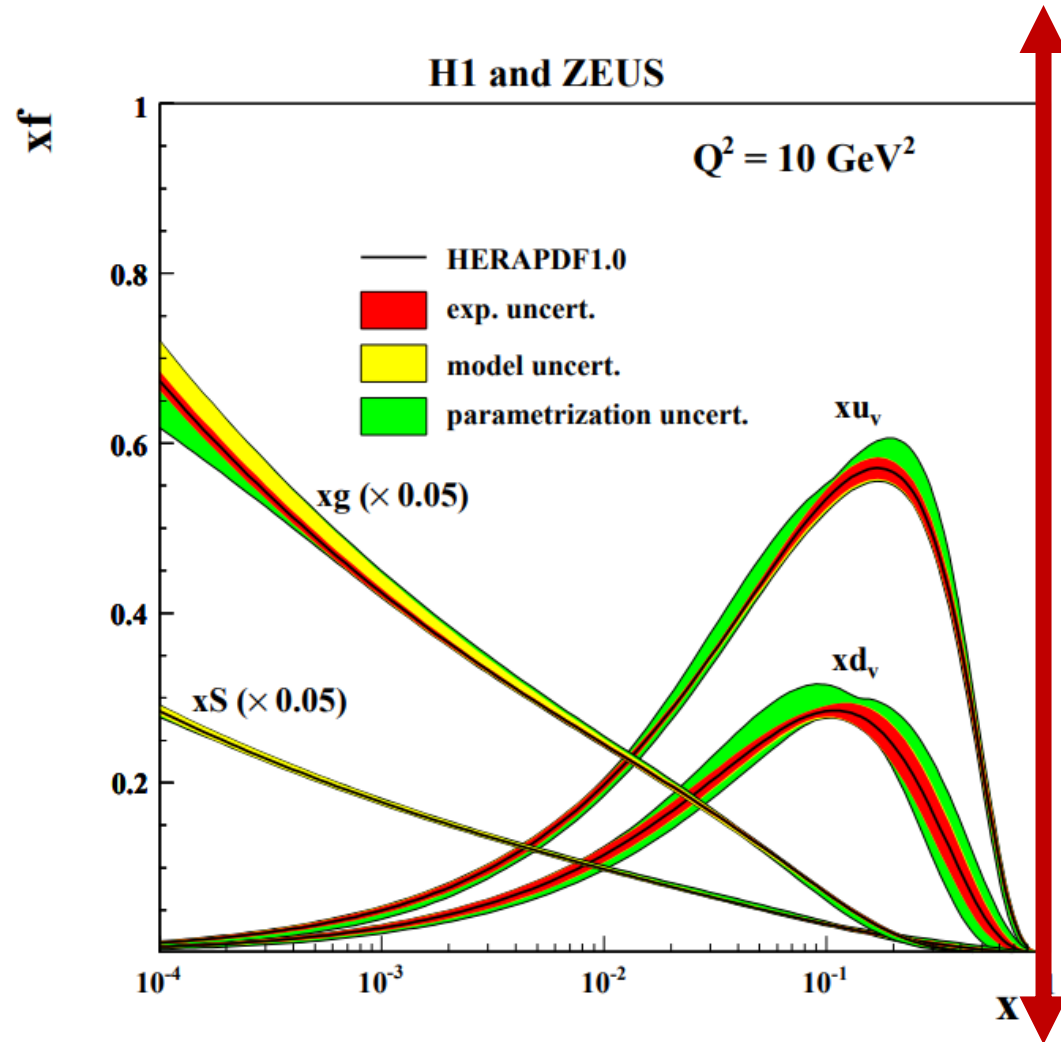
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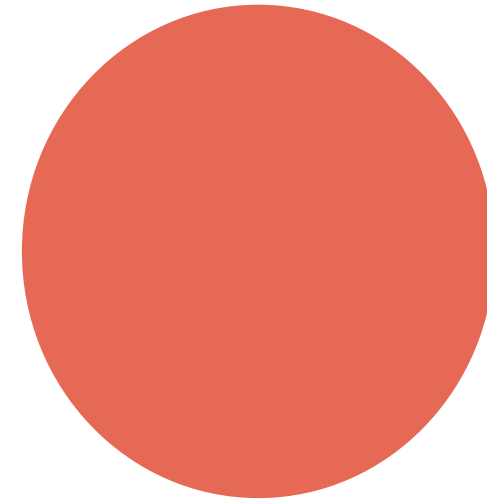
Partoni



