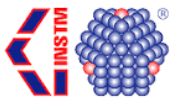




Nanomagnetismo molecolare : dalla fisica classica alla meccanica quantistica

A. Lascialfari

F. Adelnia, F. Borsa, M. Mariani, S. Sanna, L. Bordonali, T. Orlando
 D. Gerace, P. Carretta, M. Corti, M. Filibian
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 G. A. Timco, R. E. P. Winpenny, E. Mc Innes
 A. Rettori, M.G. Pini, A. Caneschi, D. Gatteschi, R. Sessoli, C. Sangregorio, L. Sorace
 M. Affronte, A. Cornia, A. Ghirri
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Univ. of Florence (Italy)

Univ. Of Bucharest (Romania)

**FIRB "Nuove sfide nel nanomagnetismo molecolare:
 dalla dinamica di spin al quantum-information processing"
 (resp. S. Carretta, UNIPR. UNIPV : D. Gerace**

Outline



Pavia, 07/06/16

- Few words on magnetic field and magnetic systems
- Nanosystems. The case of molecular nanomagnets
- “Classical” effects
- Quantum effects and applications



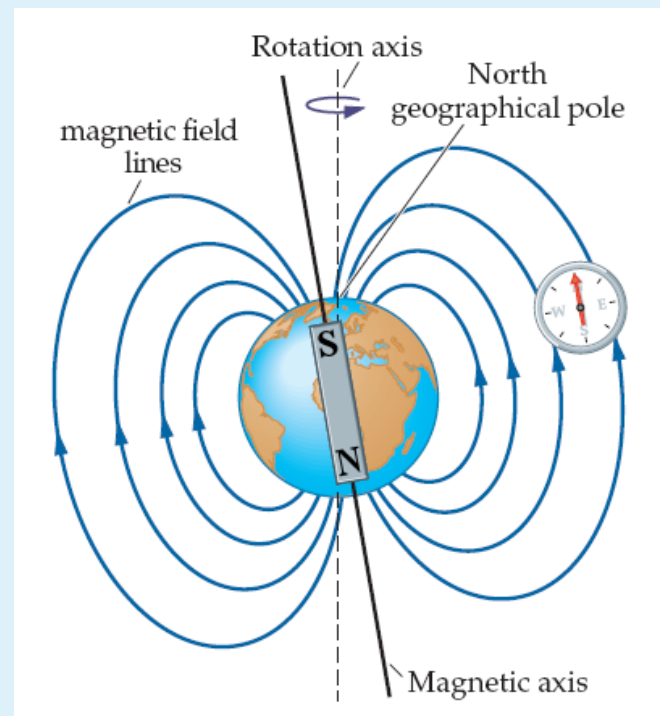
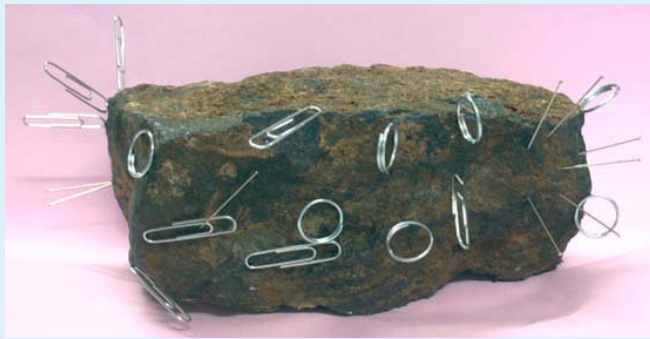
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Magnetism & magnetic field

Magnetism and magnetic field

Natural examples : rock magnetism and earth's field

Earth's magnetic field changes over time because it is generated by a geodynamo (in Earth's case, the motion of molten iron alloys in its outer core).

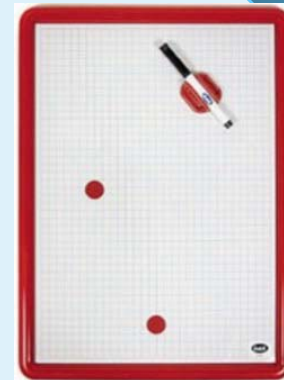
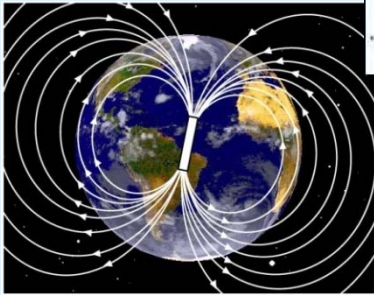


The North and South magnetic poles wander widely over geological time scales, but sufficiently slowly for ordinary compasses to remain useful for navigation. However, at irregular intervals averaging several hundred thousand years, the Earth's field reverses and the North and South Magnetic Poles relatively abruptly switch places. These reversals of the geomagnetic poles leave a record in rocks that are of value to paleomagnetists in calculating geomagnetic fields in the past. Such information in turn is helpful in studying the motions of continents and ocean floors in the process of plate tectonics.

$$B_{\text{earth}} = 0.25 - 0.65 \text{ Gauss}$$

Il campo magnetico

- Esiste sempre UNA “sorgente” di campo magnetico. Tipico esempio : la calamita
- **Sorgenti** di campo magnetico **di interesse** : elettromagneti , magneti superconduttori, magneti in genere
- E' **all'origine della forza magnetica (e/o viceversa)** fra due o più oggetti
- Ad oggi esistono molti esempi quotidiani di utilizzo del campo magnetico



Levitazione diamagnetica della rana in alti campi magnetici (10 Tesla ; il campo terrestre è 0.00005 Tesla)



Il “più grande”
magnete del mondo
(CERN)

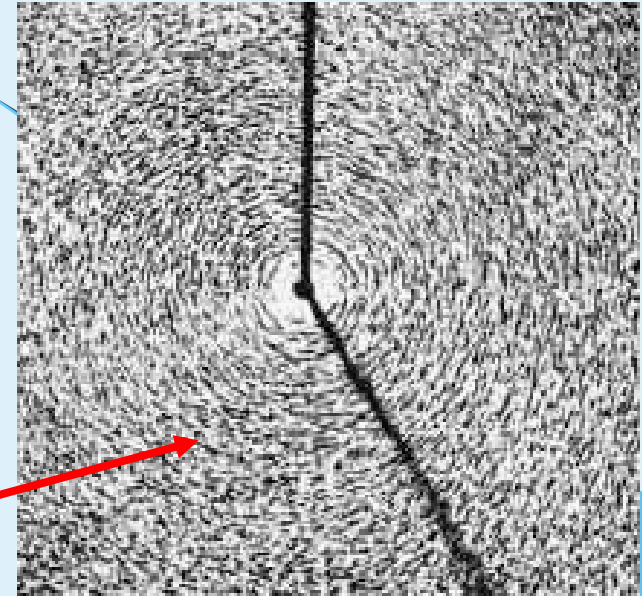
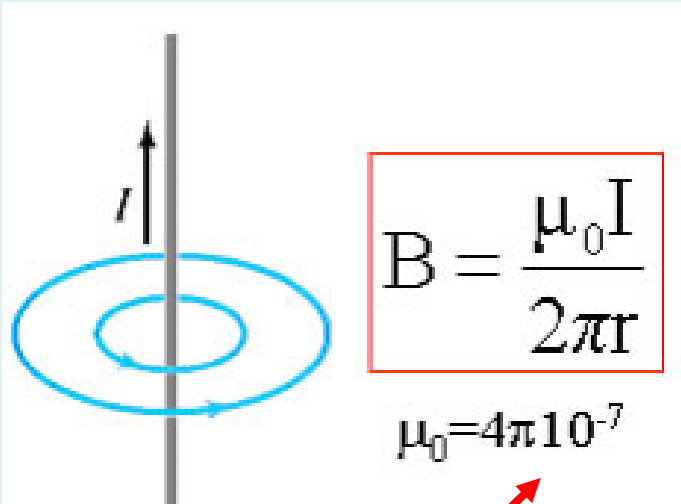


Levitazione dovuta a
superconduttori
ad alta temperatura critica



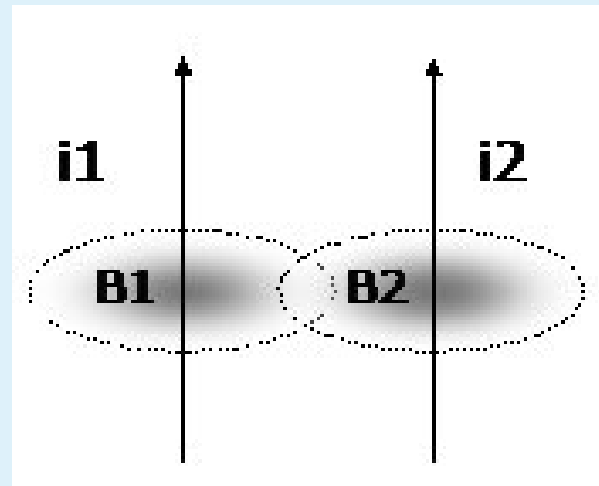
Treno a
levitazione
magnetica

Il campo magnetico dovuto a cariche elettriche circolanti



Filo elettrico percorso da corrente : legge di Biot-Savart

Fra due fili percorsi da corrente : forza magnetica

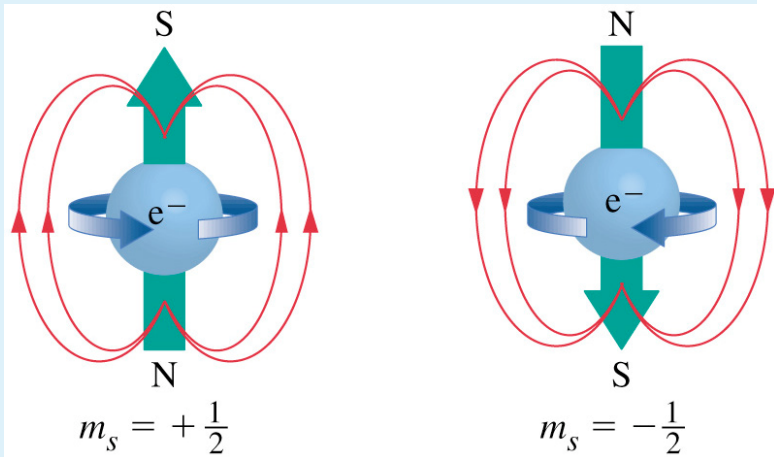


La limatura di ferro fornisce la direzione del campo magnetico generato dalla corrente che percorre il filo (vista dall'alto)

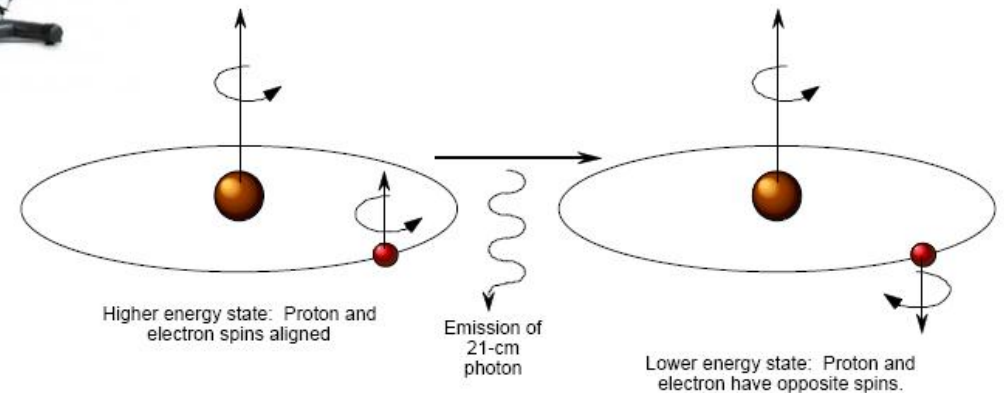
Il campo magnetico dovuto a cariche elettriche che ruotano su se stesse

Origine del campo magnetico : particelle aventi carica elettrica in moto

Altro tipo di moto di carica che genera un campo magnetico :
rotazione di una carica elettrica intorno a un asse



Formation of the 21-cm Line of Neutral Hydrogen



Rotazione (spinning) dell'elettrone
su se stesso : piccola calamita !!

Rotazione dell'elettrone
e del nucleo su se stessi

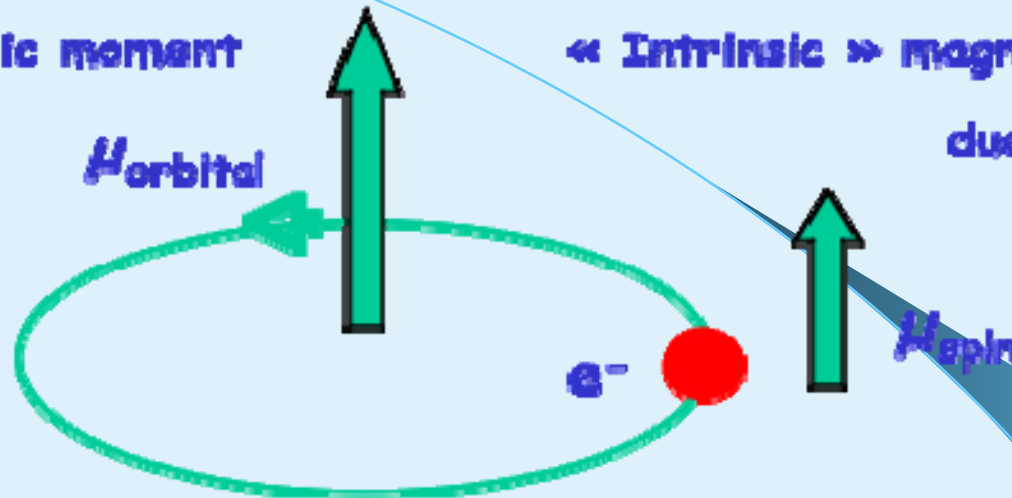
Magnetism in materials has atomic origin !!

« Orbital » magnetic moment

« Intrinsic » magnetic moment

due to the spin

$$s = \pm 1/2$$



$$\mu_{\text{orbital}} = g_l \times \mu_B \times l$$

$$\mu_{\text{spin}} = g_s \times \mu_B \times s \approx \mu_B$$

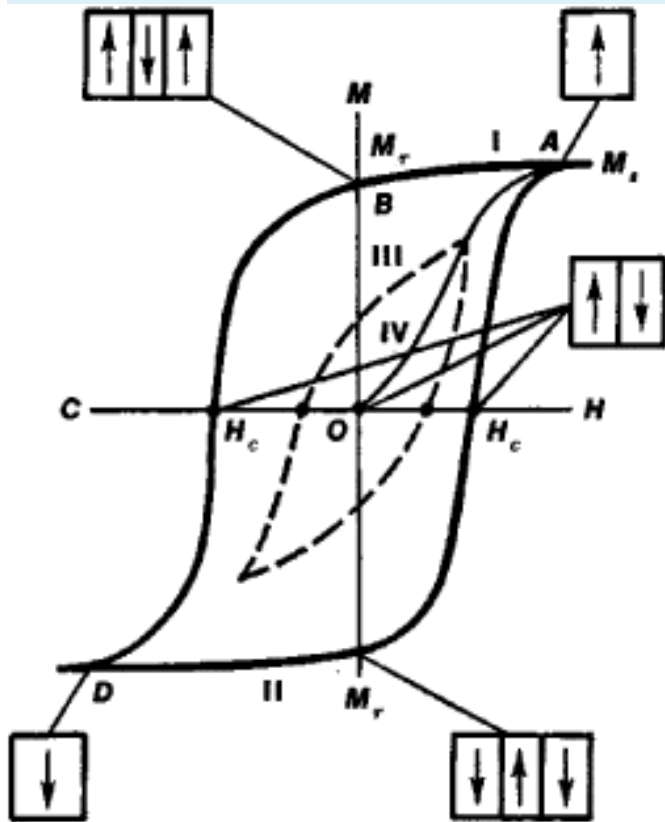
$$\mu_{\text{total}} = \mu_{\text{orbital}} + \mu_{\text{spin}}$$

$$\mathbf{M} = (1/V) \sum_i \mathbf{m}_i = (1/V) \sum_i \mu_{\text{orb}} + \mu_{\text{spin}} \quad \text{Magnetization}$$

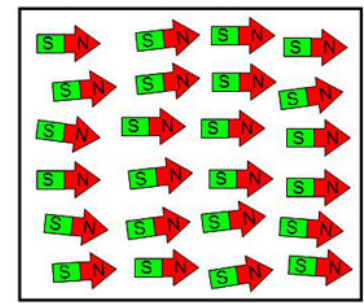
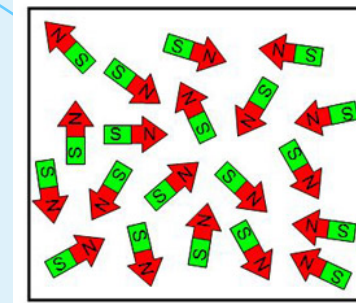
In MM, often $\mu_{\text{orb}} \sim 0 \Rightarrow$

magnetism given by μ_{spin}

"Std" magnetic systems : hysteresis and domain walls



Bulk ferromagnet



Material magnetized to saturation by alignment of domains.

Magnetization of material M

When driving magnetic field drops to zero, the ferromagnetic material retains a considerable degree of magnetization. This is useful as a magnetic memory device.

The material follows a non-linear magnetization curve when magnetized from a zero field value.

The driving magnetic field must be reversed and increased to a large value to drive the magnetization to zero again.

Applied magnetic field intensity H

Toward saturation in the opposite direction

The hysteresis loop shows the 'history dependent' nature of magnetization of a ferromagnetic material. Once the material has been driven to saturation, the magnetizing field can then be dropped to zero and the material will retain most of its magnetization (it remembers its history).



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.... toward....

"Nano" - physics

i.e.

reducing the size of
the systems to nm scale

Few examples of "nano" Magnetism applications

Information Technology



Data storage

Quantum computing



Energy

Transportation



Energy storage



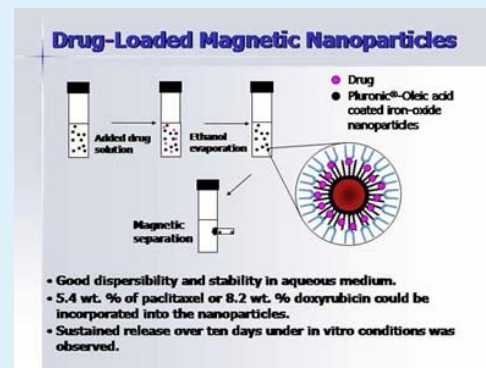
Biomedicine



Magnetic Resonance Imaging (diagnosis)

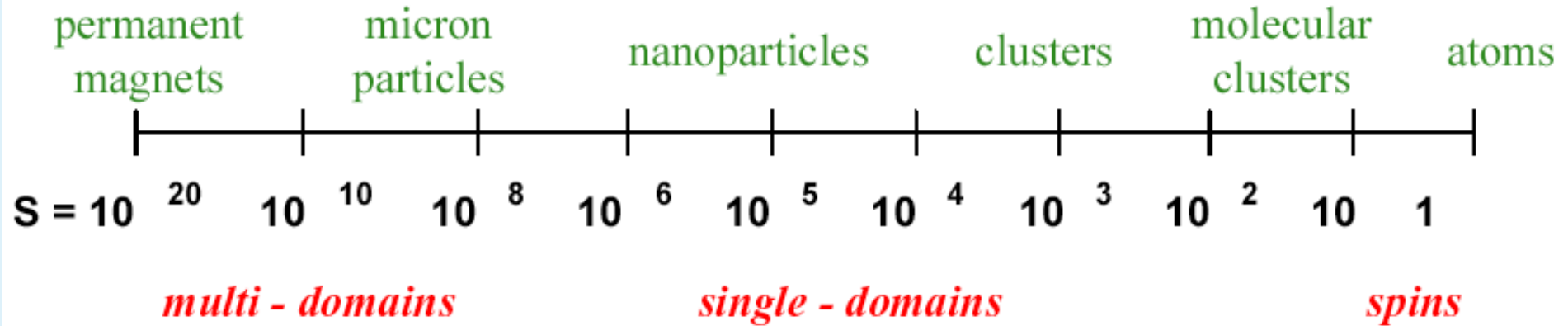
Magnetic Fluid Hyperthermia (tumour therapy)

Magnetic (drug) delivery



Magnetic structures

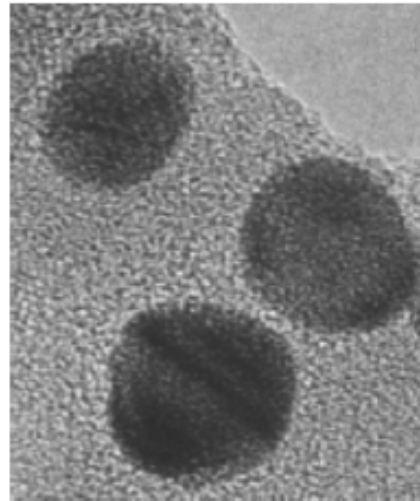
← *macroscopic* *atomic* →



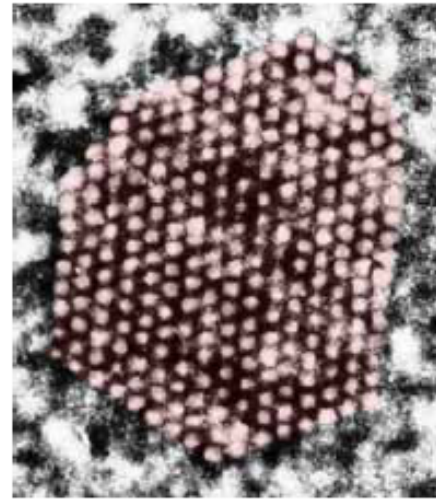
1 mm



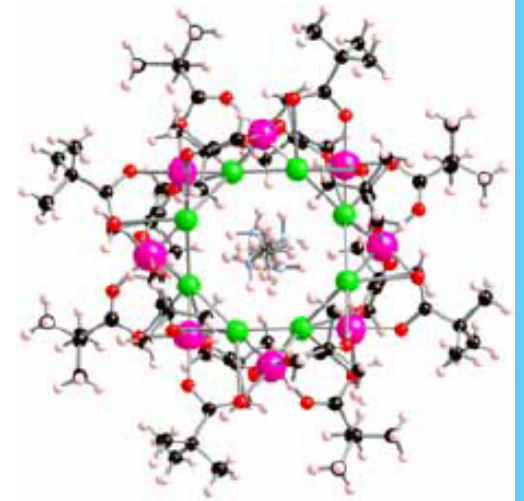
20 nm



3 nm

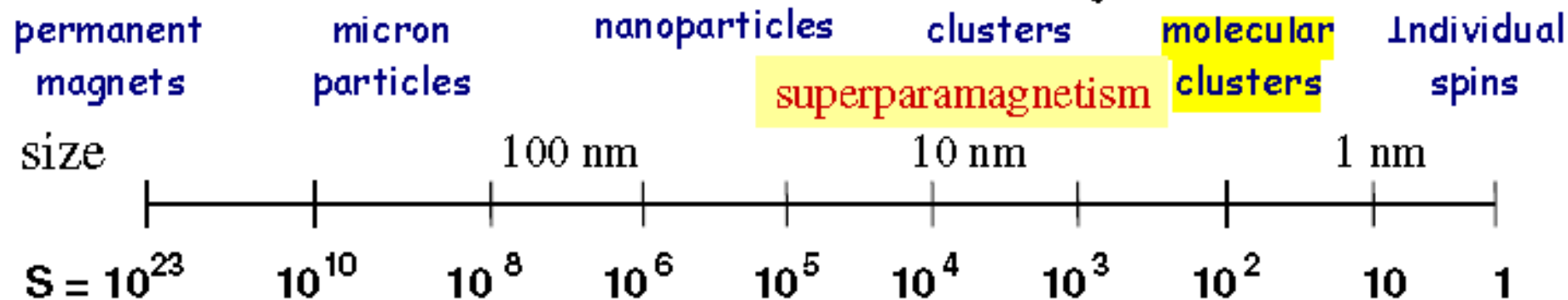


1 nm



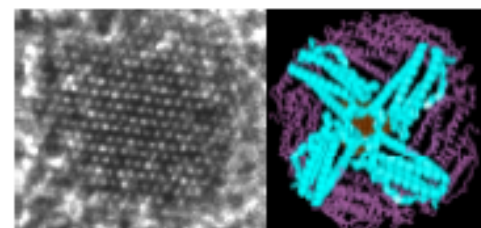
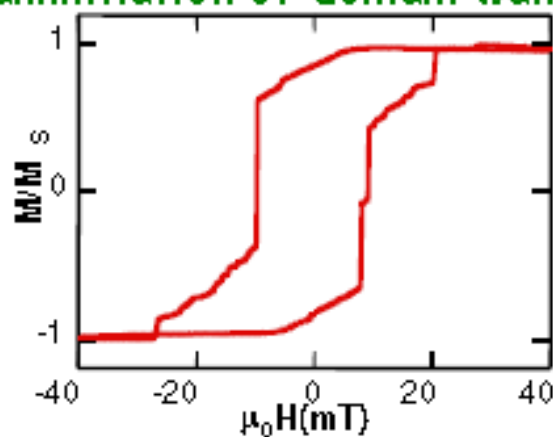
MESOSCOPIC MAGNETISM