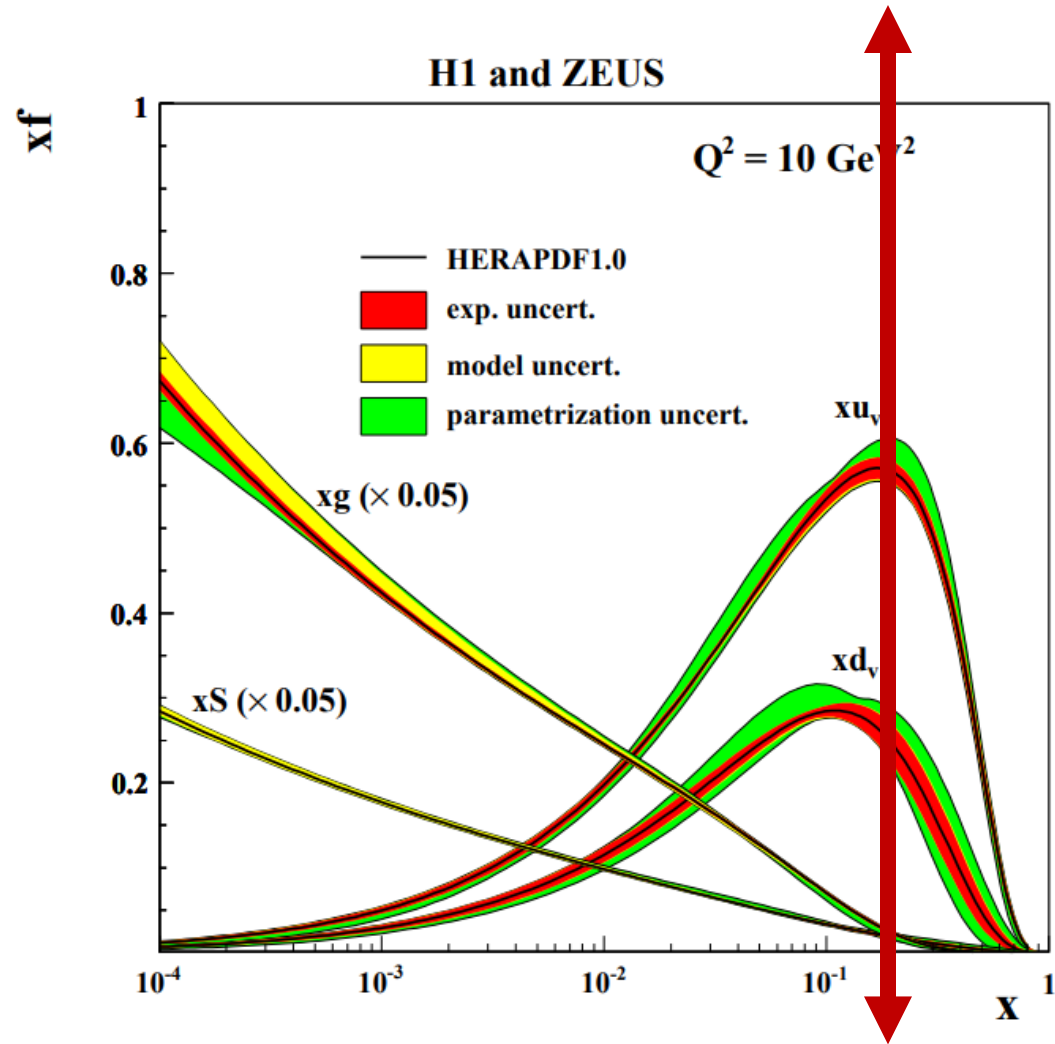
Partoni



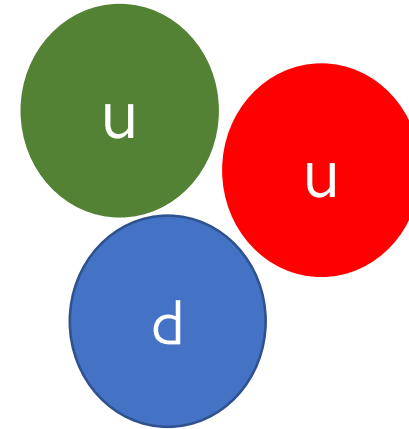
Rutherford



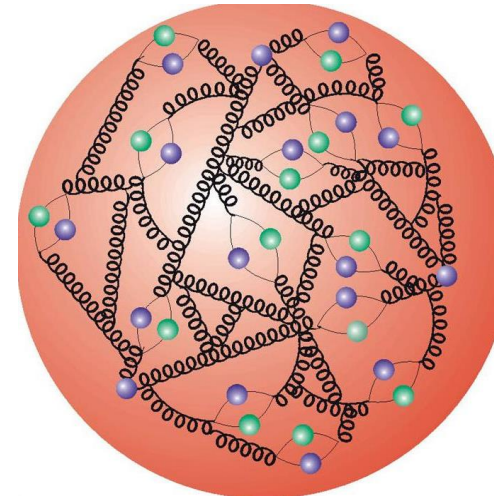
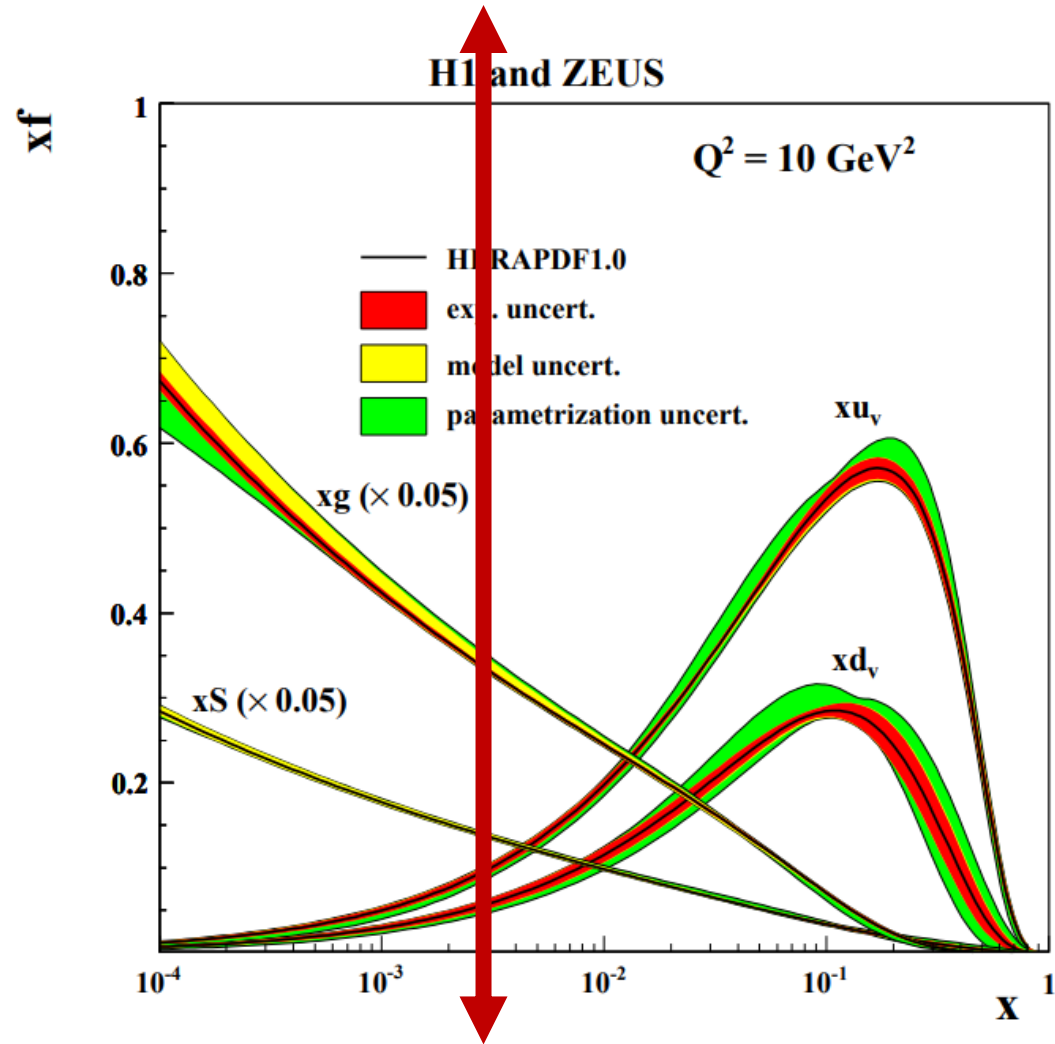
Partoni