Classical \longleftrightarrow Quantum



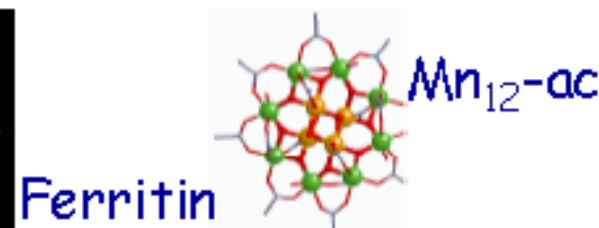
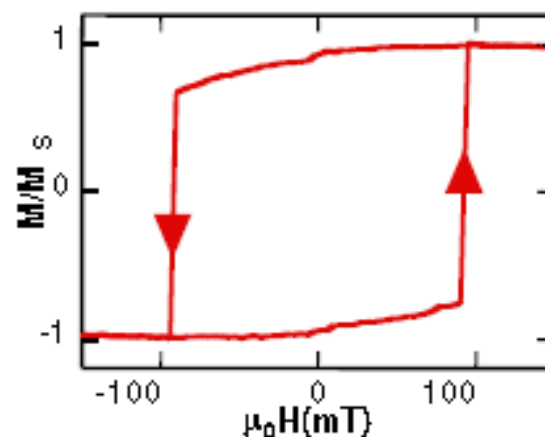
multi - domain

nucleation, propagation and annihilation of domain walls



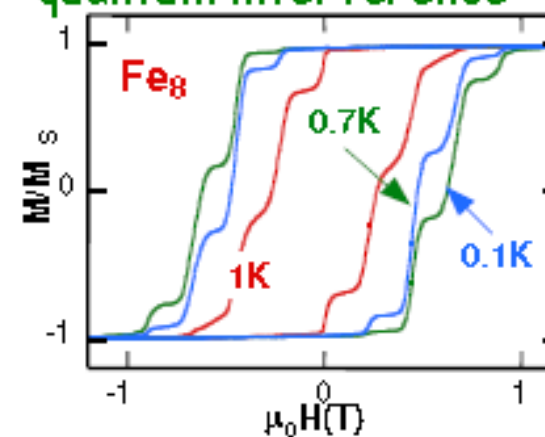
single - domain

uniform rotation



Single molecule

quantum tunneling, quantum interference





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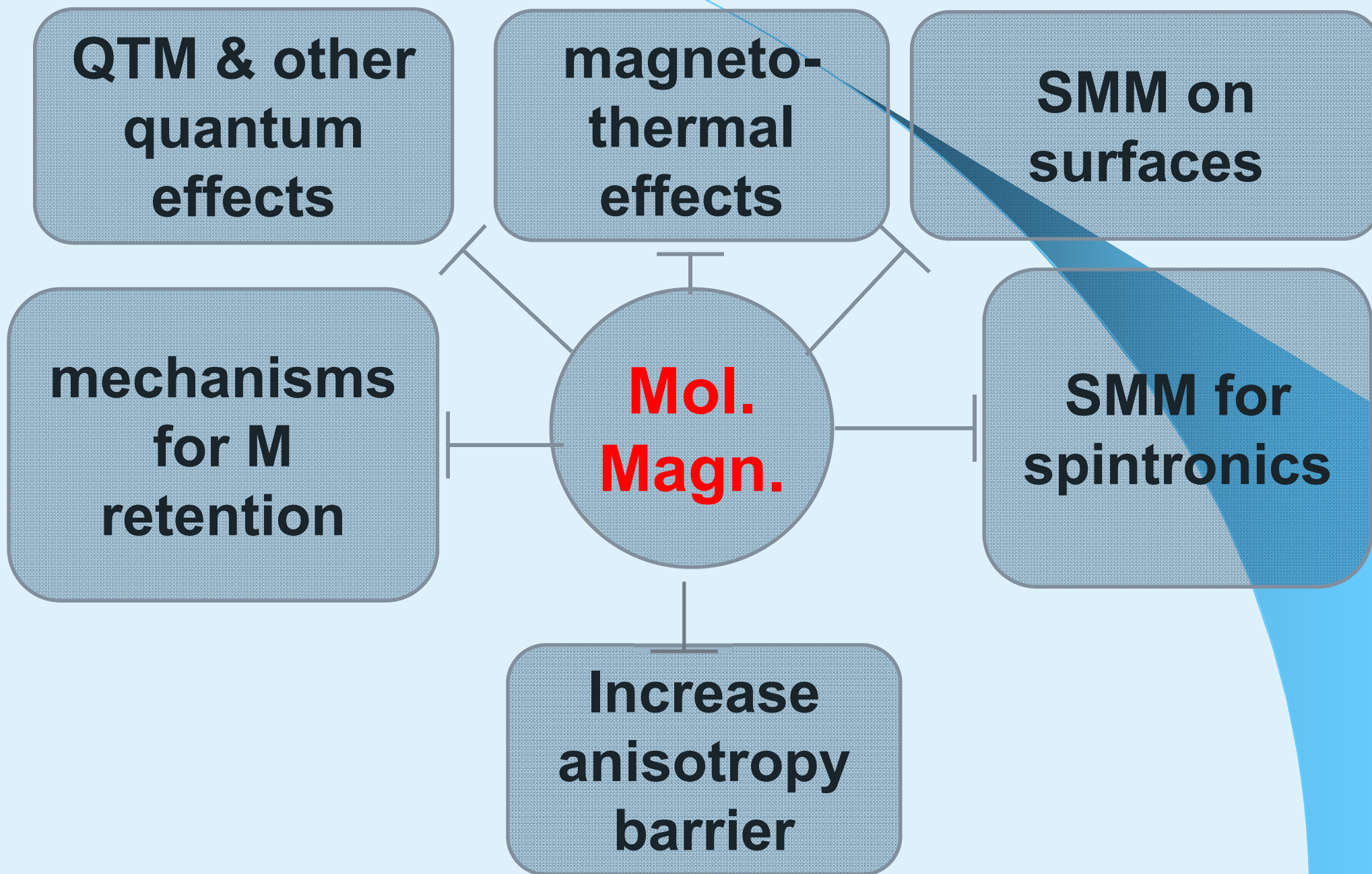
Basic dates in history of Molecular magnets or "single-molecule magnets"

- ☼ **1993** early magnetic studies on Mn₁₂
- ☼ **1996** QTM in Mn₁₂
- ☼ **1997** QTM in Fe₈
- ☼ **2000** Mn₁₂ on surface
- ☼ **2002** Agilent Technology Award to Sessoli, Gatteschi, Barbara, Wernsdorfer, Friedman
- ☼ **2004** TbPc₂ (phtalocyanines)
- ☼ **2007** Mn₆
- ☼ **2009** Fe₄ on surface
- ☼ **2015** Zavoisky award to Prof. D. Gatteschi

Related research activities



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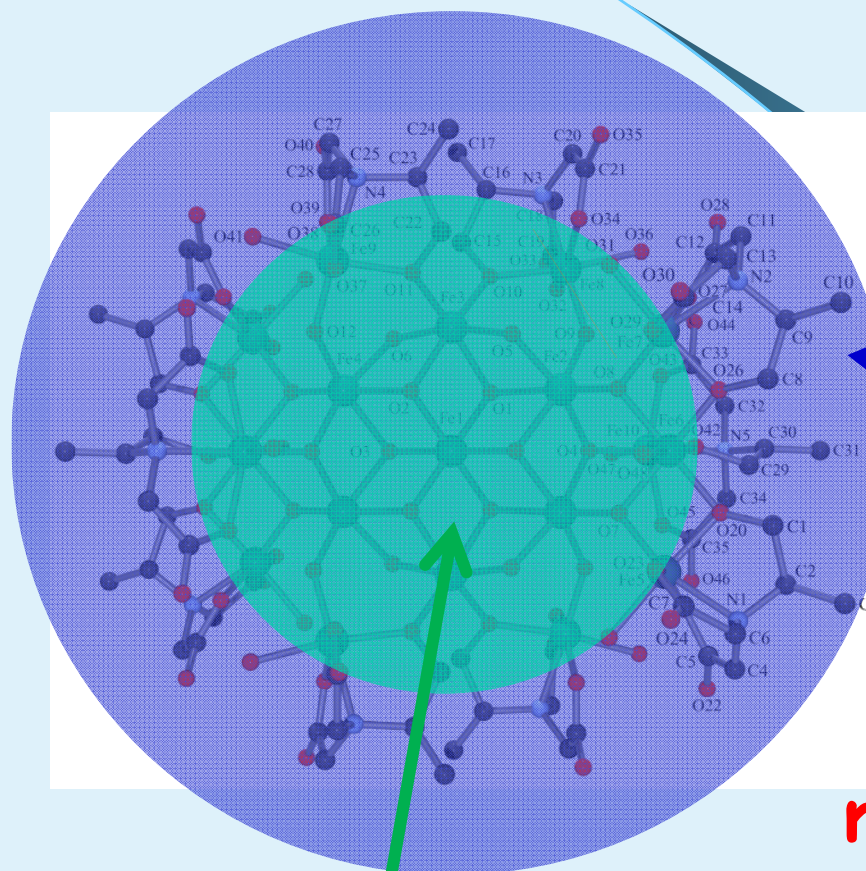
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Some applications

- Memory storage
- Magneto-thermal effects
- molecules on surfaces (read and write)
- Information Storage & Processing:
 - molecular spintronics
 - quantum computation
 - hybrid cavities

Typical Magnetic Molecule

1 nm



ligand

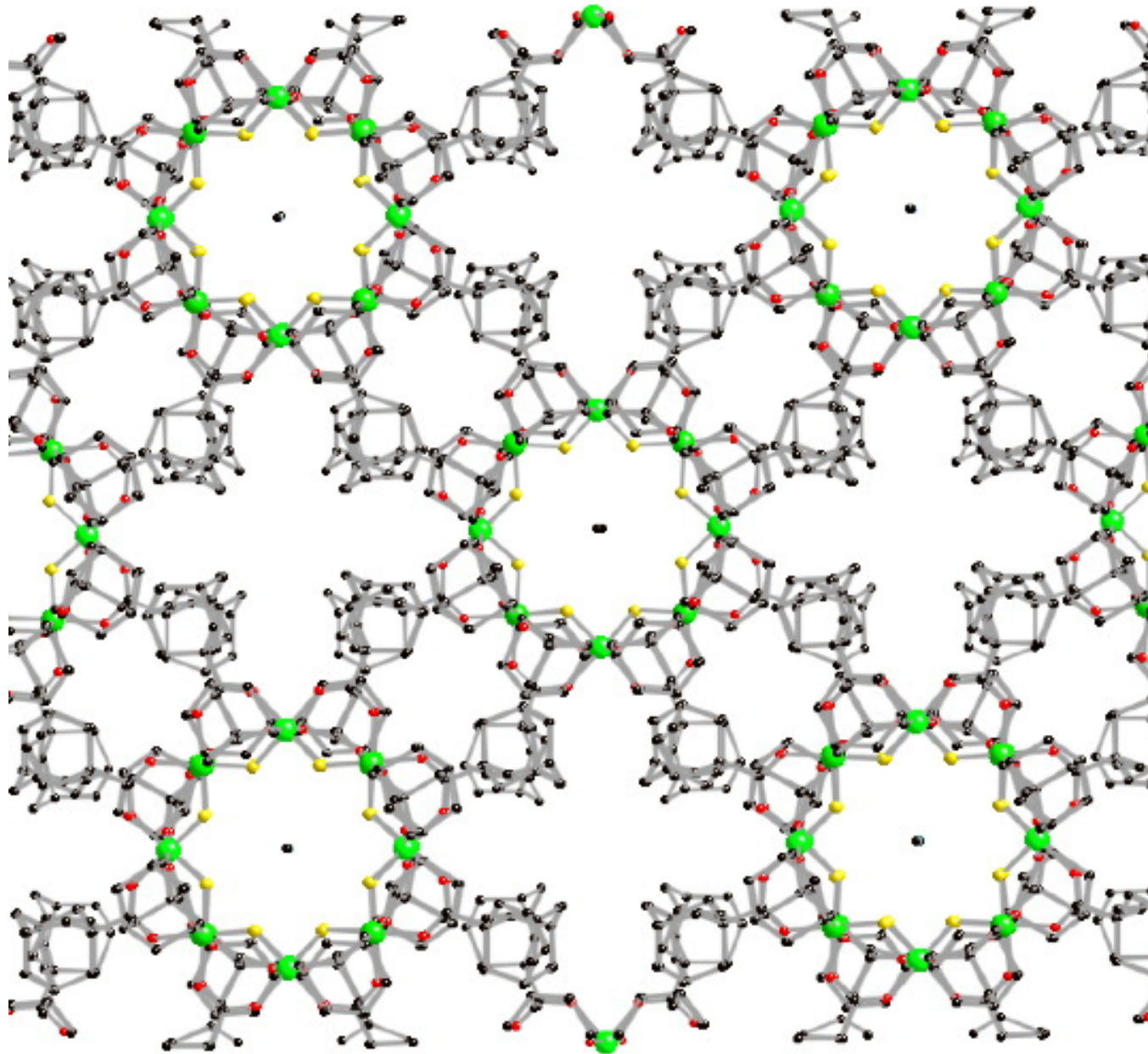
A "total"
molecular spin

magnetic core

Molecular engineering to design nanomagnets



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Cr₈

A single crystal is a collection of identical nanomagnets well separated one another and perfectly oriented

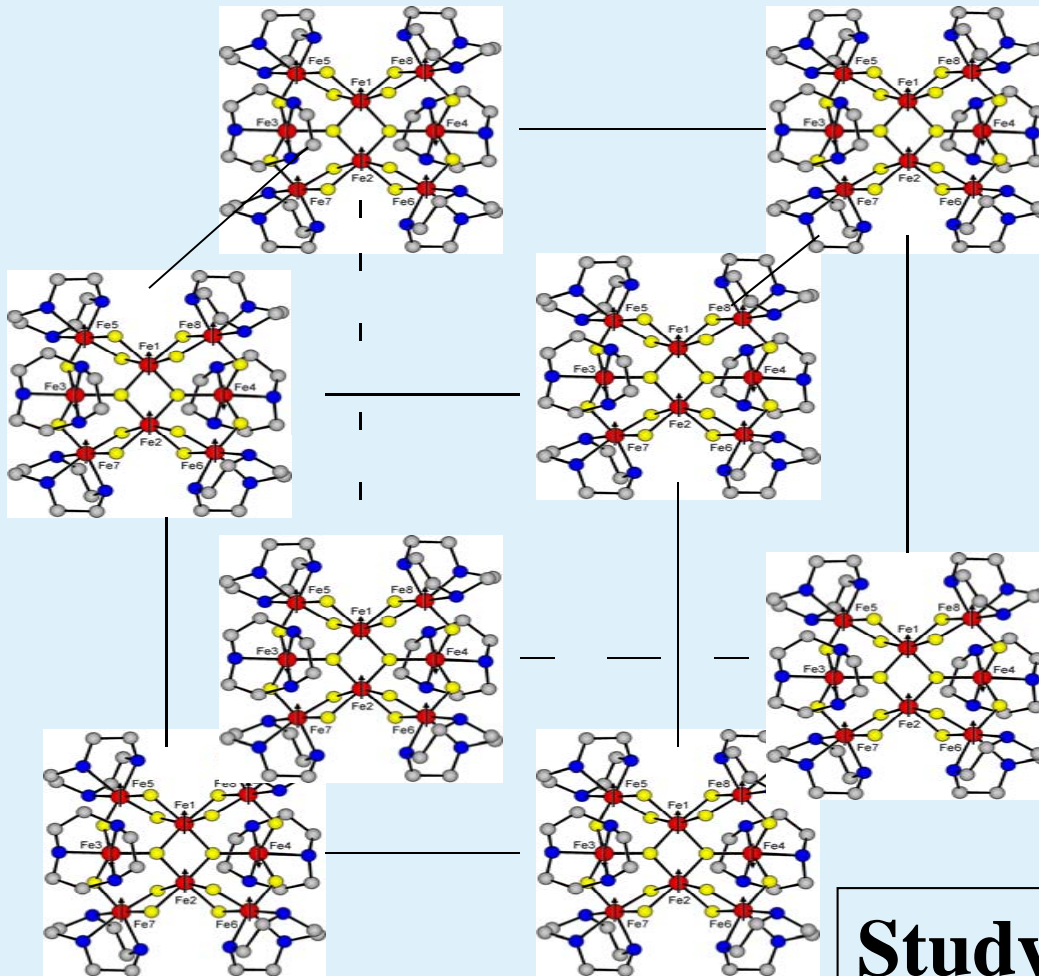
Another example of nanomagnet: crystal of Fe₈



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Few magnetic ions per molecule

Unit repeated over
all the crystal



Negligible magnetic
interactions

among molecules

i.e.

**Molecular nanomagnets
or single molecule magnets**

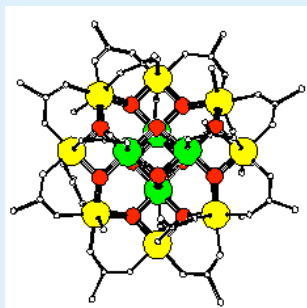
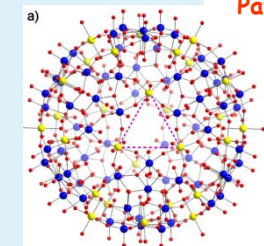
Studying the bulk \Rightarrow
Investigating the single molecule

Molecular Nanomagnets (MNM)



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Wide variety : rings (Fe₁₀, Fe₆, Cu₈, Cu₆, Cr₈.....)



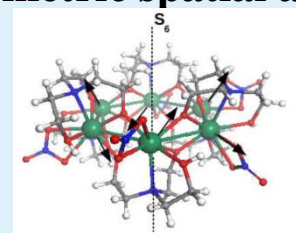
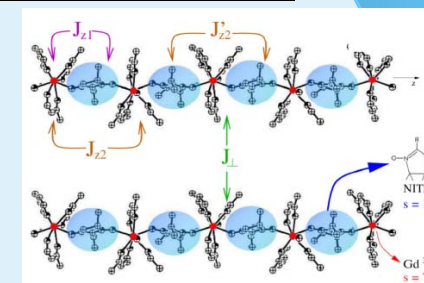
“clusters”, Single Molecule Magnets (Mn₁₂, Fe₈, Ni₁₀, Cr₄, Fe₄...)
chains , Single Chain Magnets (CoPhOMe, Dy-Ph, Gd-R,)

• Crystals made up of very weakly interacting molecules

⇒ magnetic properties determined by single molecule

• Clusters and rings can be designed at will :

- number of interacting magnetic ions (spins) ÷ geometric spatial arrangement of the ions
- single ion spin dimension ($s=1/2$ $s=5/2$)
- exchange interaction J (AF, FM)





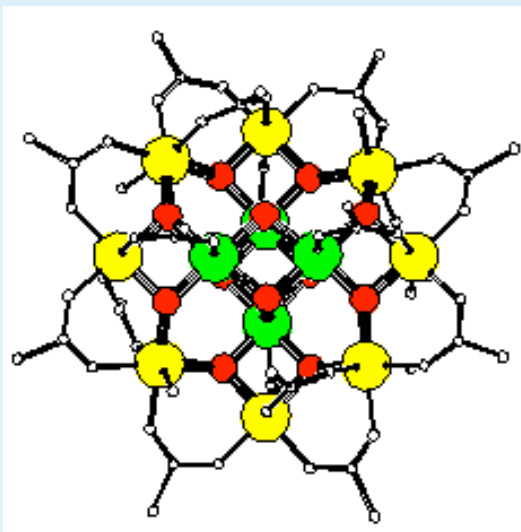
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Example: High-spin Molecular magnets

Some high spin nanomagnets

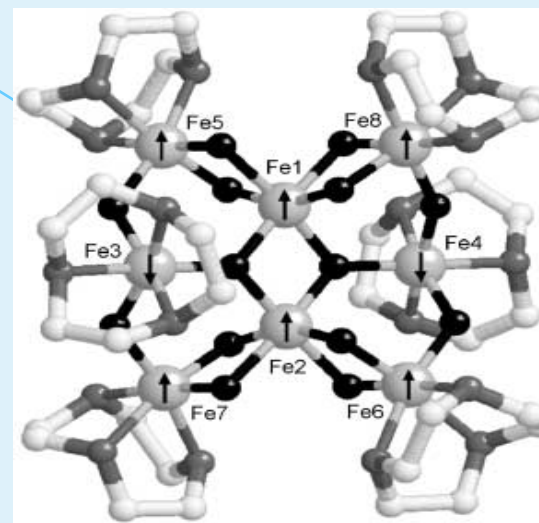


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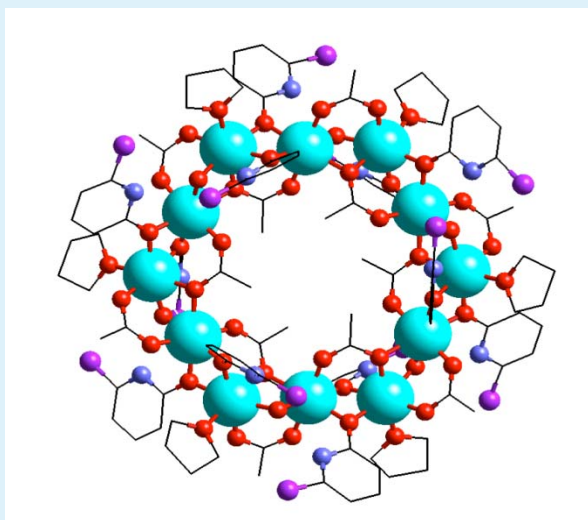
Lis, 1980