SLAC-MIT



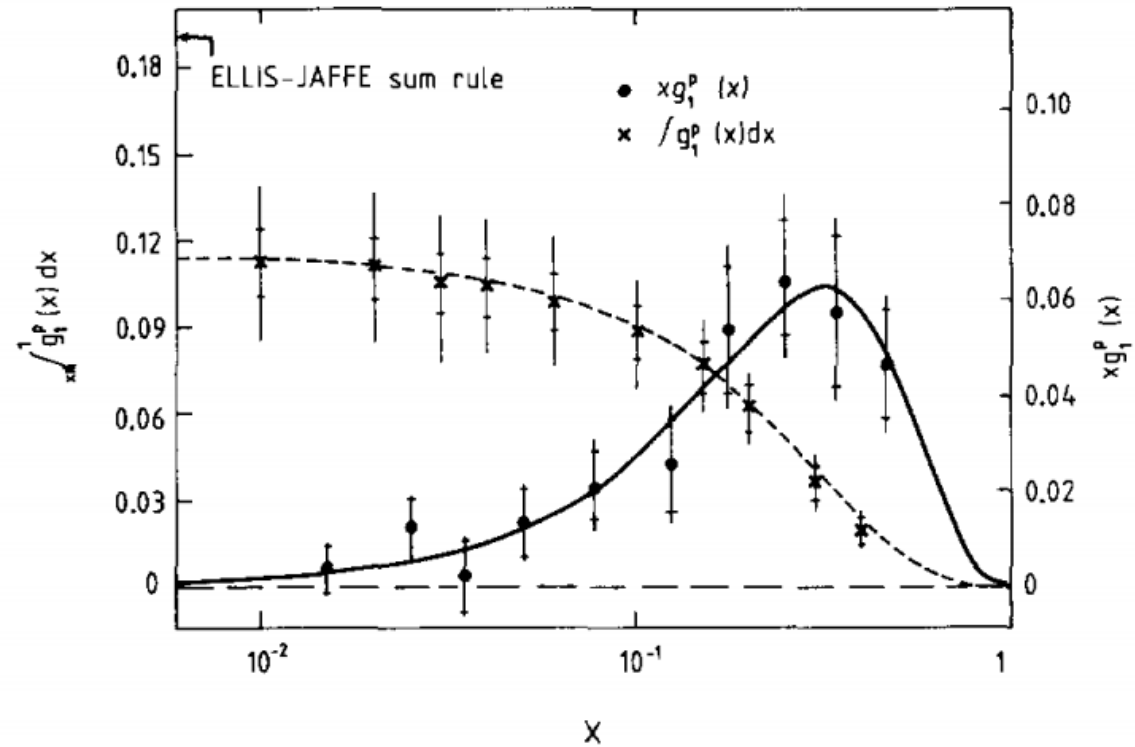
Partoni



Spin

$$\Gamma_1 = \int dx g_1(x) = 0.185 ?$$

$$\text{Spin} = \frac{1}{2} = S_q + L_q + L_{qq} + J_g$$



«This values for the integral of g_1 lead to the conclusion that the total quark spin constitutes a rather small fraction of the spin of the nucleon»