Mn12 S = 10



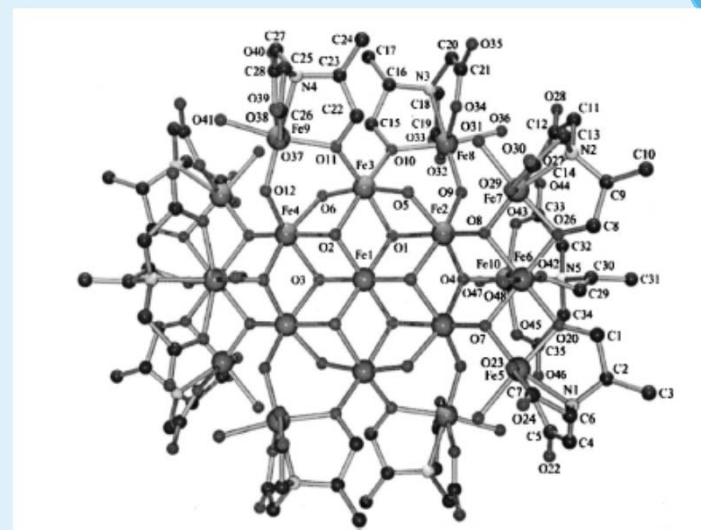
Fe8 S = 10

Wieghardt, 1984



Winpenny, 1999

Ni12 S = 12



Fe19 S=33/2

Powell, 2000



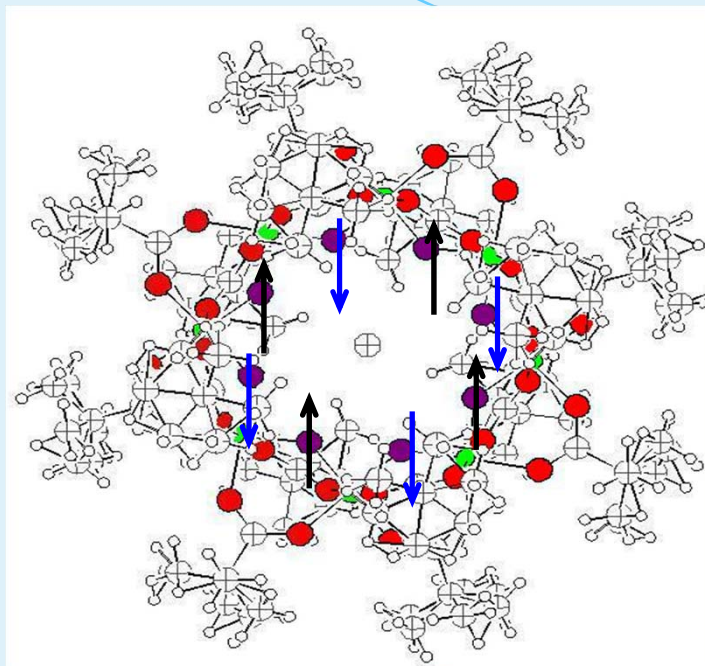
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Example :
Low-spin
Molecular magnets

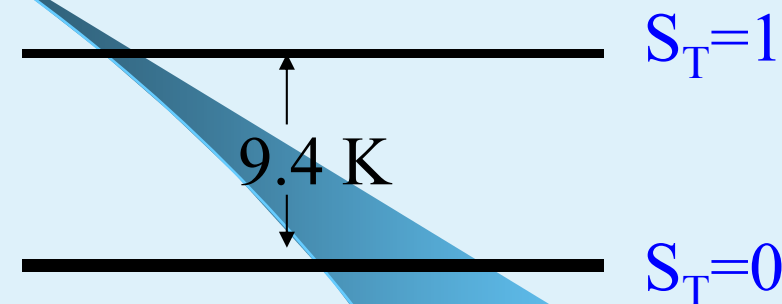
Some AF ring-like $S_T=0$ nanomagnets

Cr(III) $s = 3/2$
AF ground state
(total spin $S_T = 0$)

$J \approx 17.2$ K
 $\Delta_{0 \rightarrow 1} \approx 9.4$ K

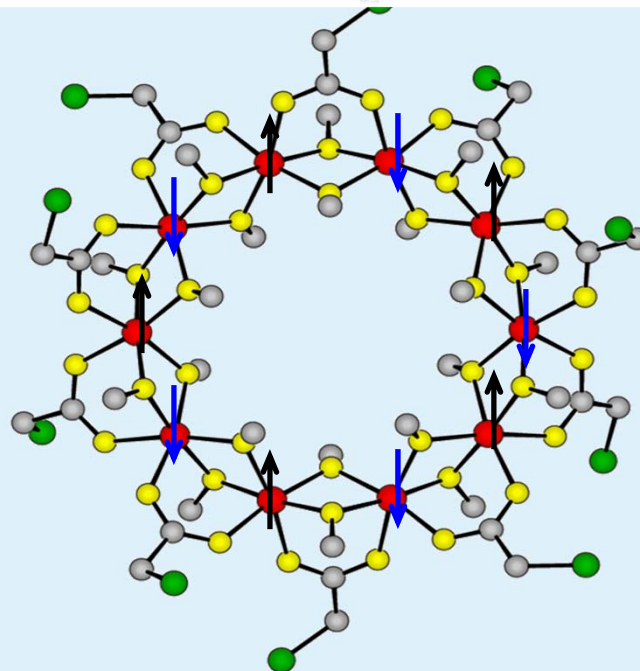


Cr8

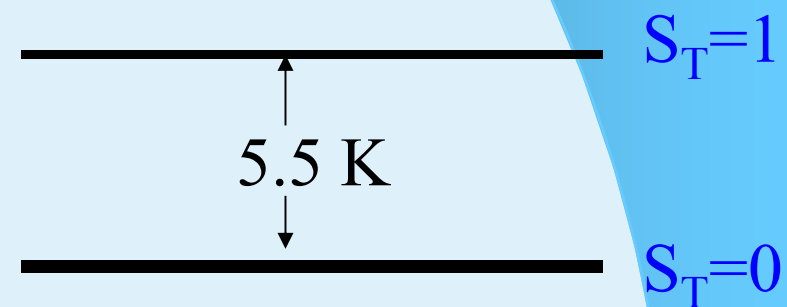


Fe(III) $s = 5/2$
AF ground state
(total spin $S_T = 0$)

$J \sim 13.8$ K
 $\Delta_{0 \rightarrow 1} \sim 5.5$ K



Fe10

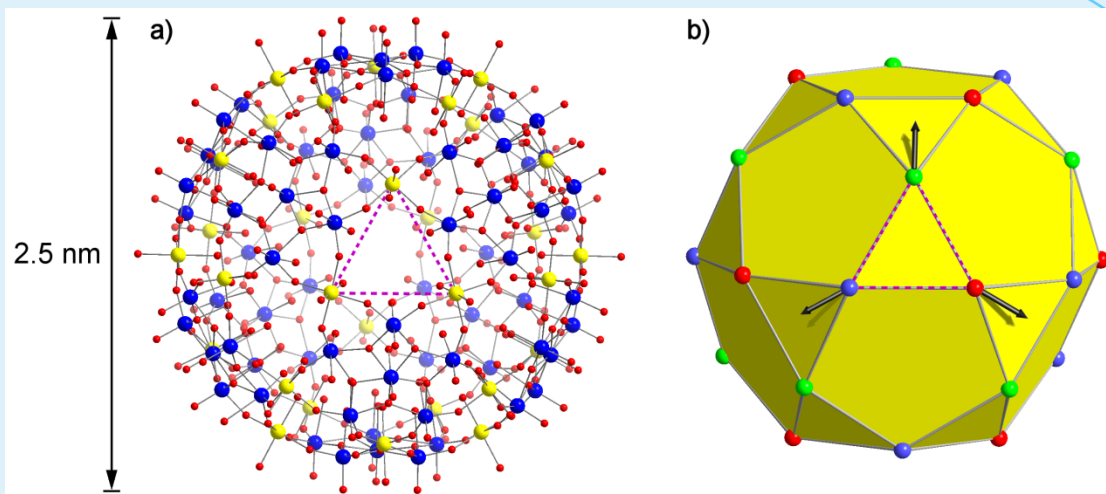


Other nanomagnets....

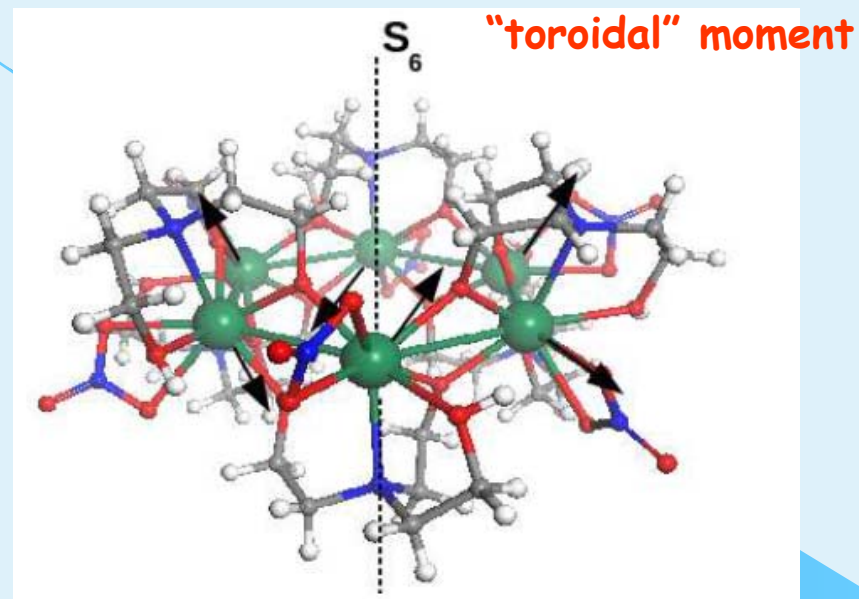


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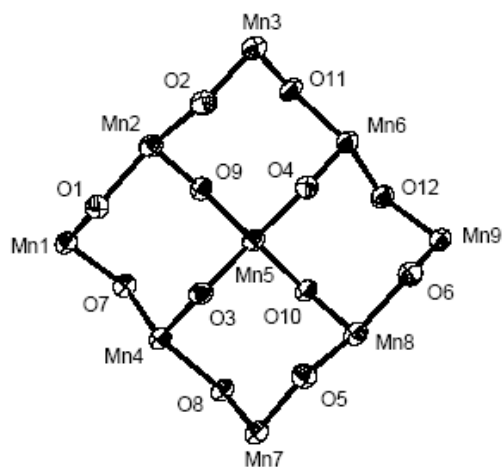
Fe₃₀



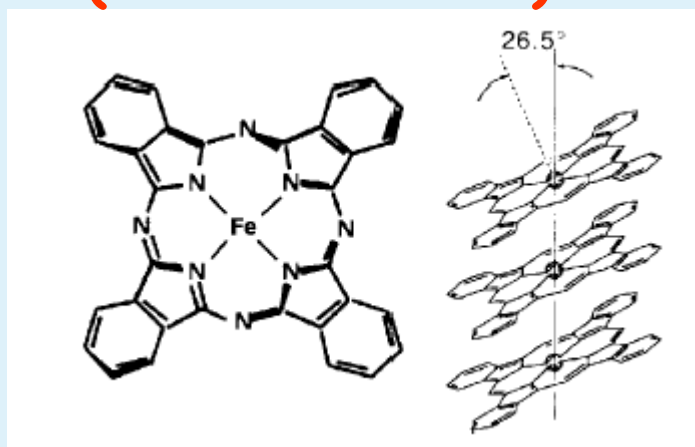
Dy₆



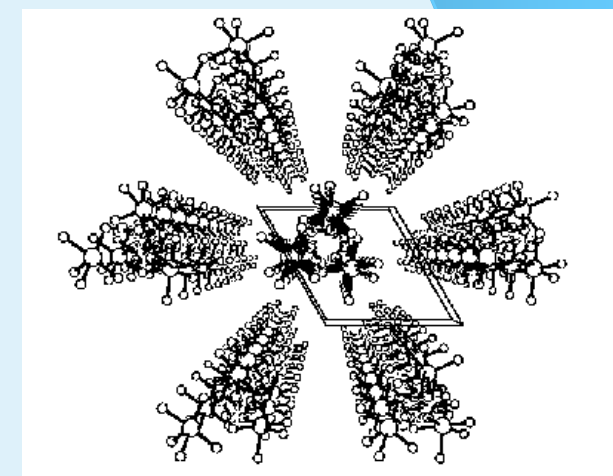
Mn 3x3 grid



Phthalocyanines-based (double deckers)



Single-chain magnets (1D magnetic nanowires)





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Example : Molecular chains

Examples of molecular chains

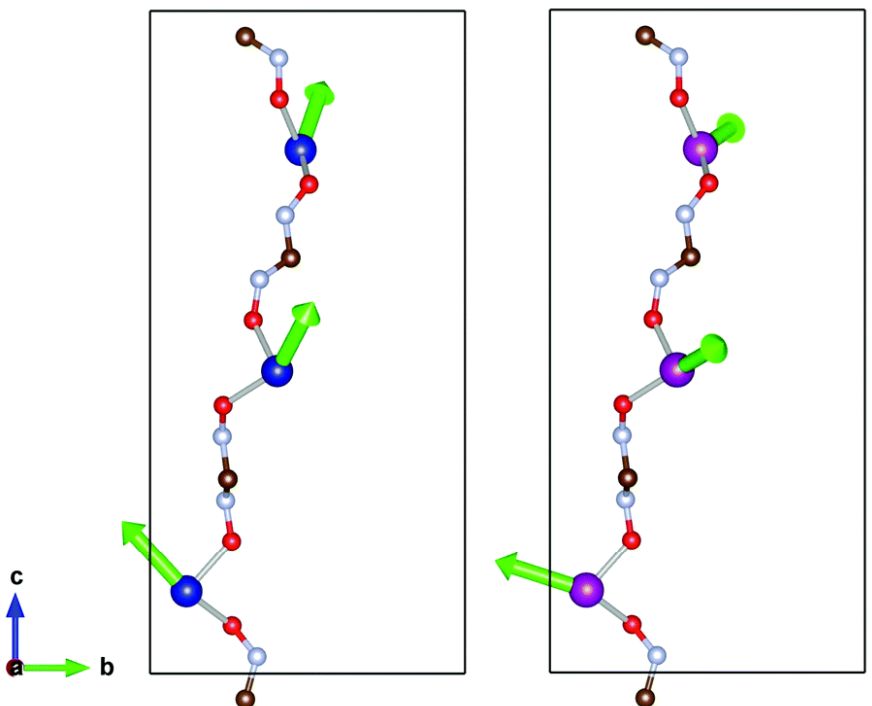


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single chain magnets

(a) CoPhOMe

(b) MnPhOMe



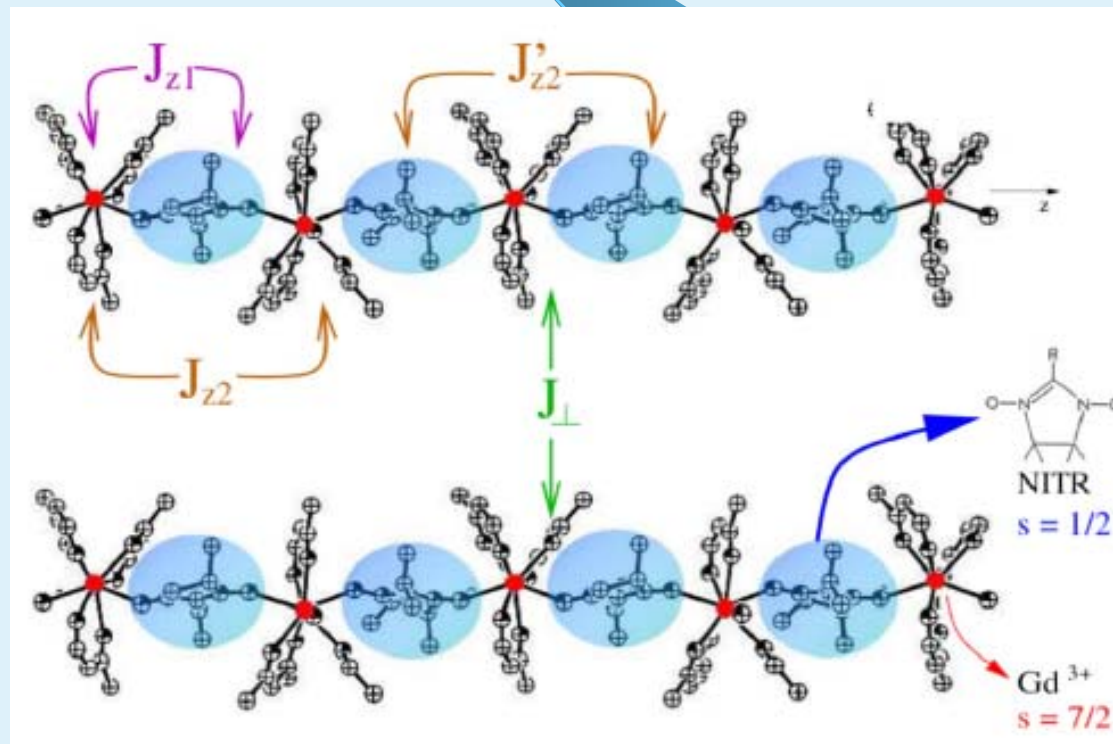
$$d_{local} = 0.51 D$$

$$\theta_{el} = 62^\circ$$

$$d_{local} = 1.22 D$$

$$\theta_{el} = 81^\circ$$

Gd-R chain. Villain's conjecture





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Why **Physics** of
Molecular magnets
is **so interesting** ?

Molecular Nanomagnets (MNM)



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Classical Physics involved

- Physics of low-dimensional systems (how magnetism depends on crystal and spin dimensionality
 - Spin dynamics : how spins move when T and H are varied
- system's dynamics, e.g. Brownian motion (due to temperature effect)

Quantum Physics involved

Due to finite number of magnetic ions \Rightarrow discrete energy levels

- gapped ground state : level crossing effects
- "macroscopic" quantum tunneling and/or tunneling of the Neel vector
(after D.Loss et al.)
 - spin dynamics in zero dimension
- measurement of the decoherence time (quantum computation)
 - quantum entanglement



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The switch from classical (physics)
to quantum mechanical depends
often on temperature region
of operation



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“Classical” (not trivial !!) physics :

Nanoparticles

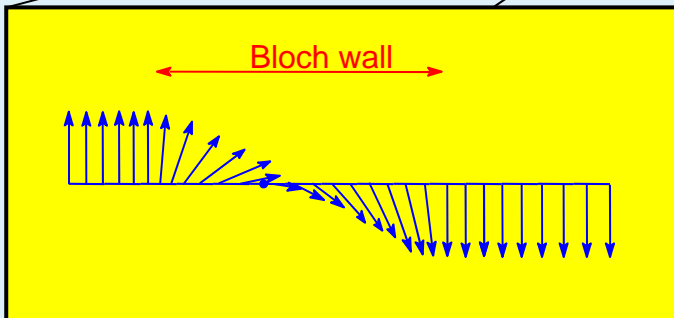
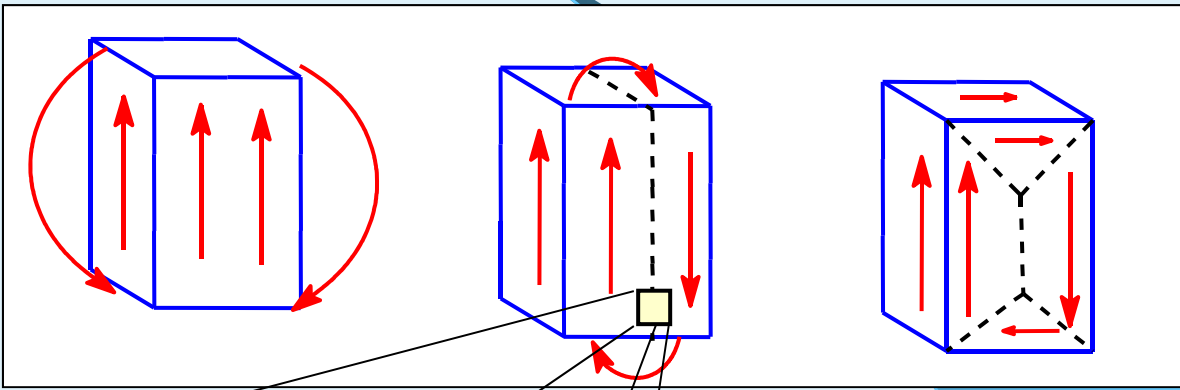
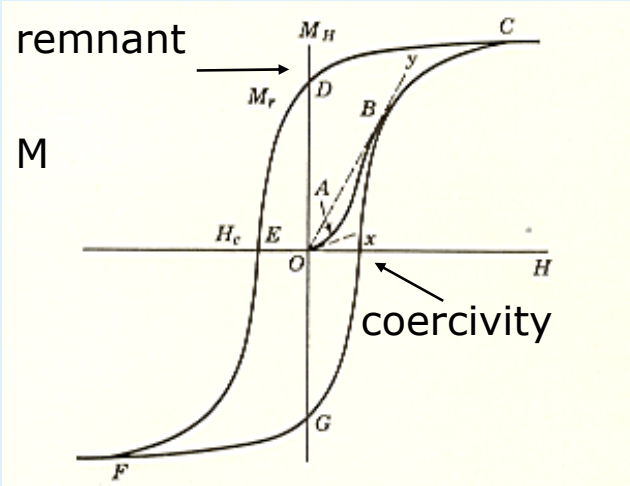
Molecular nanomagnets at “high” temperature

Nanomagnetism for "classical" NPs

Below a critical temperature, T_C , some materials exhibit spontaneous magnetization (ferro- and ferrimagnetism). Demagnetizing field induces domain formation (i.e. uniformly magnetized regions of different shape and size are formed).

$$E = E_{ex} + E_k + E_\lambda + E_D$$

E_{ex} exchange energy, E_k magnetocrystalline anisotropy energy, E_λ magnetoelastic energy, E_D magneto-static energy



The width of the domain wall depends on the anisotropy and exchange coupling and

$$\delta = \pi \sqrt{A/K}$$

A = exchange energy density (J/m^2)

K = magnetic anisotropy energy density (J/m^2)

Typical values of domain wall width are in the 10-100 nm range.

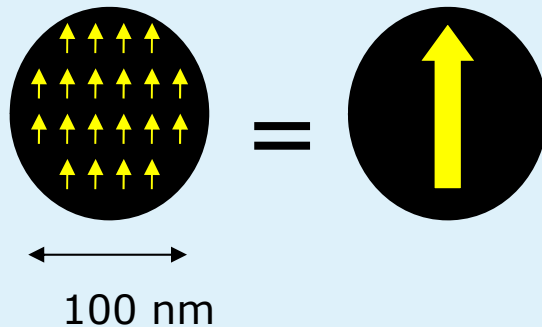
Single Domain Nanoparticles

Total wall energy per area unit: $E_\sigma = 2(AK)^{1/2}$

Reducing the dimensions of the crystal: competition among E_σ and the magnetostatic energy, E_λ . But E_λ scales with the volume, E_σ with the surfaces

→ There exists a lower limit in size, D , corresponding to the single domain state.

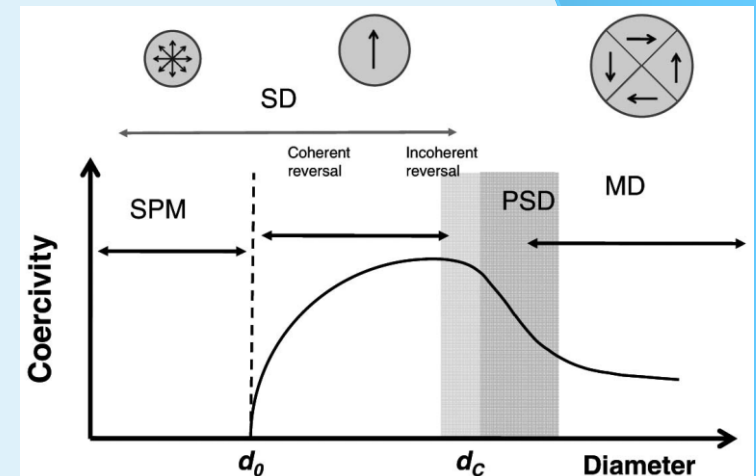
$$D = 18 E_\sigma / \mu_0 M_S^2$$



Typical D values:

| | |
|----------------------------------|--------|
| Fe | 15 nm |
| Co | 70 nm |
| Ni | 55 nm |
| NdFeB | 100 nm |
| Fe ₃ O ₄ | 128 nm |
| γ-Fe ₂ O ₃ | 166 nm |

When $D < \delta$ all the spins are coupled (Exchange Energy is constant). The inversion of M occurs through a coherent movement of all the spins of the particle.