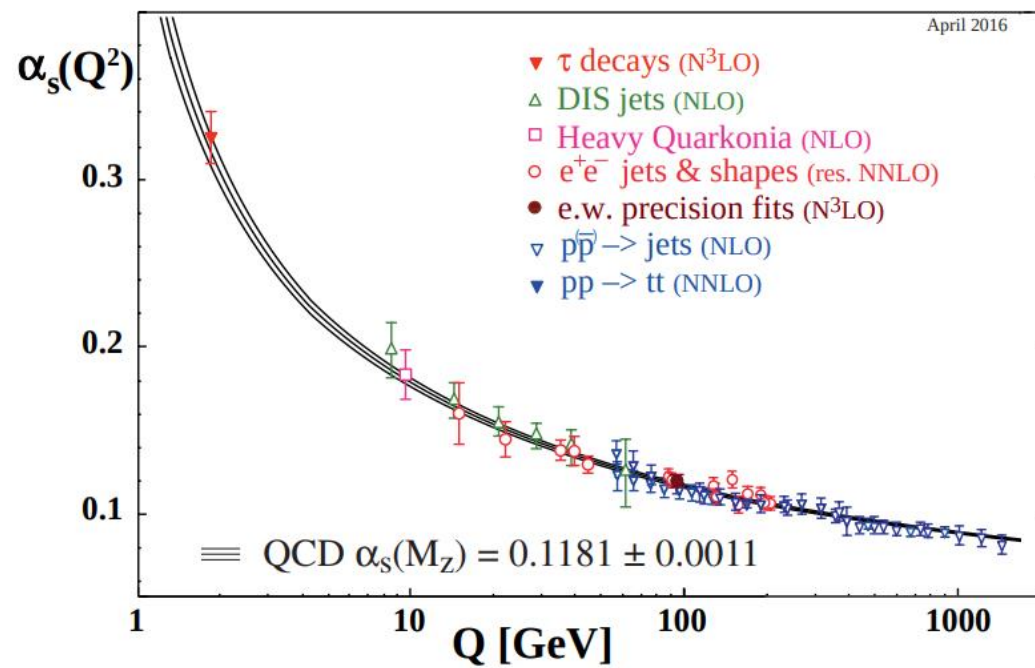
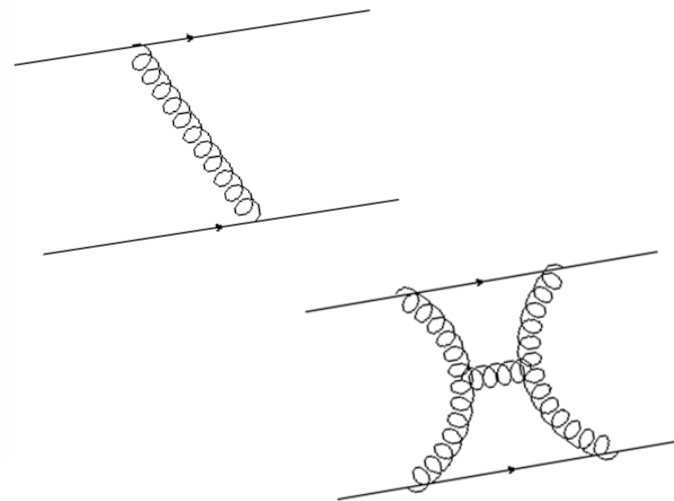
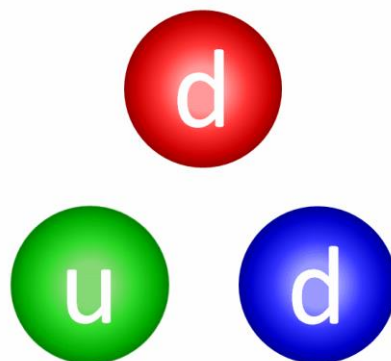
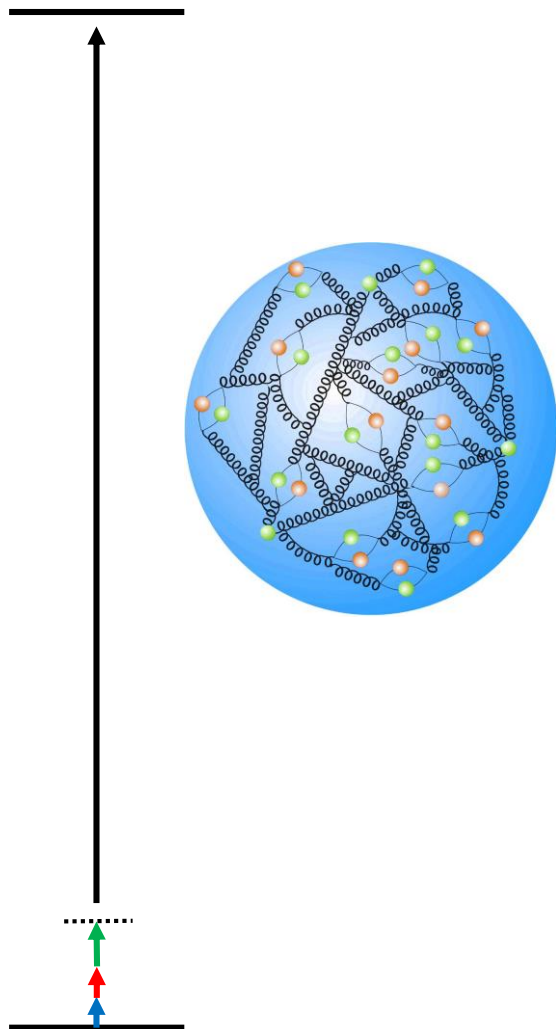
EMC collaboration, 1988

QCD

$$M_P = 938 \text{ MeV}$$

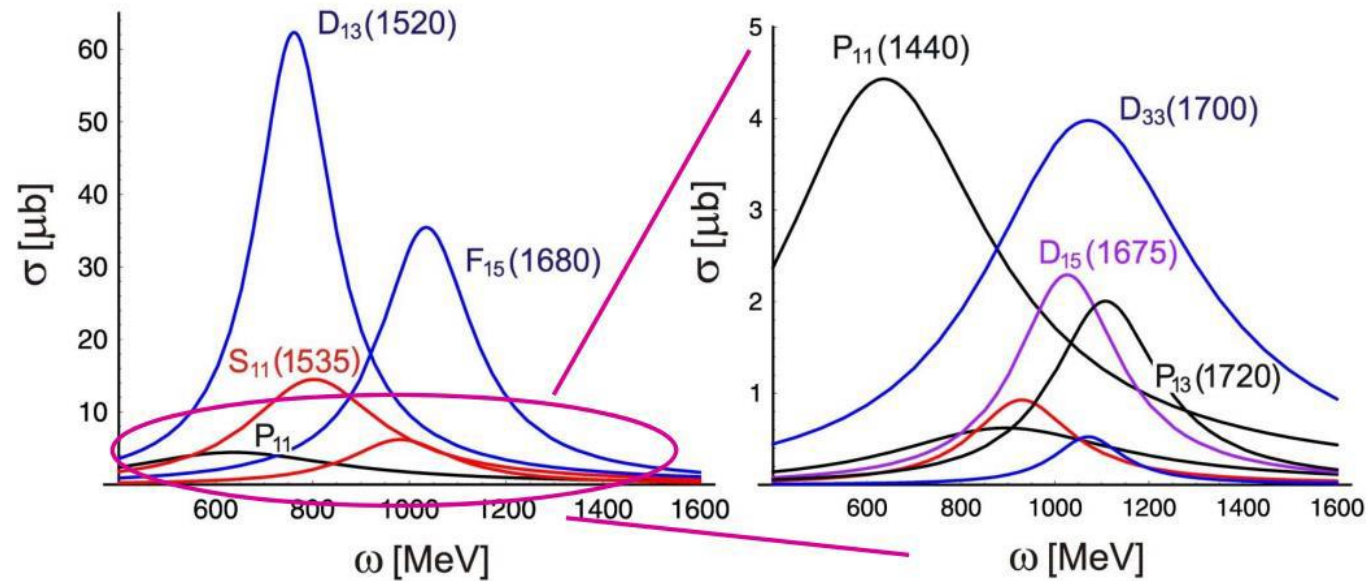