Single Domain Nanoparticles

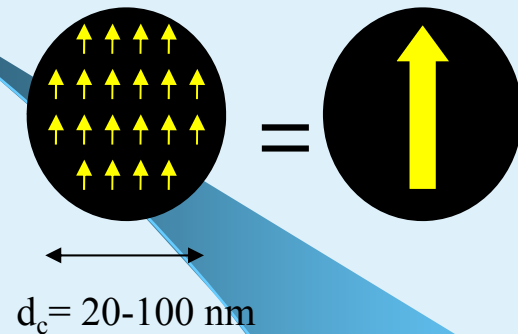
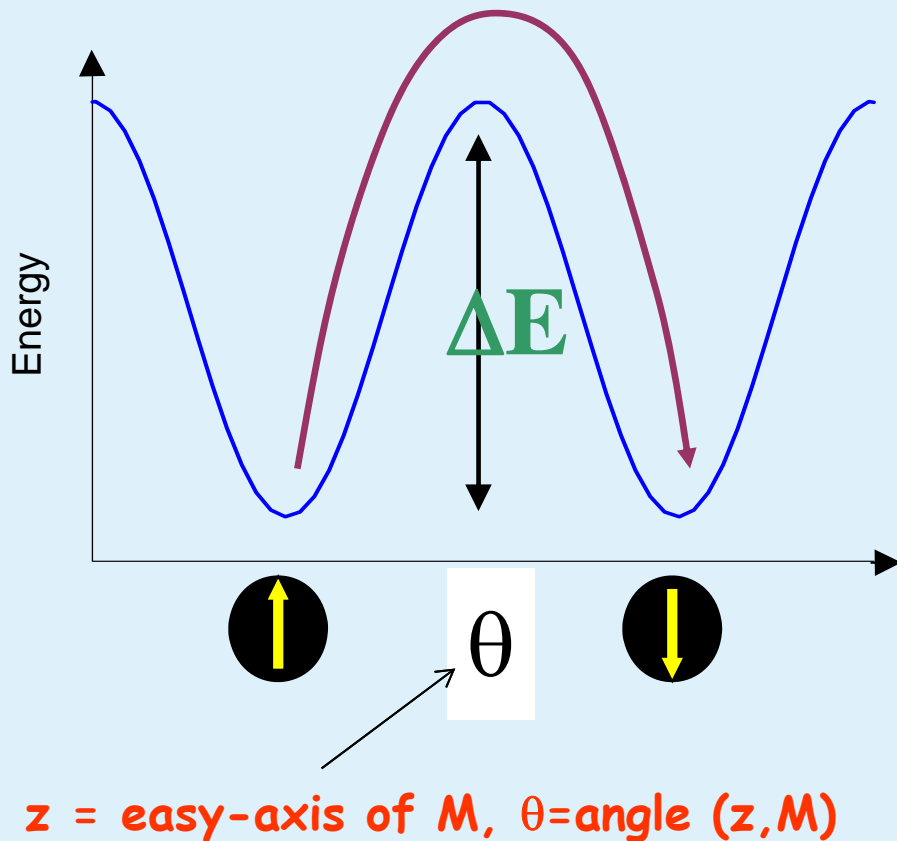
(small ferromagnets under critical diameter d_c)



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Superparamagnetism (giant spin)

Stoner-Wolhfarth model:



The inversion of M occurs through a **coherent movement** of all the spins of the particle

$$\text{Energy barrier } \Delta E = k_A V$$

$k_A =$ anisotropy constant, $V =$ particle volume

$$\tau_N = \tau_0 \exp(\Delta E / k_B T)$$

Neel correlation time

If NPs interact : **Vogel-Fulcher model**, $\tau_N = \tau_0 \exp[\Delta E / k_B (T - T_0)]$



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Also in MM for studying the
fundamental physical processes and
for the applications **we need** to
follow **the typical**
times of the systems

**For example some MM
are superparamagnetic**



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**How to detect the dynamics
typical of systems ?**

**The (extended) "resonance"
concept**

Il fenomeno della risonanza

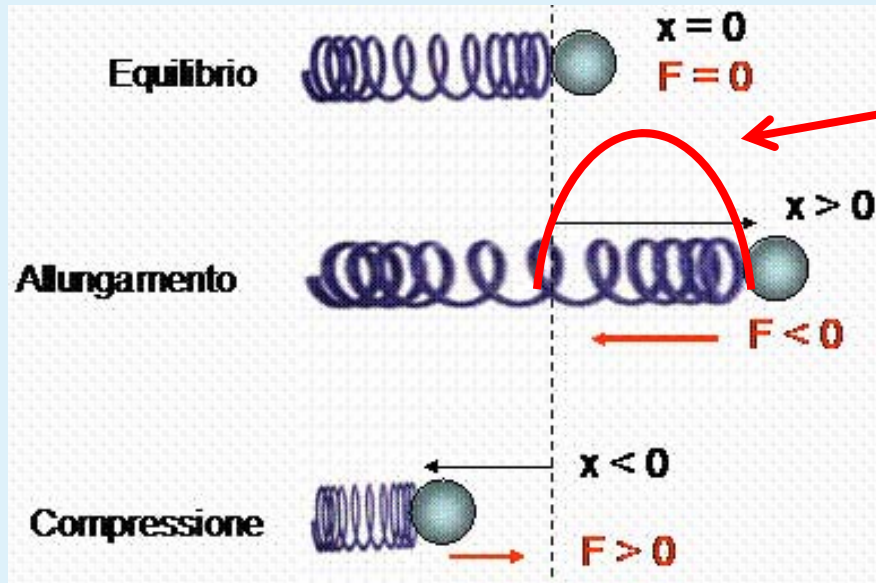
- Consiste in una risposta "aumentata" dei sistemi

(molla, chitarra/microfono, ponti, nuclei, elettroni, molecole,...)

sollecitati da una azione esterna agente a frequenze proprie dei sistemi stessi

Quando si ha risonanza c'è un picco nella risposta del sistema

Il fenomeno della risonanza

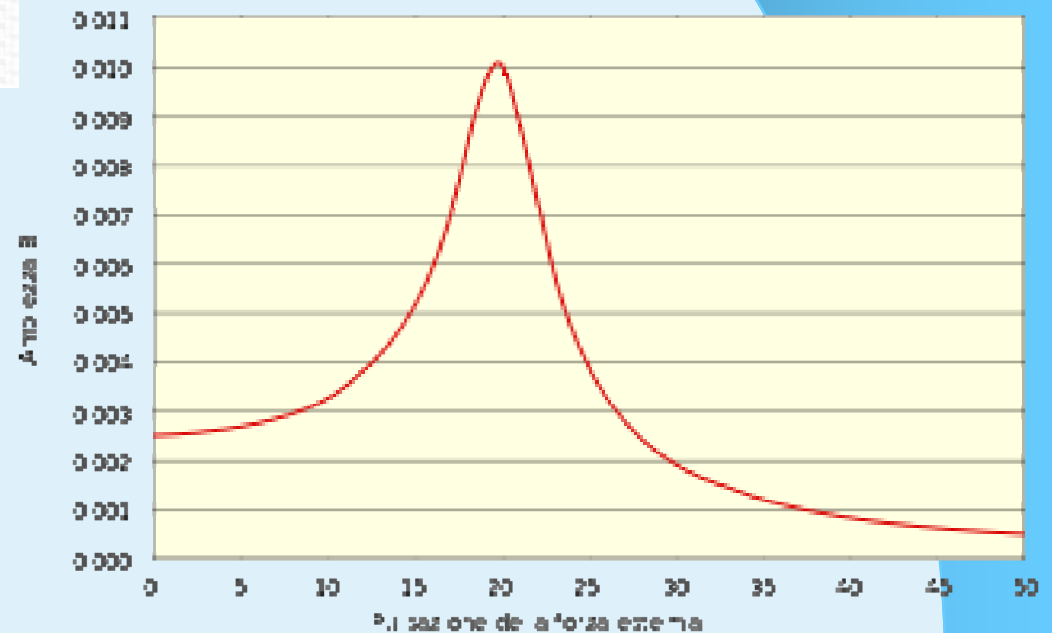


**AMPIEZZA DELLA MOLLA
(MAX ALLUNGAMENTO)**

RISONANZA DELLA MOLLA

Se la molla viene "forzata"
dall'esterno alla sua
frequenza,
aumenta l'ampiezza della sua
oscillazione

Ampiezza dell'oscillatore forzato



Il fenomeno della risonanza



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RISONANZA SONORA : effetto Larsen in chitarre amplificate

20 Hz - 500 Hz

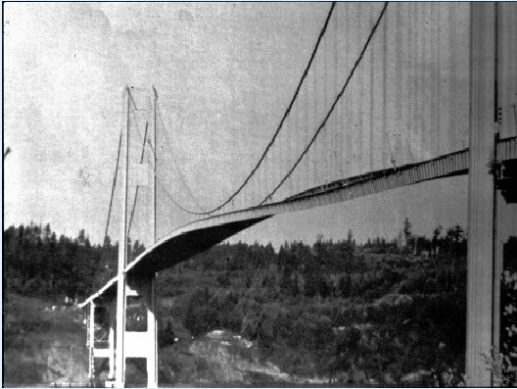
Time 2.00 & 3.15



Il fenomeno della risonanza

RISONANZA MECCANICA :

Ponte di Tacoma che oscilla e poi crolla causa vento a circa 67 km/h



GALE CAUSES
BRIDGE
TO SWAY



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**Conditions for observing
a resonance** typical of motions
inside the investigated system :
stimulate the system **with**
a frequency ω_{meas}
near a typical system frequency $\nu_c = 1/\tau_c$:

$$\omega_{\text{meas}} \tau_c \approx 1$$

Possible motions : spin motion,
Brownian motion, molecular motion



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**FOR THIS PURPOSE
ONE CAN USE DIFFERENT
TECHNIQUES ABLE TO
DETECT MAGNETIC PROPERTIES**

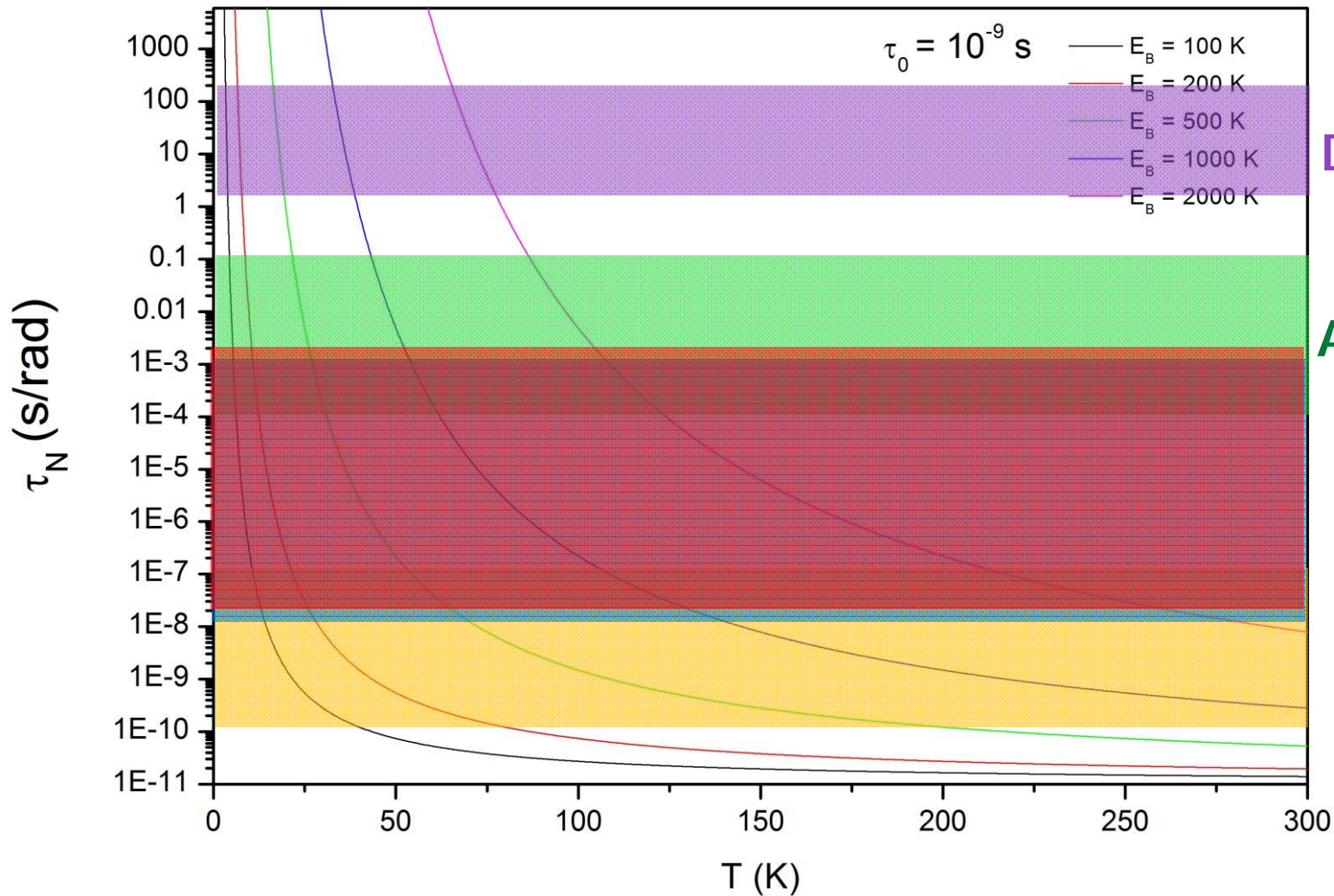
Concept of response function

**(e.g. specific heat, magnetic
susceptibility)**

Typical times/frequencies : how to observe the dynamics



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DC Magnetometry

AC Susceptibility

MUSR

NMR

Mössbauer Spectroscopy

SPM particle blocking is noticeable when $\tau_m = \tau_N$ at a given temperature



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Some response functions

(to the external stimuli)

Molecular magnets

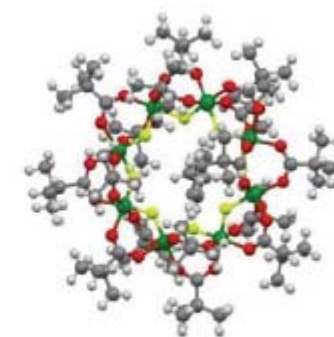
DC susceptibility : Curie law for $T > 100\text{K}$

RINGS

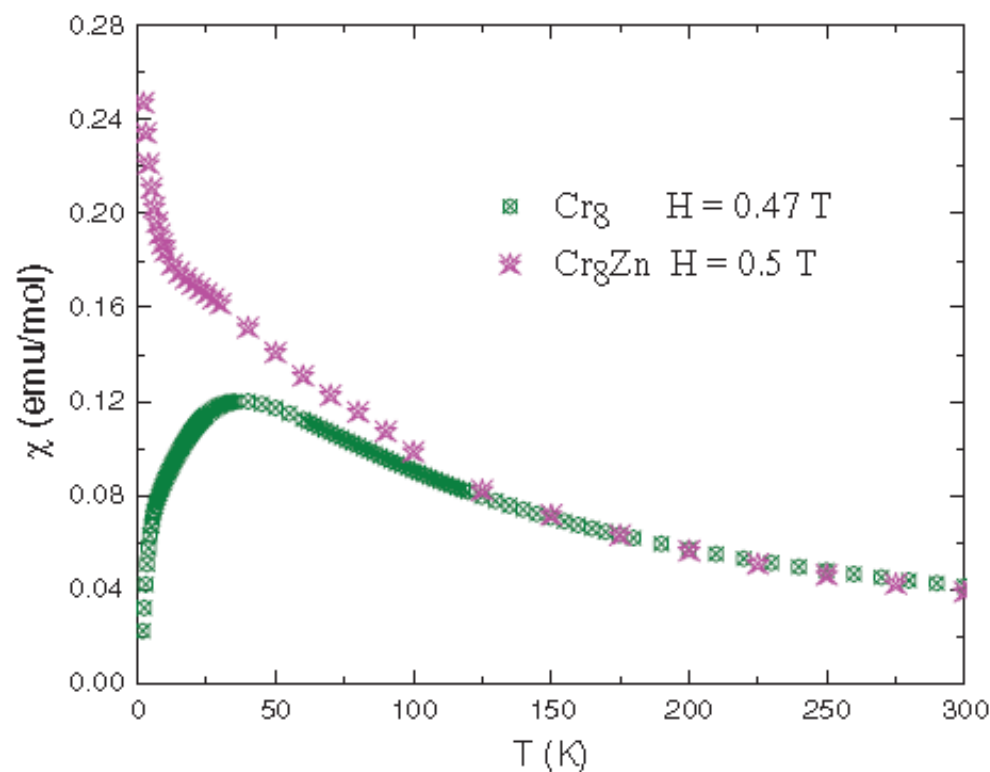
Just one atom
makes the difference !!



Cr_8Zn "Open Ring"

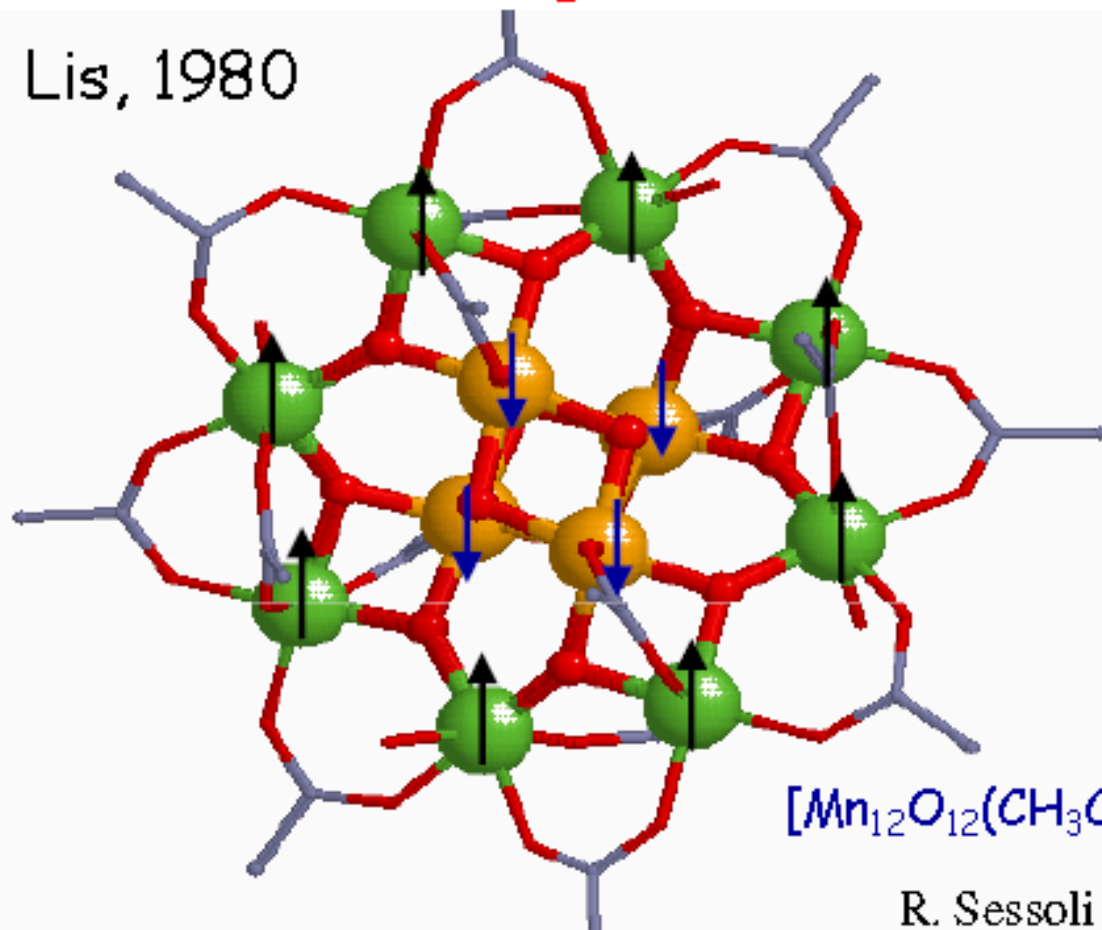


Cr_8 "Closed Ring"



The first single molecule magnet: Mn_{12} -acetate

Lis, 1980

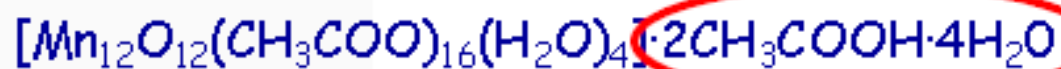


Mn(III) ● $S = 2$ ↑

Mn(IV) ● $S = 3/2$ ↓

Oxygen ●

Carbon ●



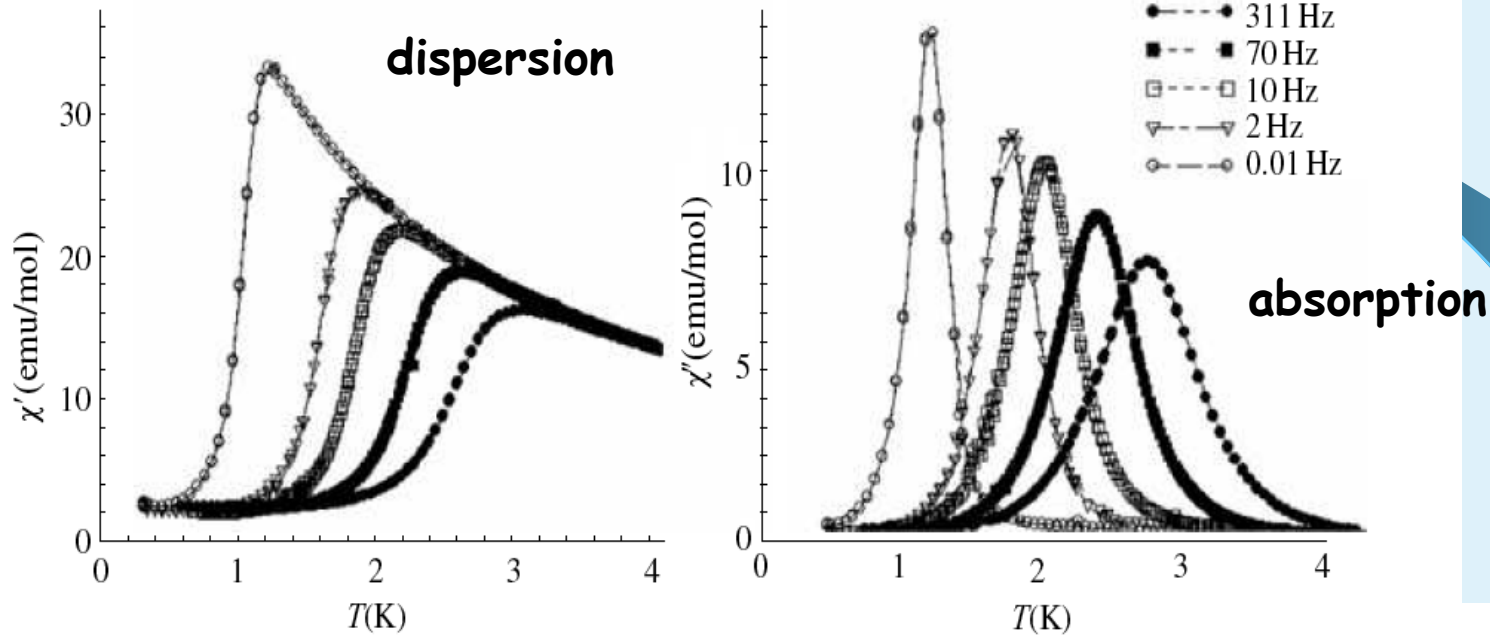
R. Sessoli et al. JACS 115, 1804 (1993)

AC susceptibility typical data : varying the frequency

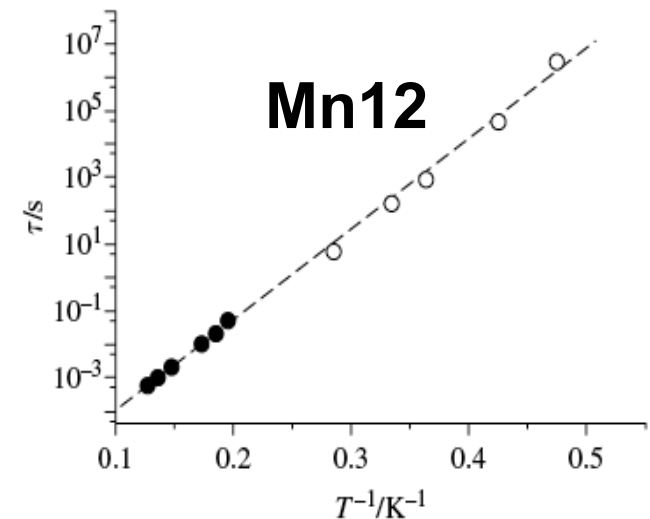


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Spin block : “Blocking” temperature



Maximum (response) for
 $\omega_{AC}\tau = 1$
 τ = correlation time of spins
i.e. Neel time !





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Another "source" for understanding
the response function.

An historical technique for Pavia:

Nuclear Magnetic Resonance

An historical technique for Pavia: Nuclear Magnetic Resonance



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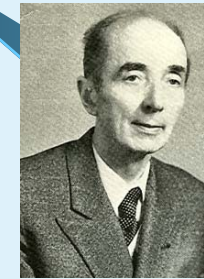


1944

Isidor Isaac Rabi

The Nobel Prize in Physics 1944 was awarded to Isidor Isaac Rabi "for his resonance method for recording the magnetic properties of atomic nuclei".

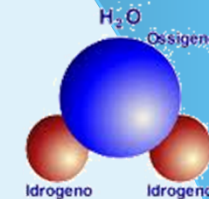
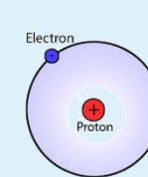
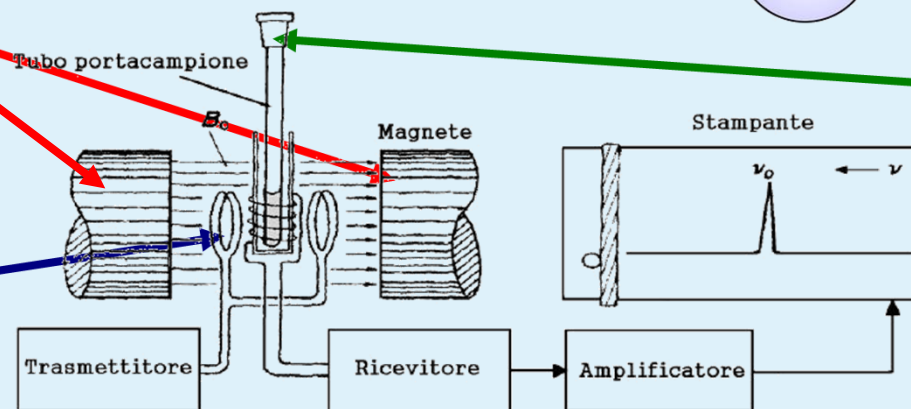
**Esperimenti RMN di
Luigi Giulotto (Università di Pavia)**



1948/50

Il **primo esperimento** di Risonanza Magnetica Nucleare nella materia condensata (nucleo dell'atomo di idrogeno)

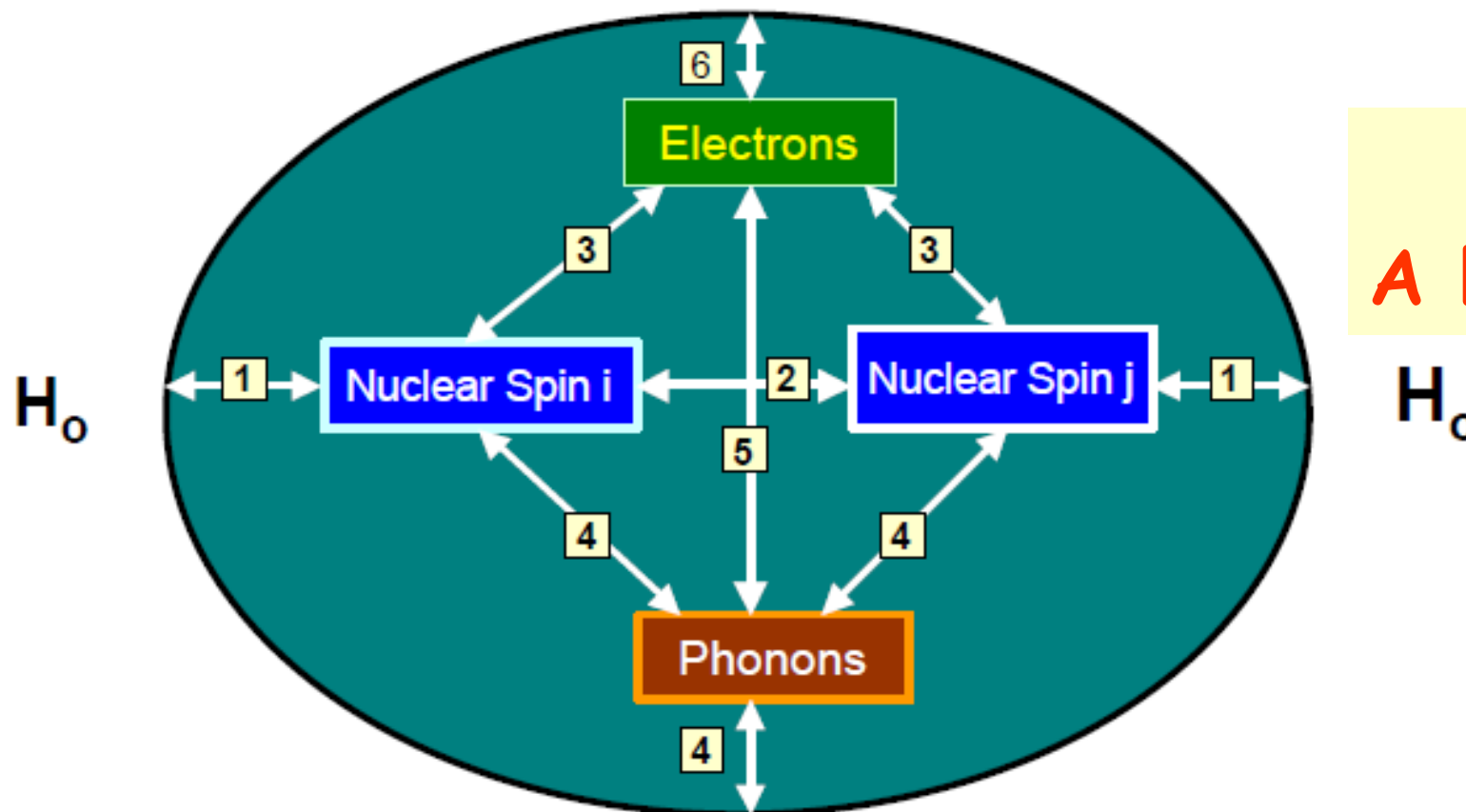
Magnete che genera un campo magnetico statico
Bobine che generano un campo magnetico a radiofrequenza



**Campione
di H₂O**

1945/46 : Bloch - Purcell

NMR.
A local probe



$$H = H_z + H_D + H_{CS} + H_Q + H_{hyp} + H_J + H_{ce}$$

H_z = Zeeman interaction, path 1 ($\propto B_0 \sim 10^9$)

H_D = Dipolar interactions among nuclear spins, path 2,3 ($\propto I \cdot S \cdot r^{-3} \sim 10^{3-5}$)

H_{CS} = Chemical shielding interaction, path 6 and 3 ($\sim 1 - 10^5$)

H_Q = Quadrupolar interaction (nuclei $I > 1/2$) with surrounding ∇E , path 3 ($10^3 - 10^7$)

H_{hyp} (paramagnetic shift) = hyperfine e-n dipolar (pseudocontact) and contact interactions, path 3 (influenced by 5)

H_J = J-coupling, path 2 via path 3

H_{ce} = interaction of nuclei with conduction electrons (e.g. nuclei, Knight shift), path 3



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NMR

- Absorption spectra (almost **static** response)
- Nuclear time to reach equilibrium $1/T_1$:
nuclear **dynamical** response
- Also T_2

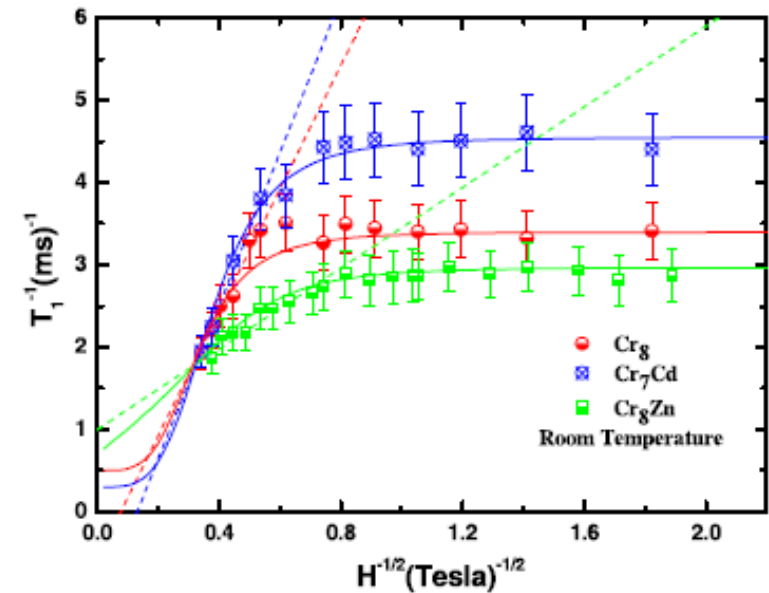
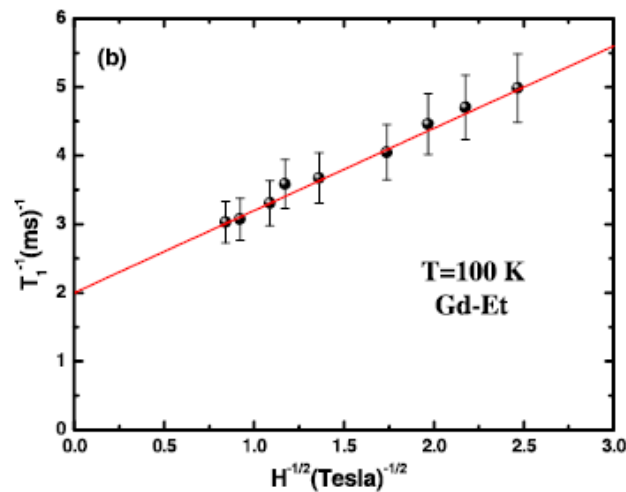
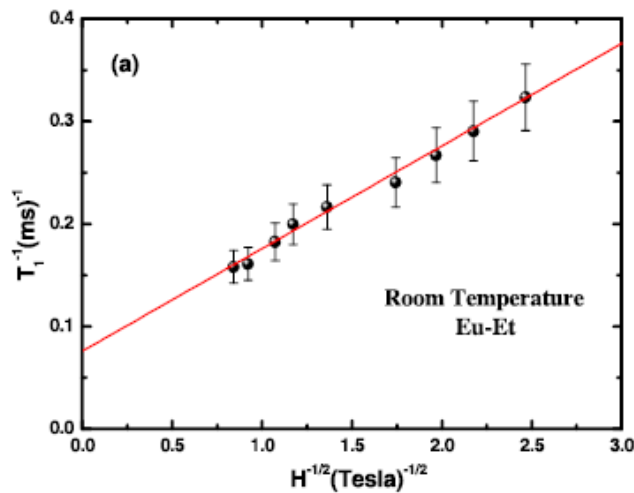
EXAMPLE AT ROOM TEMPERATURE



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1D spin diffusion
Molecular chains

No spin diffusion
Molecular rings



$$1/T_1 = A / (1 + (H/H_c)^2) + C \text{ (ms}^{-1}\text{)}$$

$$1/T_1 = PH^{1/2} + Q.$$

AGAIN "CLASSICAL" BEHAVIOUR DETECTING SPIN MOTION

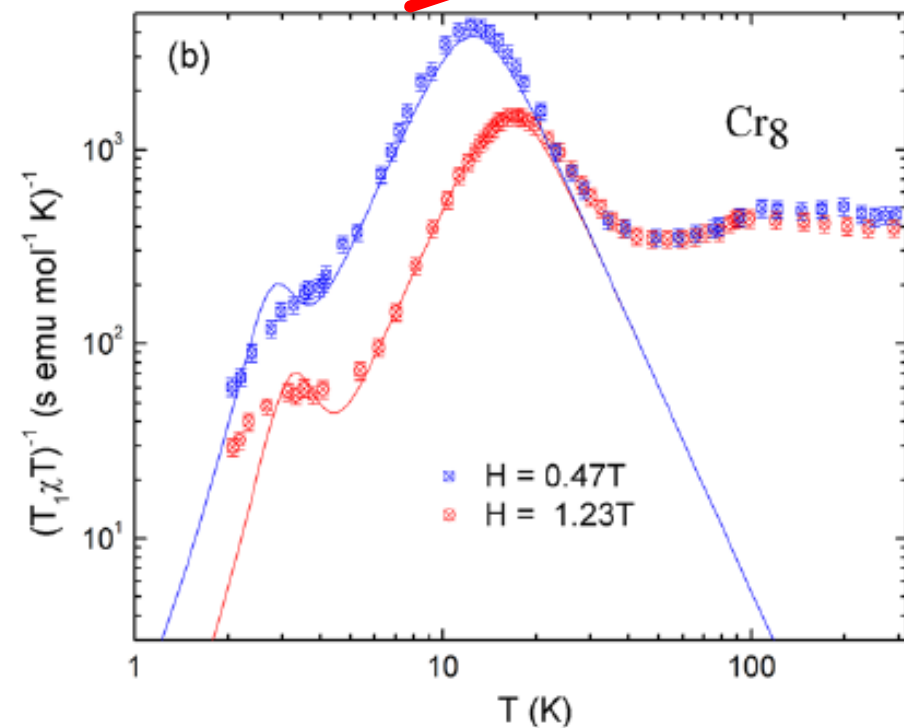
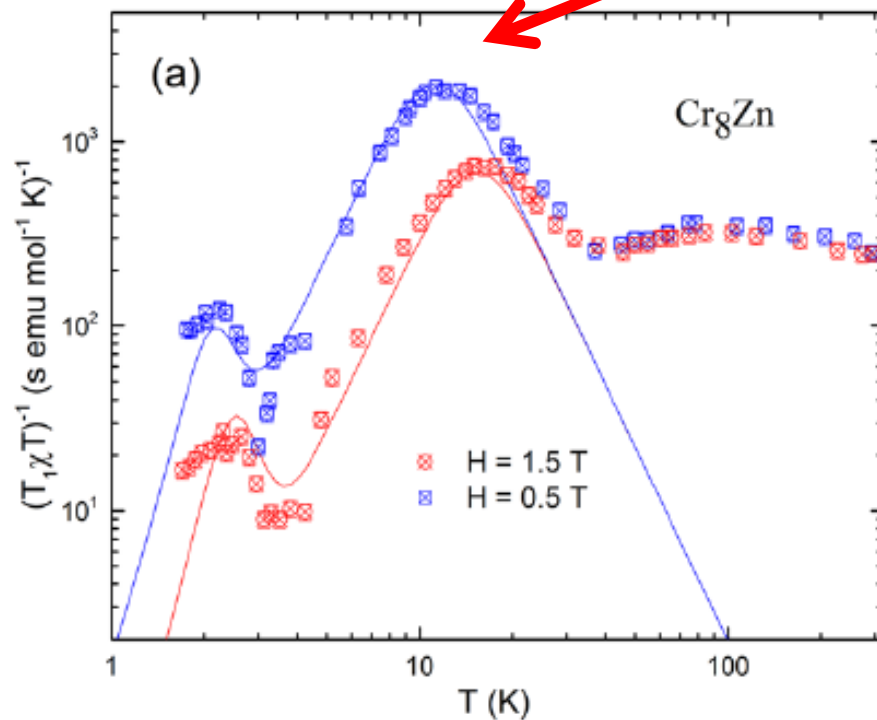


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Vs temperature behaviour

Peaks → max resp. function at

$$\frac{1}{T\chi T} = A \left\{ \frac{\lambda_1 \omega_{e1}(T)}{\omega_{e1}^2(T) + \omega_L^2} + \frac{\lambda_2 \omega_{e2}(T)}{\omega_{e2}^2(T) + \omega_L^2} \right\}$$

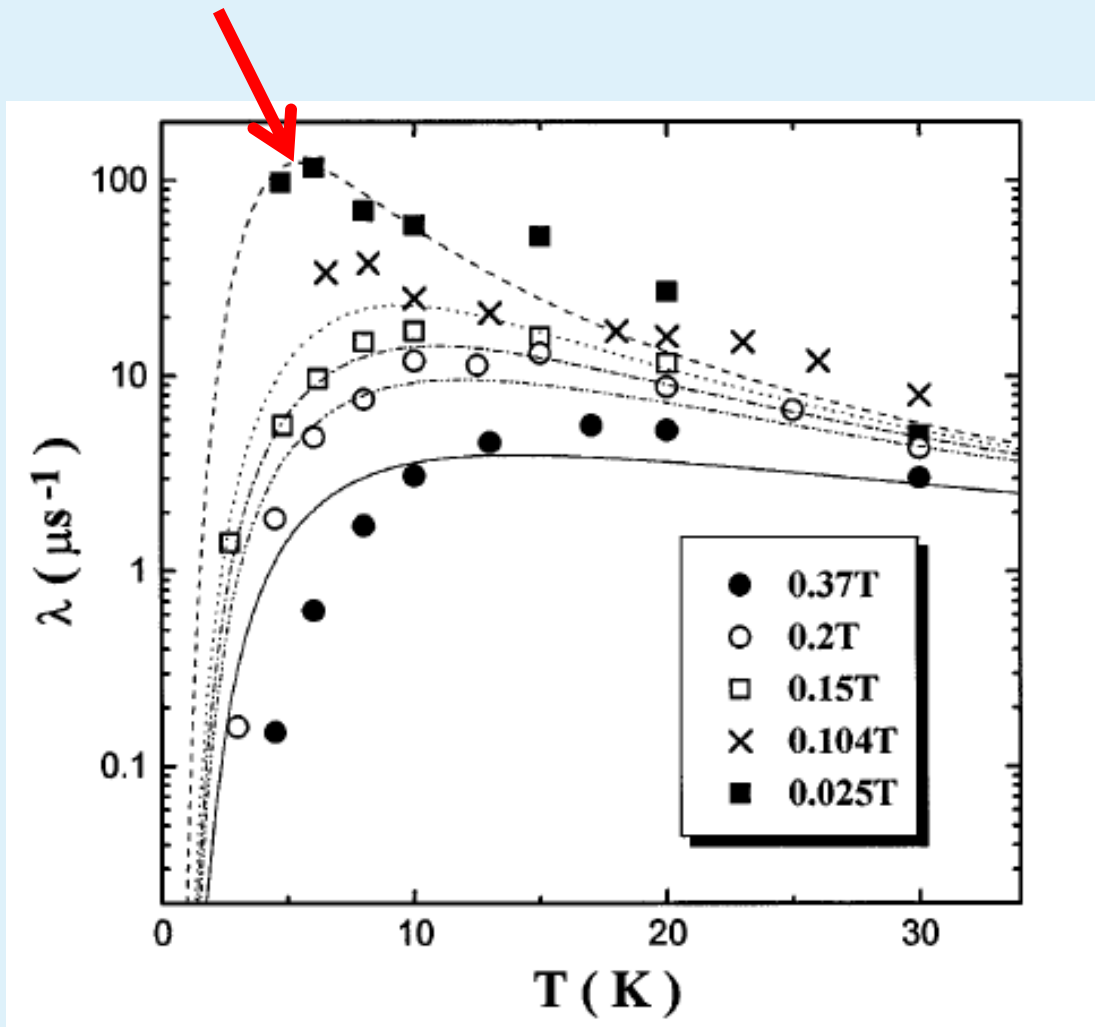




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"Quasi-classical" effect : Muon Spin Resonance, a local technique similar to NMR

Peaks at $\omega_{\text{meas}}\tau \approx 1$



Mn12

max when $\omega_{\text{meas}}\tau_c \approx 1$
In this case a bit more
complicate
due to quantum structure
of energy levels

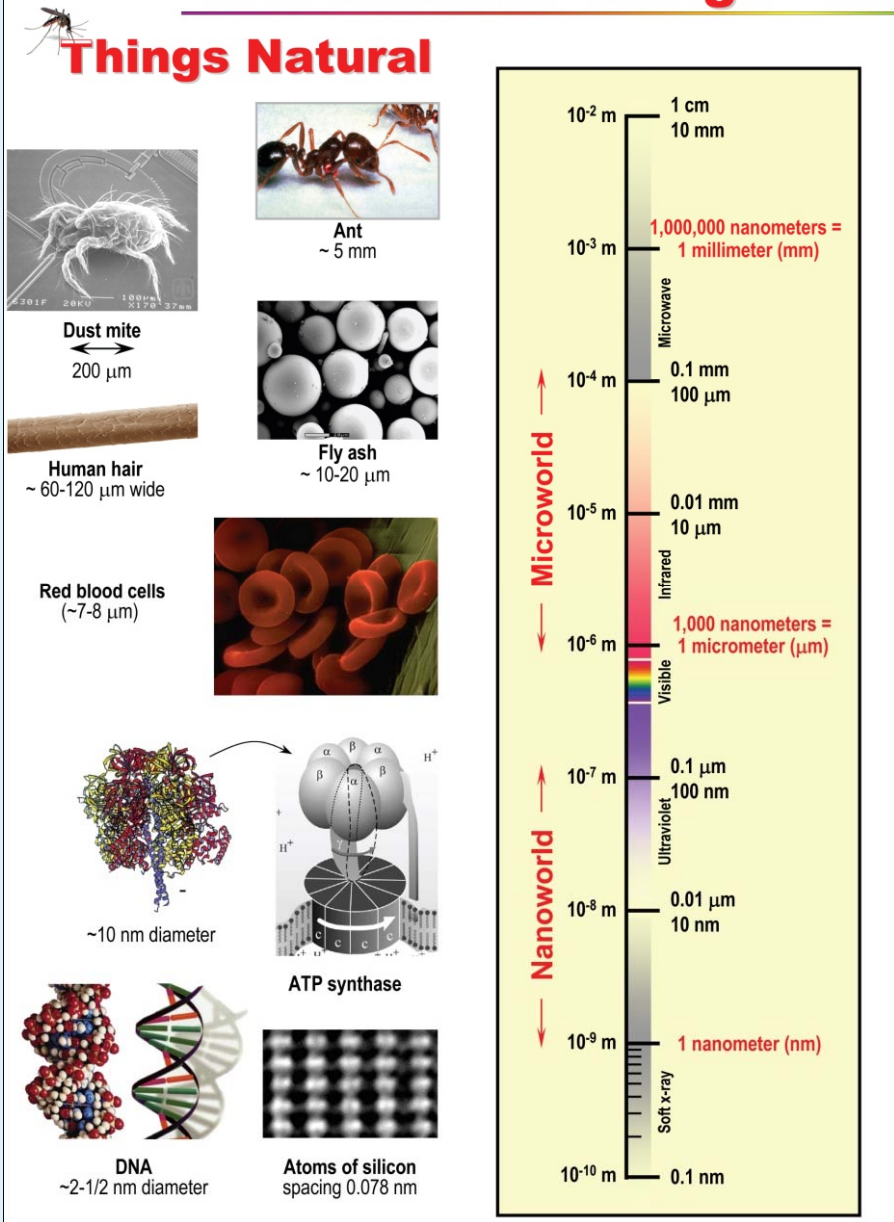


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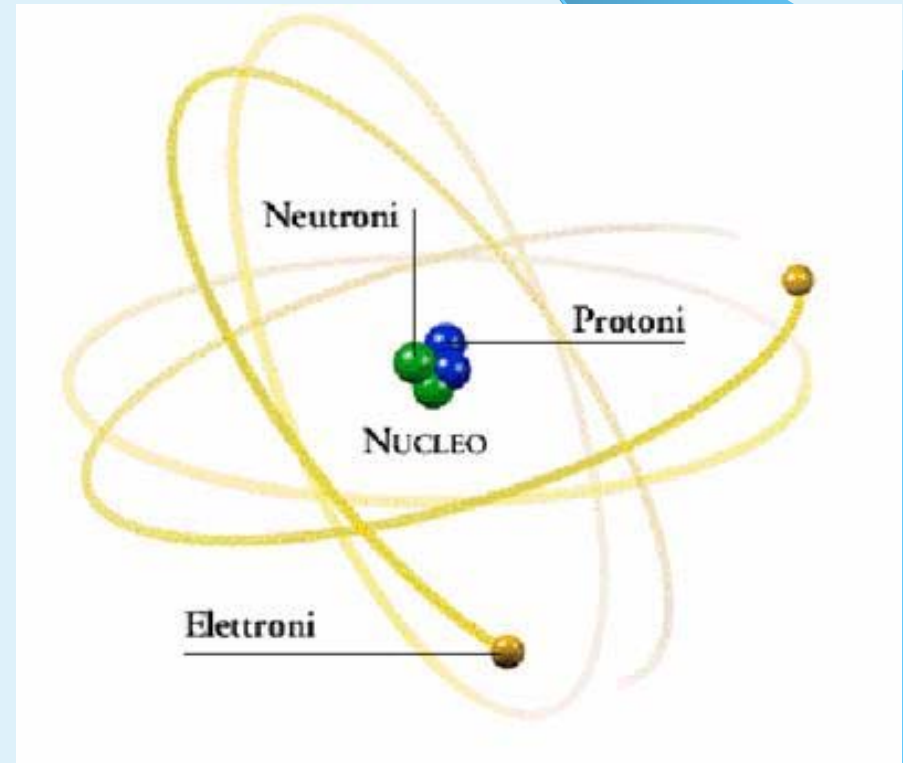
... going to quantum world