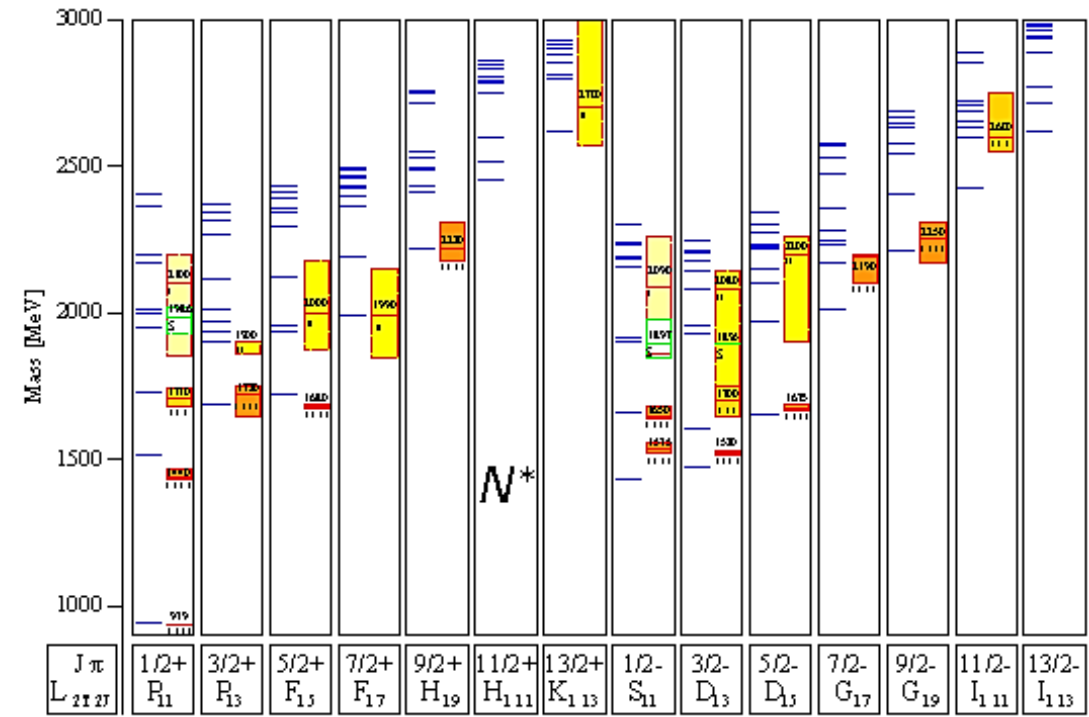
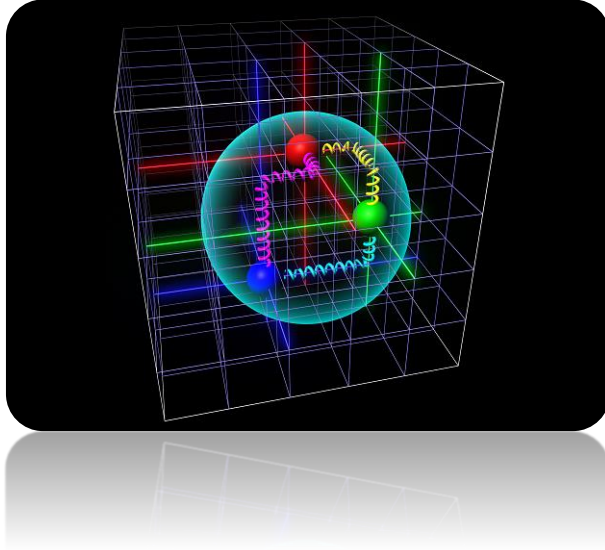
$$m_u \simeq 2 \text{ MeV}$$