Struttura atomica e nucleare

The Scale of Things – Nature



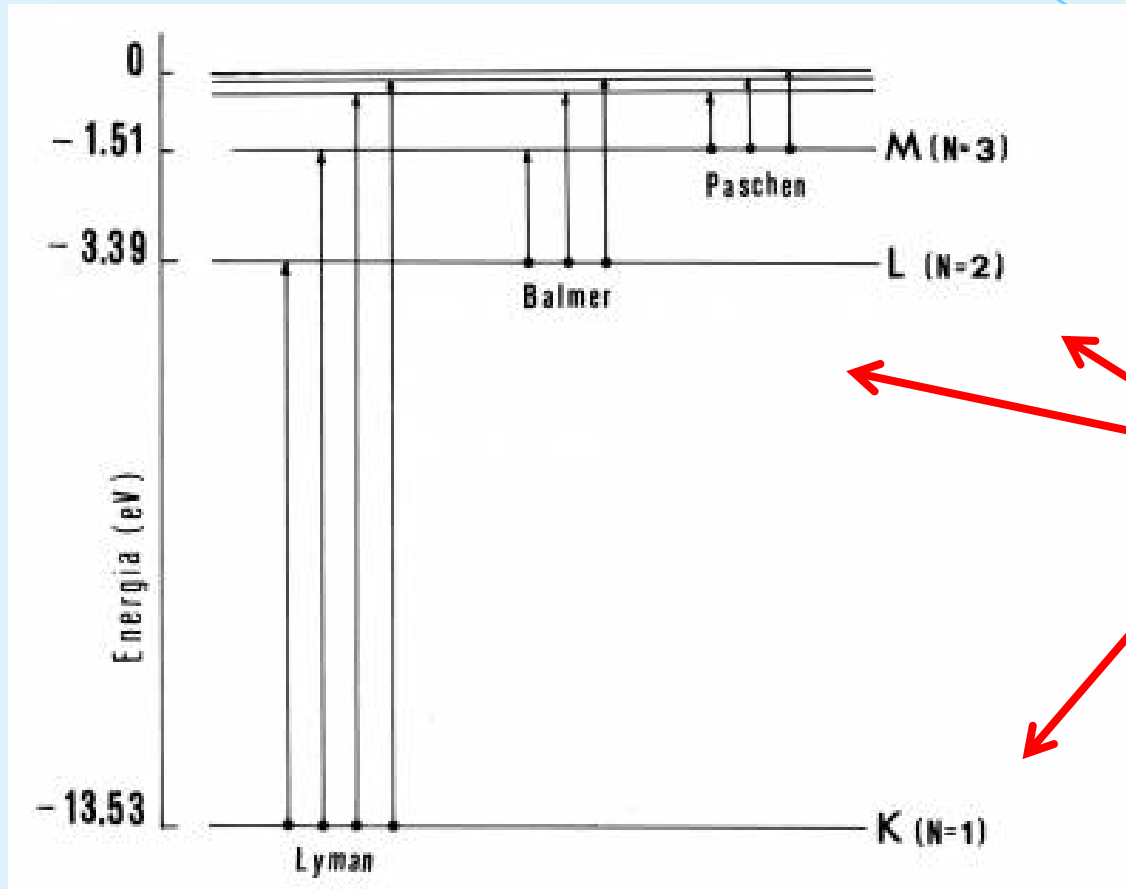
Organi → tessuti → molecole
→ Atomi → nuclei
Particelle atomiche e subatomiche



Struttura atomica e nucleare



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Quantizzazione dei
Livelli energetici

Esempio : atomo di
idrogeno

ATOMI E NUCLEI
SONO SISTEMI
QUANTISTICI

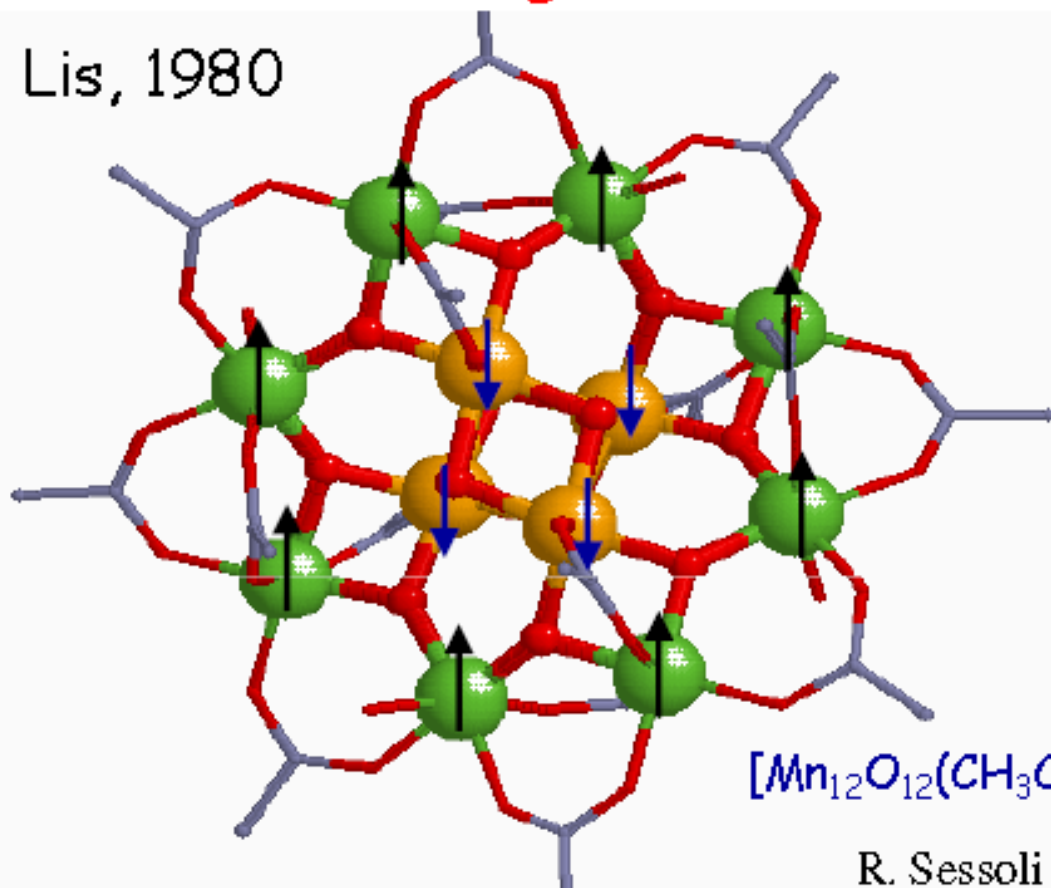
Un sistema quantistico non può assumere (in modo continuo) tutti i valori di energia

Quantum Physics of Mn12

Few N spins : $(2s+1)^N$ levels

The first single molecule magnet: Mn_{12} -acetate

Lis, 1980

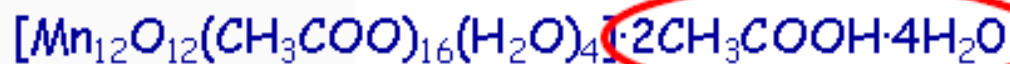


Mn(III) ● $S = 2$ ↑

Mn(IV) ● $S = 3/2$ ↓

Oxygen ●

Carbon ●



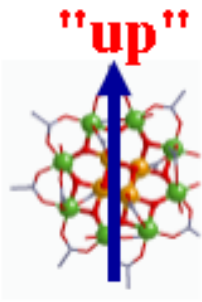
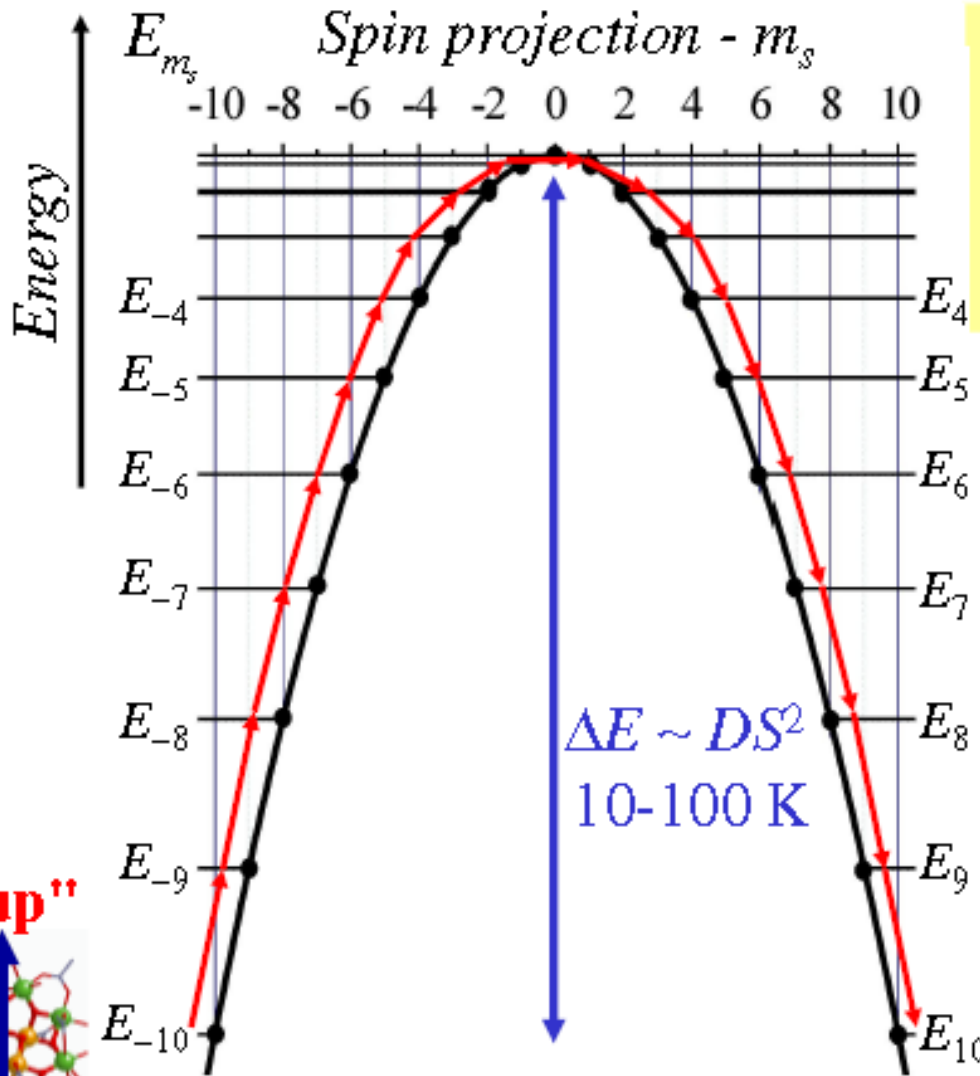
R. Sessoli et al. JACS **115**, 1804 (1993)

Discrete levels. Superparamagnetic behaviour



Pavia, 07/06/16

Quantum effects at the nanoscale ($S = 10$)



Thermal activation

Simplest case: axial
(cylindrical) crystal field

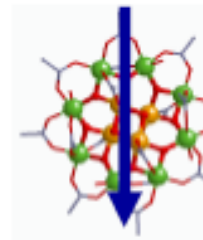
$$\hat{H} = D\hat{S}_z^2 \quad (D < 0)$$

Eigenvalues given by:

$$E(m_s) = -|D|m_s^2$$

- Small barrier - DS^2
- Superparamagnet at ordinary temperatures

"down"



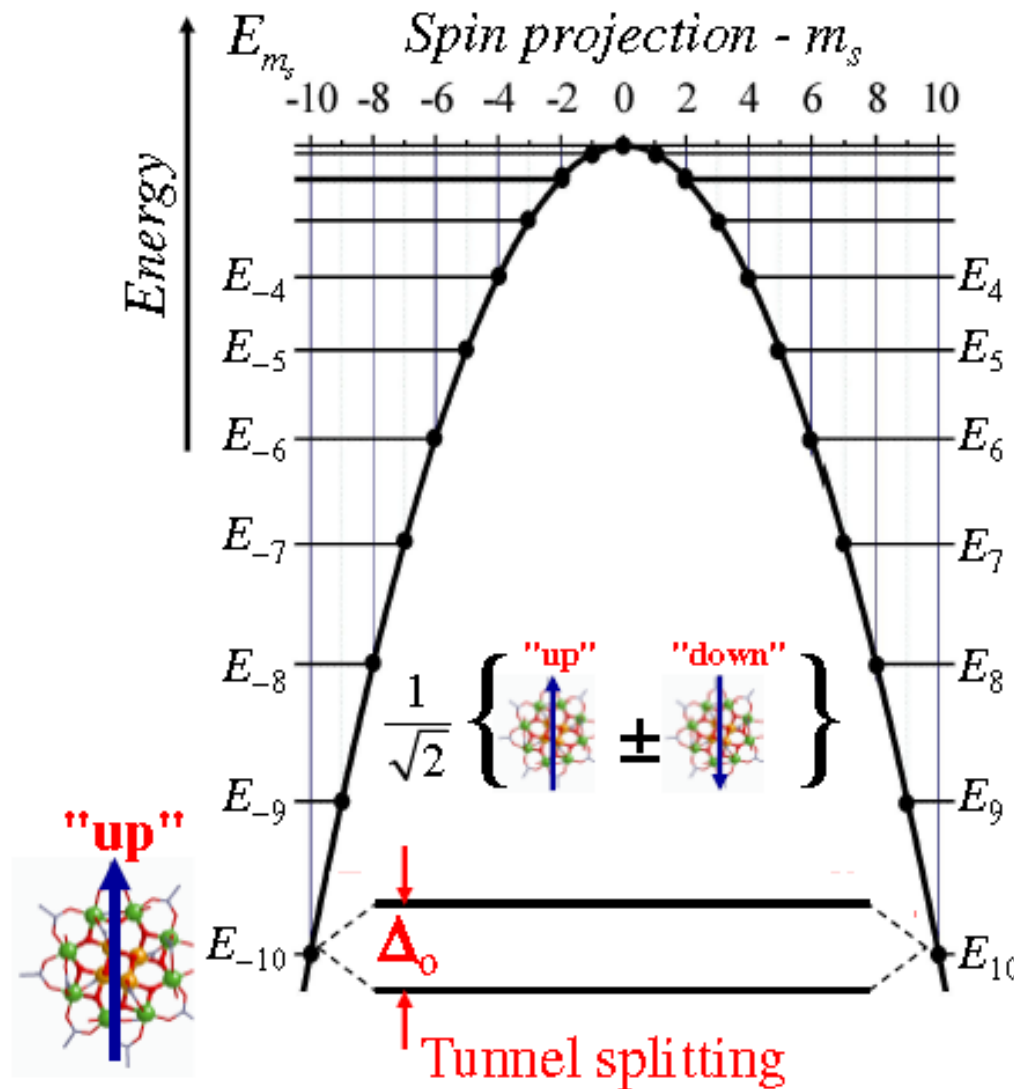
$|D| \sim 0.1 - 1$ K
for a typical
single molecule
magnet

Quantum tunneling of the magnetization (QTM)



Pavia, 07/06/16

Quantum effects at the nanoscale ($S = 10$)



letters to nature

Quantum computing in molecular magnets

Michael N. Leuenberger & Daniel Loss

Department of Physics and Astronomy, University of Basel, Klingelbergstrasse 82,
4056 Basel, Switzerland

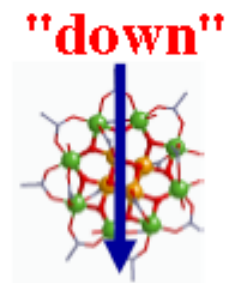
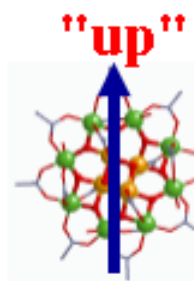
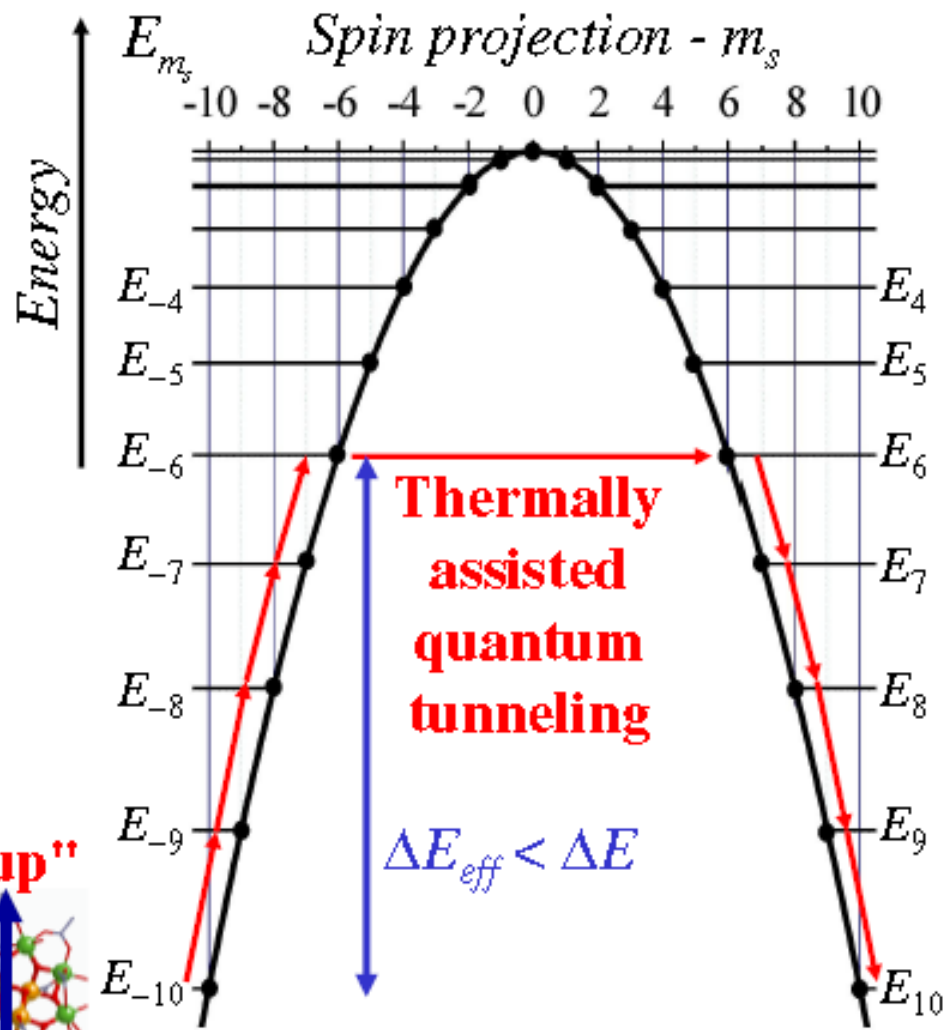
Shor and Grover demonstrated that a quantum computer can outperform any classical computer in factoring numbers¹ and in searching a database² by exploiting the parallelism of quantum mechanics. Whereas Shor's algorithm requires both superposition and entanglement of a many-particle system³, the superposition of single-particle quantum states is sufficient for Grover's algorithm⁴. Recently, the latter has been successfully implemented⁵ using Rydberg atoms. Here we propose an implementation of Grover's algorithm that uses molecular magnets⁶⁻¹⁰, which are solid-state systems with a large spin; their spin eigenstates make them natural candidates for single-particle systems. We show theoretically that molecular magnets can be used to build dense and efficient memory devices based on the Grover algorithm. In particular, one single crystal can serve as a storage unit of a dynamic random access memory device. Fast electron spin resonance pulses can be used to decode and read out stored numbers of up to 10^5 , with access times as short as 10^{-10} seconds. We show that our proposal should be feasible using the molecular magnets Fe_8 and Mn_{12} .