$$m_d \simeq 4 \text{ MeV}$$

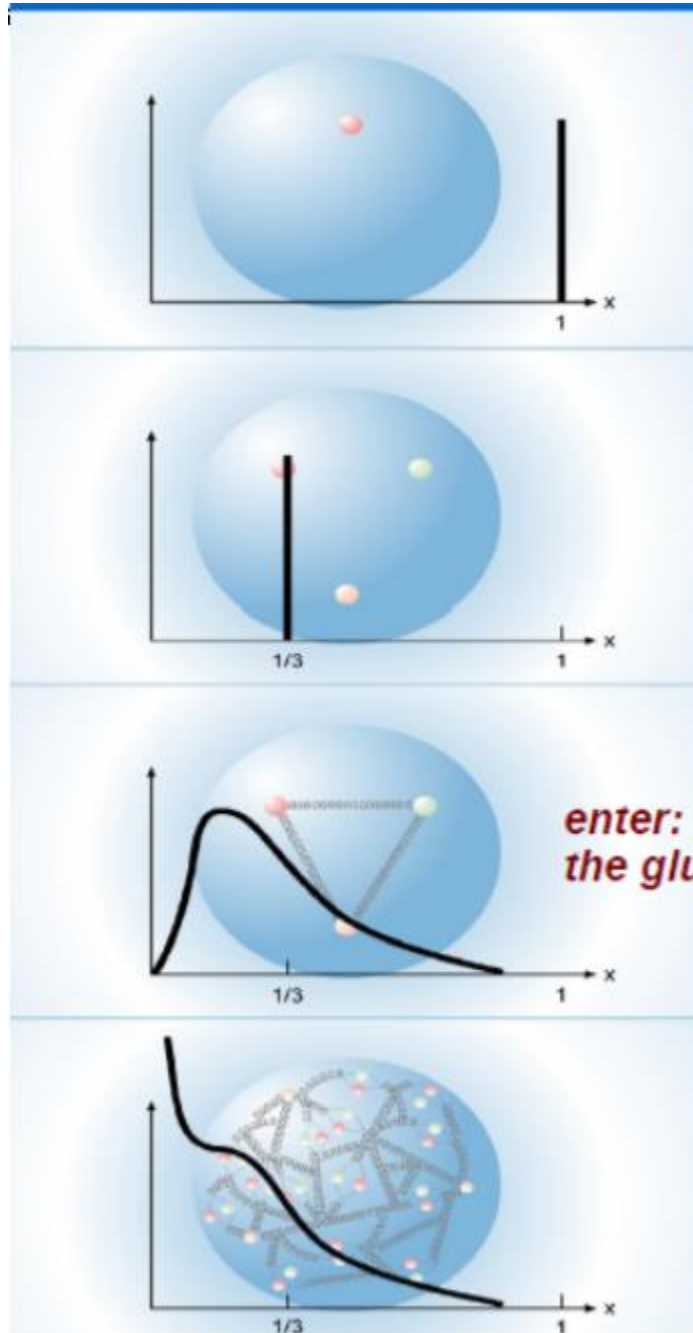


Backup

Risonanze



PROTON STRUCTURE



1 quark

proton=pointlike particle,
no structure

3 quarks

each quark carries
 $1/3$ of proton momentum
 $x=1/3$

3 bound valence quarks

3 quarks share
proton momentum

3 bound valence quarks and sea quarks

valence and seaquarks
(and gluons) share proton
momentum – very low
momentum fractions
possible

$q\bar{q}$ sea!