Thermally assisted Quantum Tunneling



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Quantum effects at the nanoscale ($S = 10$)



Break axial symmetry:

$$\hat{H} = D\hat{S}_z^2 + \hat{H}_T$$

$H_T \Rightarrow$ interactions which do not commute with \hat{S}_z

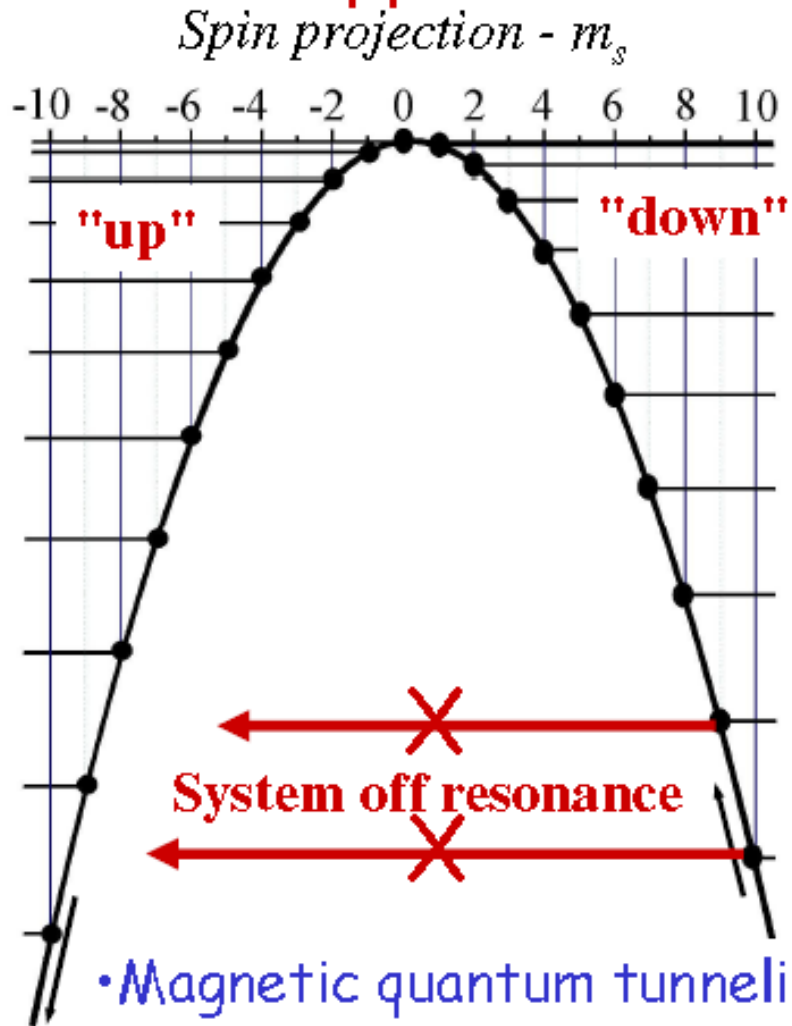
- m_s not good quantum #
- Mixing of m_s states
- \Rightarrow resonant tunneling (of m_s) through barrier
- Lower effective barrier

"down"



Applying a field : levels change (Zeeman effect)

Application of a magnetic field



$$\hat{H} = D\hat{S}_z^2 + \hat{H}_T + g\mu_B\vec{B} \cdot \hat{S}$$

$$\vec{B} \cdot \hat{S} \equiv B_x\hat{S}_x + B_y\hat{S}_y + \underbrace{B_z\hat{S}_z}_{\text{circled}}$$

Several important points to note:

- Applied field represents another source of transverse anisotropy
- Zeeman interaction contains odd powers of \hat{S}_x and \hat{S}_y

For now, consider only $B//z$:
(also neglect transverse interactions)

$$E(m_s) = -|D|m_s^2 + g\mu_B Bm_s$$

- Magnetic quantum tunneling is suppressed
- Metastable magnetization is blocked ("down" spins)

OFF
Res

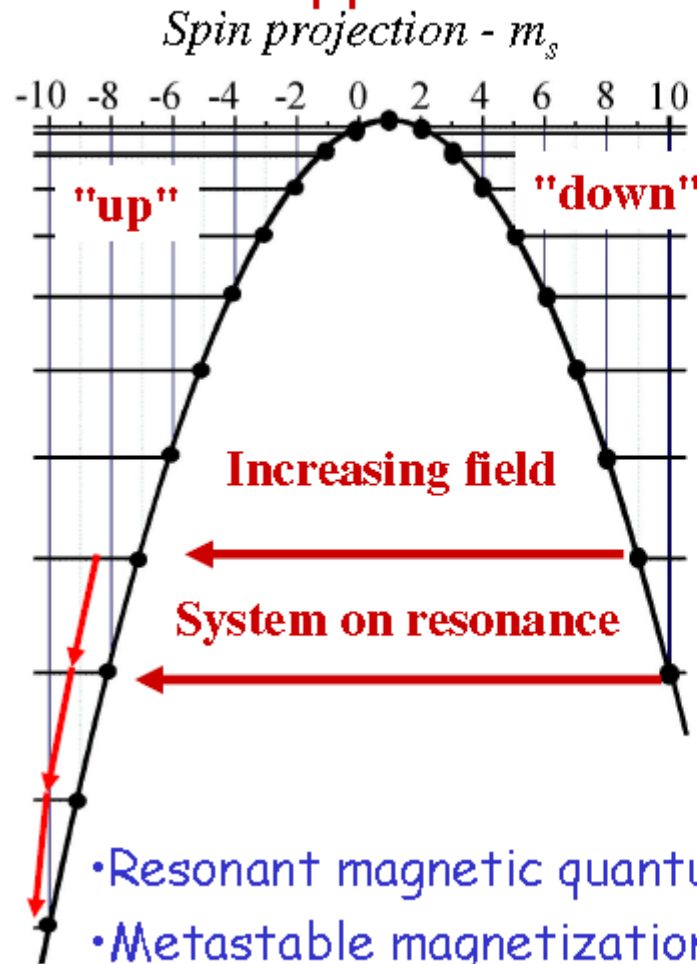
QTM
OFF

Applying a field : levels change (Zeeman effect)



Pavia, 07/06/16

Application of a magnetic field



$$\hat{H} = D\hat{S}_z^2 + \hat{H}_T + g\mu_B \vec{B} \cdot \hat{S}$$

$$\vec{B} \cdot \hat{S} \equiv B_x \hat{S}_x + B_y \hat{S}_y + B_z \hat{S}_z$$

Several important points to note:

- Applied field represents another source of transverse anisotropy.
- Zeeman interaction contains odd powers of \hat{S}_x and \hat{S}_y .

For now, consider only $B//z$:
(also neglect transverse interactions)

$$E(m_s) = -|D|m_s^2 + g\mu_B B m_s$$

- Resonant magnetic quantum tunneling resumes
- Metastable magnetization can relax from "down" to "up"

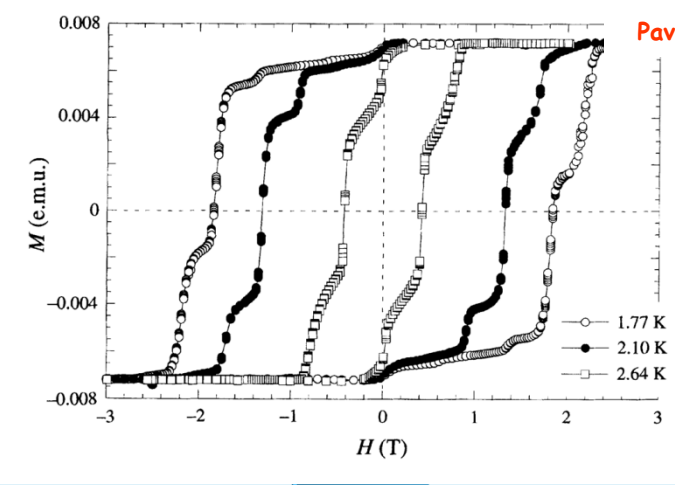
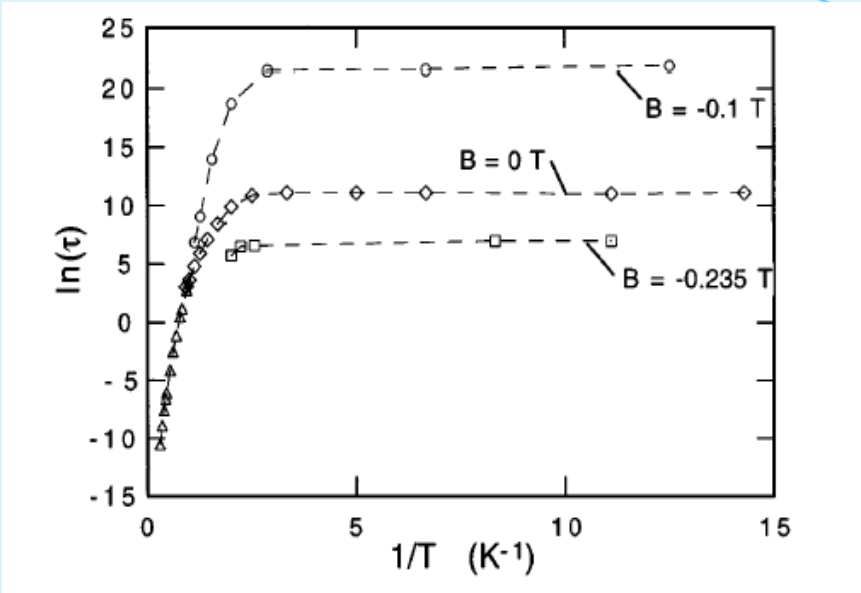
ON
Res

QTM
ON

EXPERIMENTAL EVIDENCES of QTM



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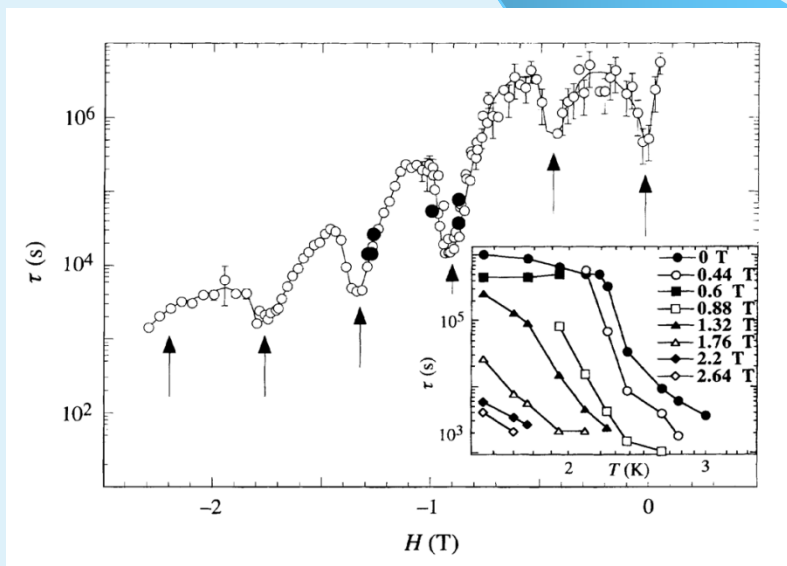


vertical steps for H_z values corresponding to the LA

the relaxation time becomes T-independent

Nature 383, 145.

appearance of step-like hysteresis loop of M



drop of the relaxation time in proximity of LA



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Quantum energy level crossing

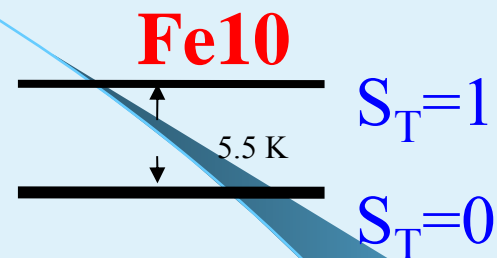
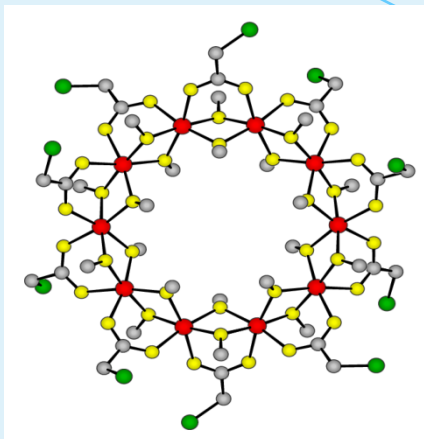
The $S_T=0$ homometallic ring-like systems



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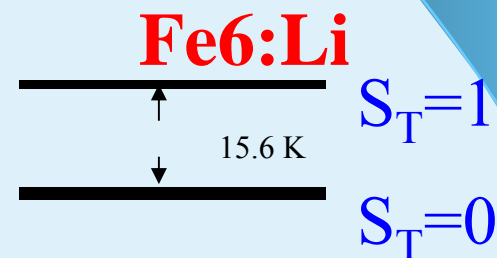
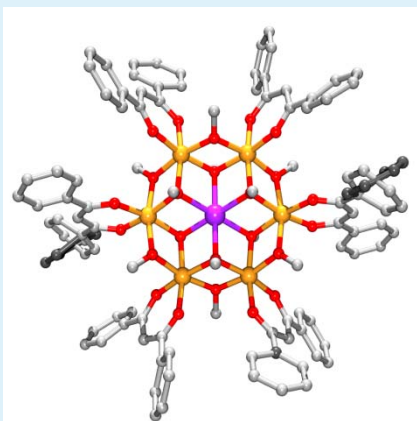
Fe(III) $s = 5/2$
AF ground state
(total spin $S_T = 0$)

$J \approx 13.8$ K
 $\Delta_{0 \rightarrow 1} \approx 5.5$ K



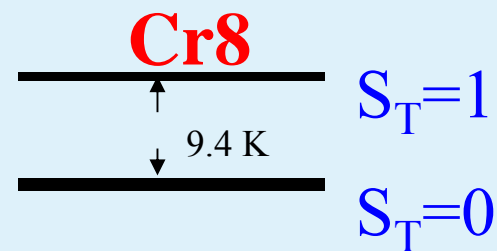
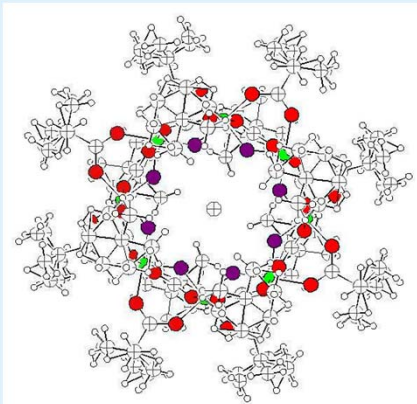
Fe(III) $s = 5/2$
AF ground state
(total spin $S_T = 0$)

$J \approx 21$ K
 $\Delta_{0 \rightarrow 1} \approx 15.6$ K



Cr(III) $s = 3/2$
AF ground state
(total spin $S_T = 0$)

$J \approx 17.2$ K
 $\Delta_{0 \rightarrow 1} \approx 9.4$ K



Hamiltonian - energy levels

Hamiltonian for **ring nanomagnets** :

$$\sum_i J \mathbf{s}_i \cdot \mathbf{s}_{i+1} + \sum_i U(\mathbf{s}_i) + \sum_{ij} U_{i,j}(\mathbf{s}_i, \mathbf{s}_j) + g \mu_B \mathbf{B} \cdot \sum_i \mathbf{s}_i$$

$U(\mathbf{s}_i)$ = crystal field anisotropies

$U_{i,j}(\mathbf{s}_i, \mathbf{s}_j)$ = intramol. dipolar interactions, hyperfine couplings, D-M interact., higher order exch., etc.

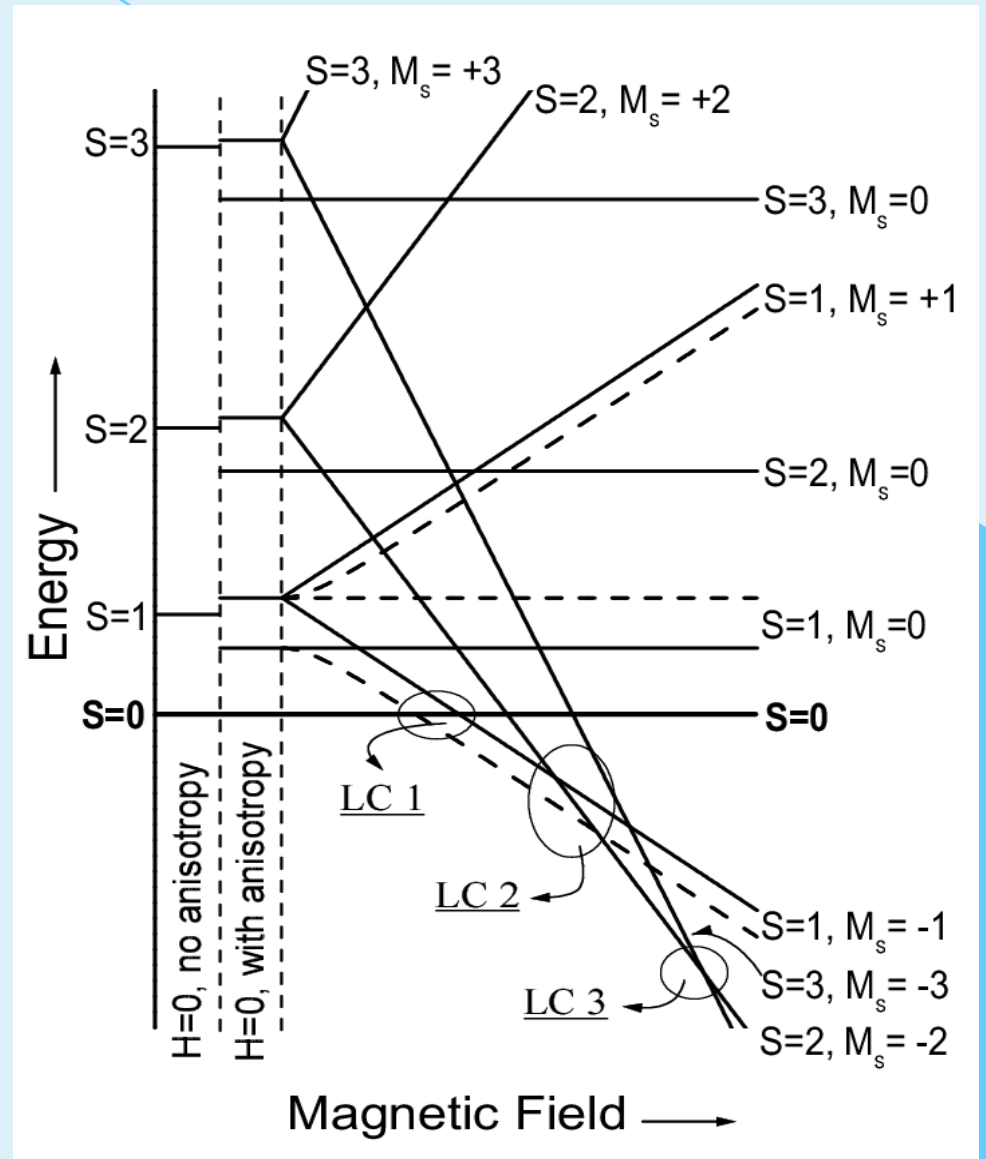
Approximate energy levels (Landè rule) :

$$E(S_{TOT}) = P/2 S_{TOT} (S_{TOT} + 1) \quad P = 4 J / N$$

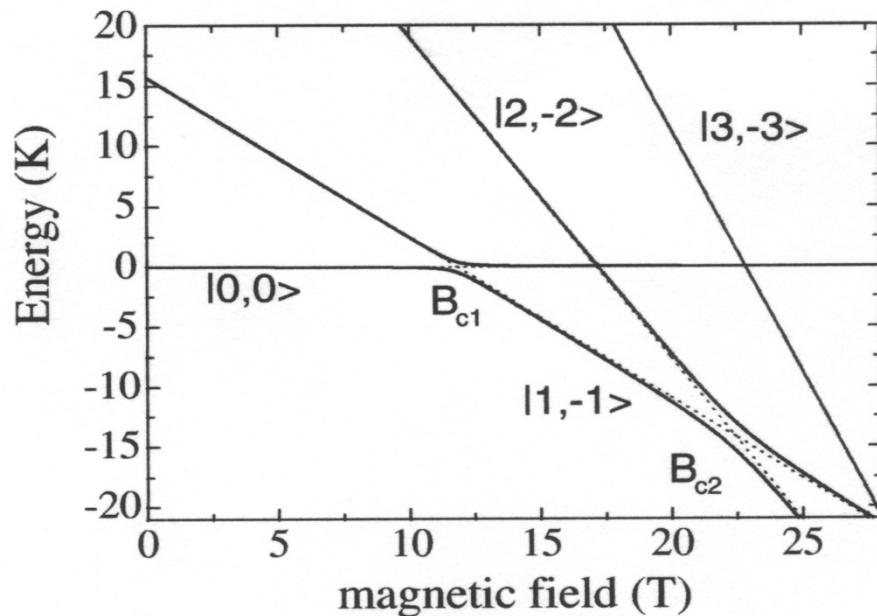
N = number of magnetic ions in the ring

- Level crossing fields depend on the angle θ between field and molecular axis z
- **POSSIBLE LEVEL REPULSION AT CROSSING FIELDS (LEVEL ANTICROSSING)**

Diagram of energy levels (scheme)



ANTICROSSING OR AVOIDED LEVEL CROSSING (ALC)



ALC means mixing of wave-functions of two different levels

example case of energy levels of Fe6:Li

IN SOME RINGS THERE IS EXPERIMENTAL EVIDENCE FOR LEVEL REPULSION AT CROSSING FIELDS (ALC).

Questions (experimental) on fundamental structure of levels arise :

- 1) How can we distinguish LC from ALC ?**
- 2) What is the “value” of ALC, i.e. the “gap” at the crossing ?**
- 3) How (if) levels’ lifetime affects the degree of ALC ?**
- 4) Does any other quantum effect (e.g. QT of the Neel vector, QTNV in brief) occurs, especially near ALC or LC ?**

Macroscopic probes (magnetization , EPR, specific heat,....) help , but give not definitive answers

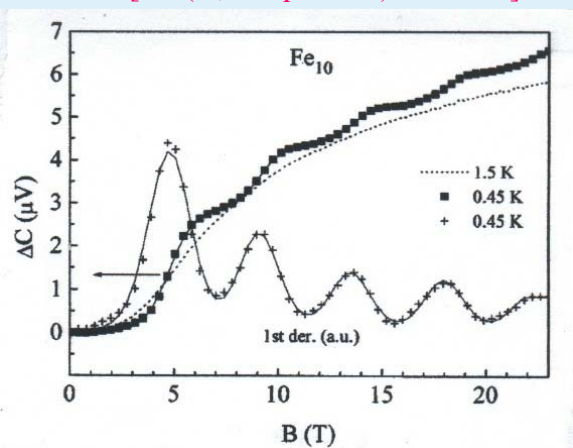


Evidences for ground state spin change & LC/LAC : torque and specific heat on single x-tals

1) Peaks of dM/dH at crossing fields ; 2) Plateaus in $M(H)$ corresponding to $S=0, 1, 2, \dots$ states

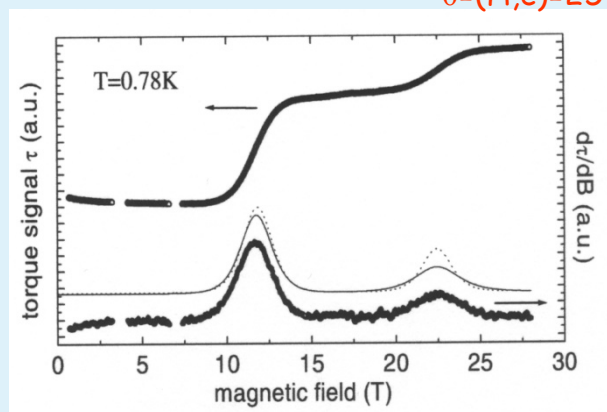
Ferric wheel Fe_{10}

[$\vartheta(H, \text{unique axis}) = 49.8^\circ$]

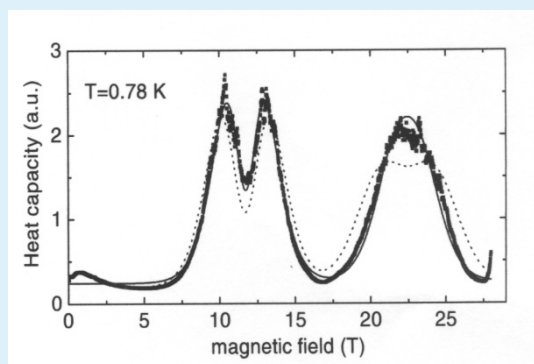


$Fe_6:Li$

$\theta=(H,c)=25^\circ$

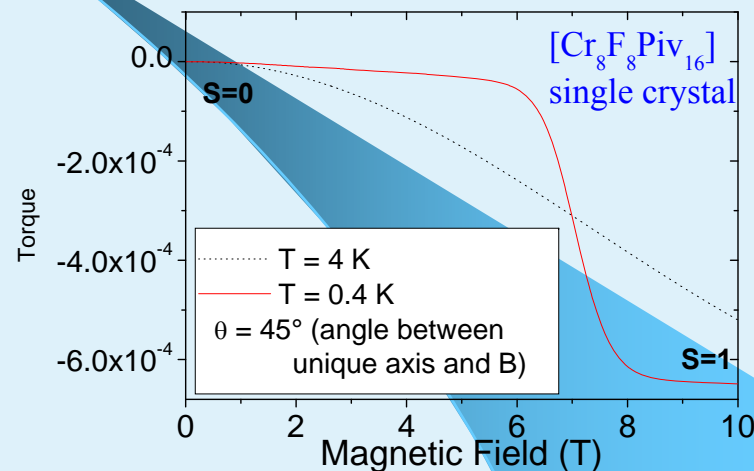


SPECIFIC HEAT

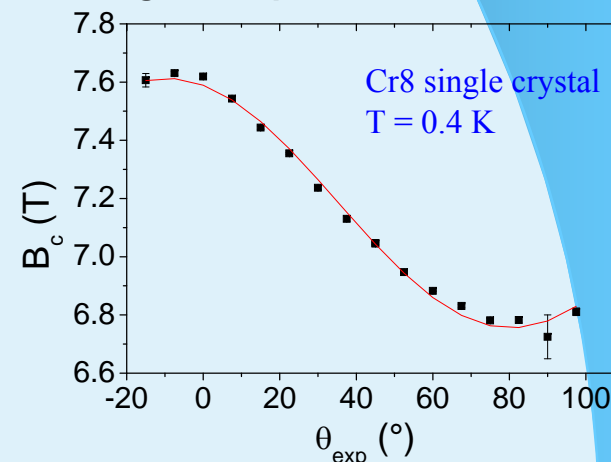


⇒ Level anti-crossing (LAC)

$Cr_8(Piv)_{16}$



• Angular dependence of the crossing field

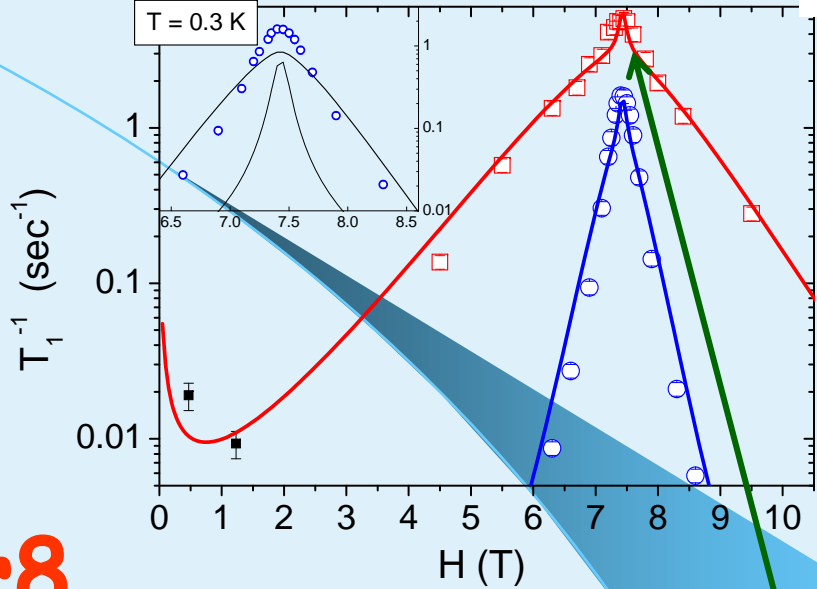
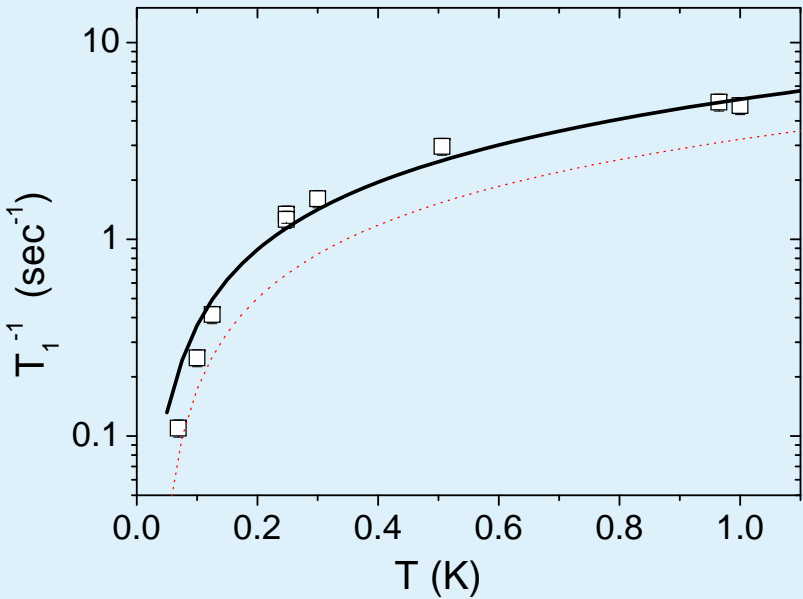


• From specific heat : very small LAC

1H NMR on Cr8 . T ≤ 1K



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Cr8

$$T_1^{-1} = A^2 \left\{ \frac{e^{-\frac{\Delta}{T}}}{1 + e^{-\frac{\Delta}{T}}} \right\} \frac{\Gamma_1}{\Gamma_1^2 + \omega_N^2} + B^2 \frac{\Gamma_2}{\Gamma_2^2 + (\hbar\omega_L - \Delta)^2}$$

$$\Delta = \sqrt{[g\mu_B (H_{c1} - H)]^2 + \Delta_1^2}$$

Quasi-elastic Inelastic

Cross. Field
H_{c1}

Fit parameters :
 $\Delta_1 = 0.10 (5) \text{ K}$, $A^2 = 9 (1) \cdot 10^{13} \text{ rad}^2 \text{ Hz}^2$, $B^2 = 7 (1) \cdot 10^{13} \text{ rad}^2 \text{ Hz}^2$,
 $\Gamma_1 = 4.0(3) \cdot 10^4 \text{ H T rad Hz}$, $\Gamma_2 = 4.0(6) \cdot 10^6 \text{ T rad Hz}$

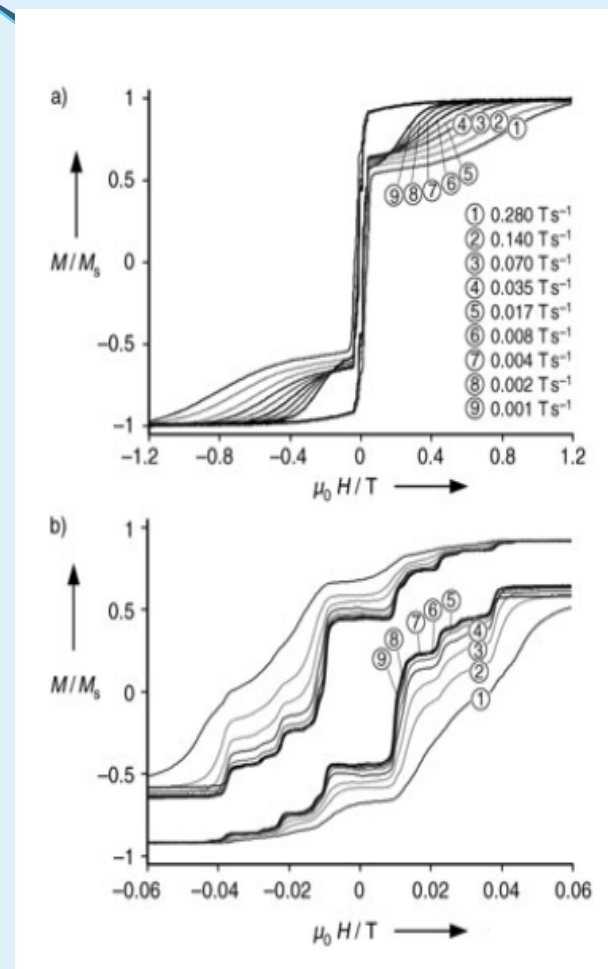
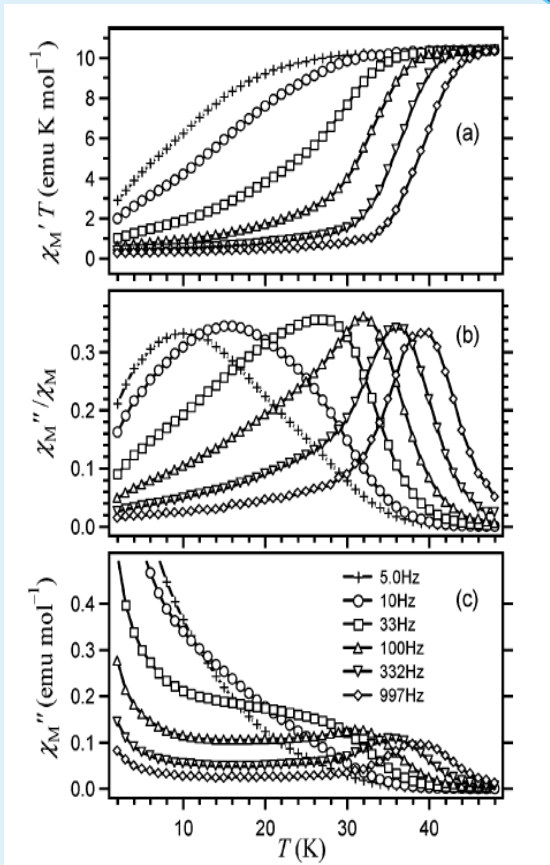
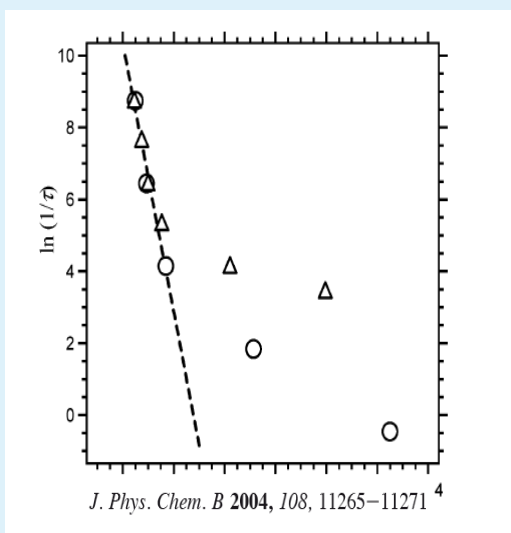
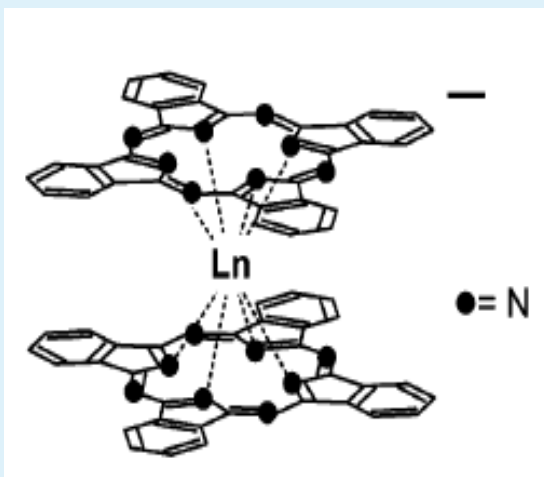
The **H** and **T** dependences are due to direct, Raman or Orbach processes ? Between nuclei and phonons or electrons and phonons ? Does QTNV play any role ?



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Looking for high anisotropy barrier
For having e.g. room temperature
Storage memories

High anisotropy Single ion Magnets: Tb-double deckers of phtalocyanines



AC susceptibility

hysteresis

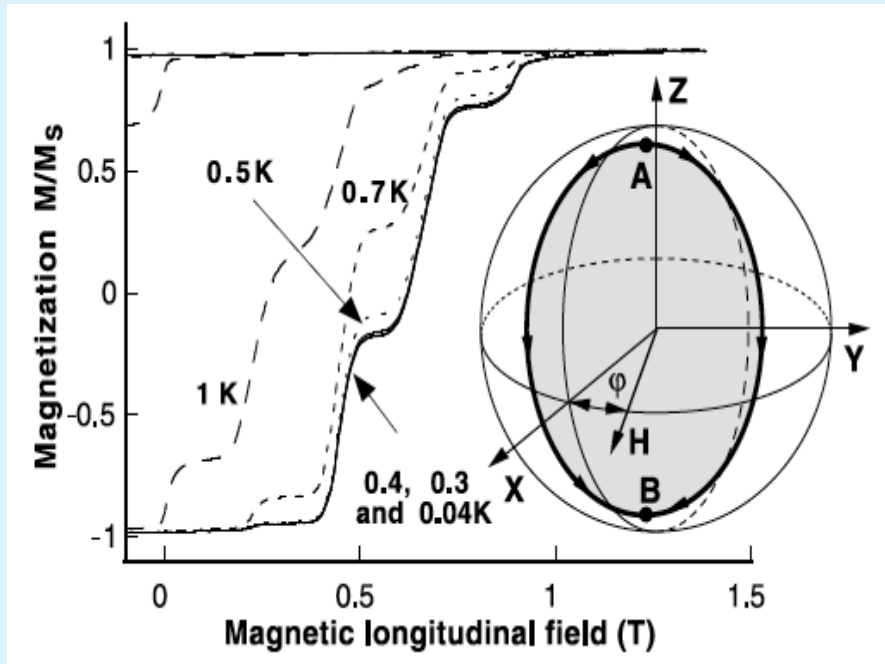
**Tb³⁺ (J=6)=
U_{eff}/k_B=80K**



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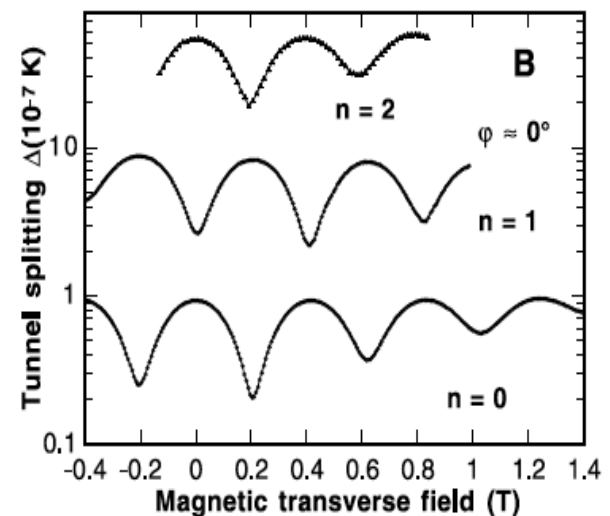
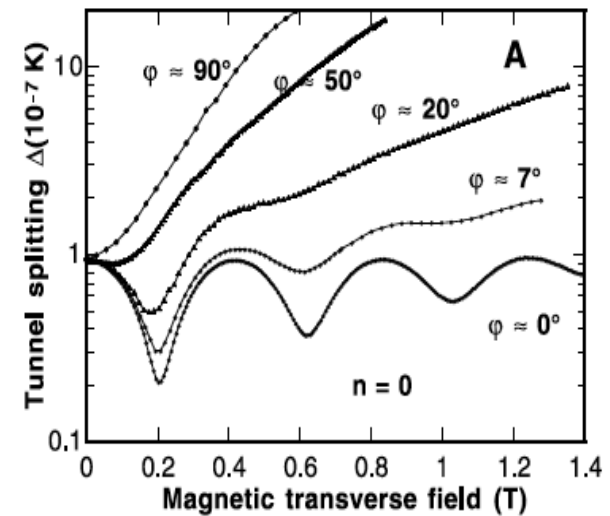
Other quantum effects

Quantum phase interference (Berry phase)



SCIENCE VOL 284 2 APRIL 1999

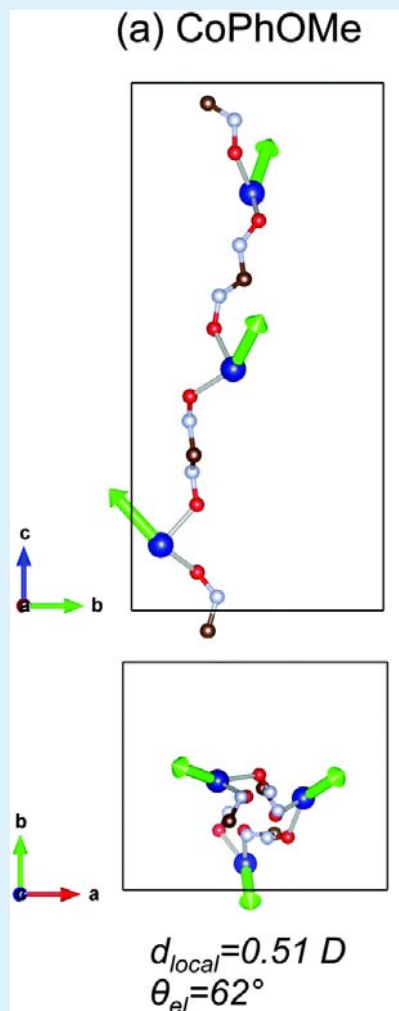
$$P = 1 - \exp\left[-\frac{\pi\Delta^2}{4\hbar g\mu_B S dH/dt}\right]$$



Glauber dynamics of spin chain

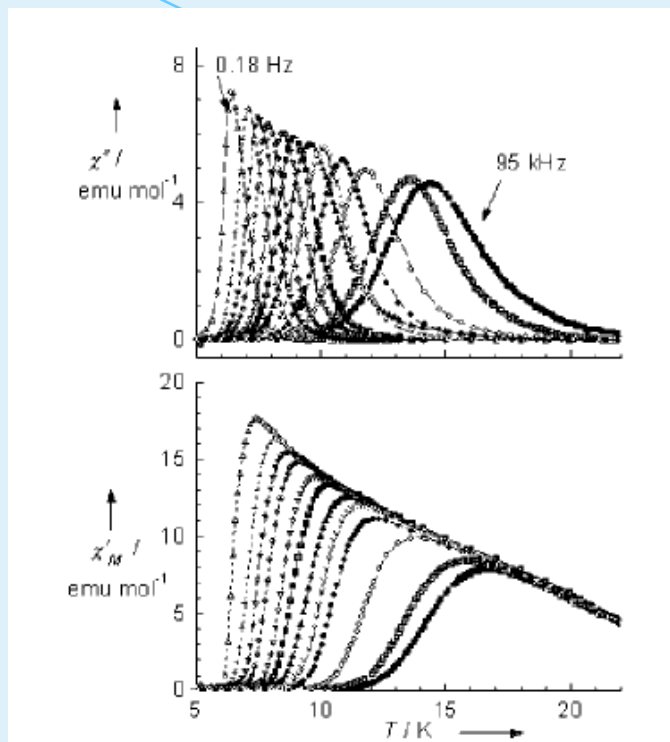


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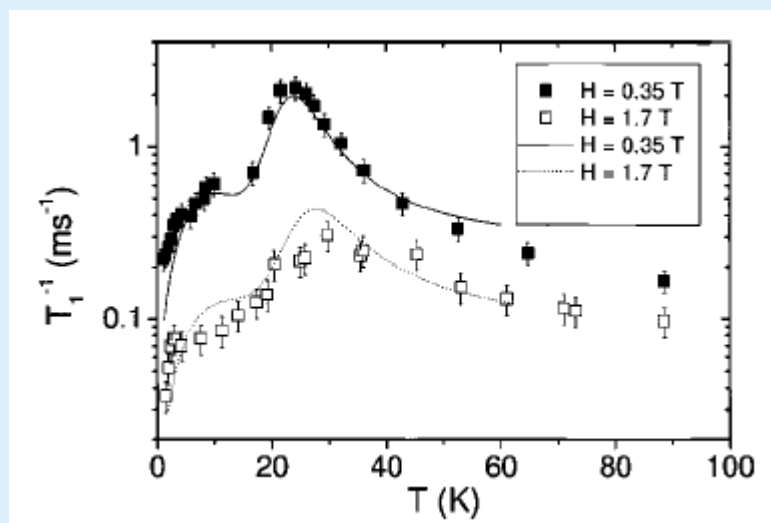


Single chain magnets

Angew. Chem. Int. Ed. 2001, 40, No. 9

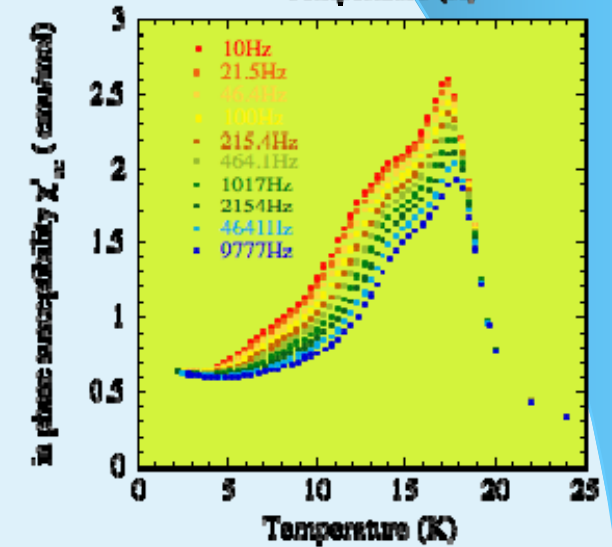
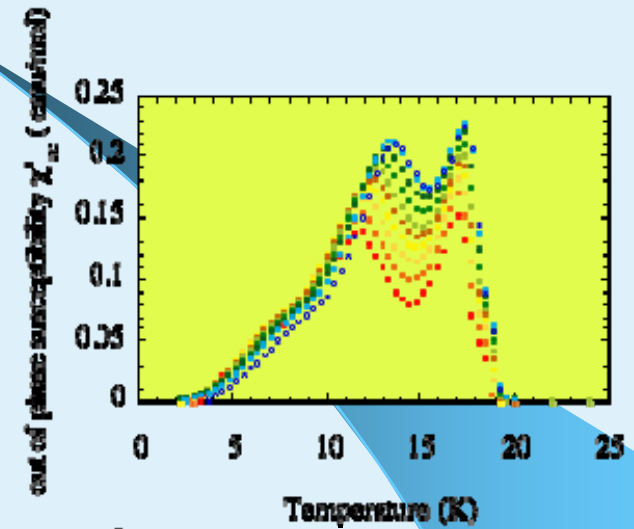
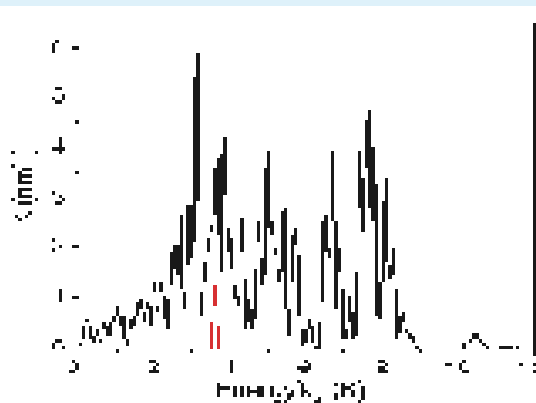
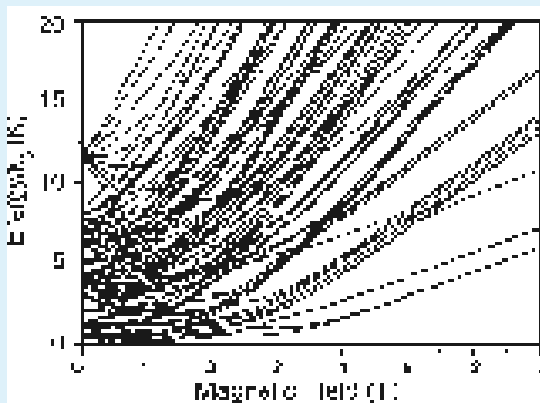
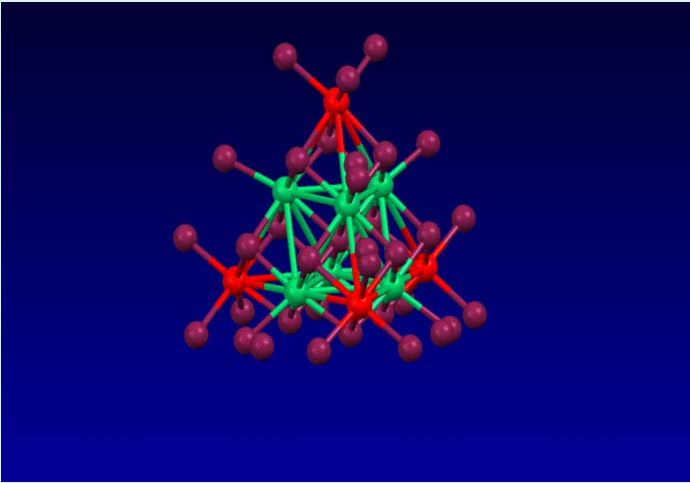


AC susceptibility



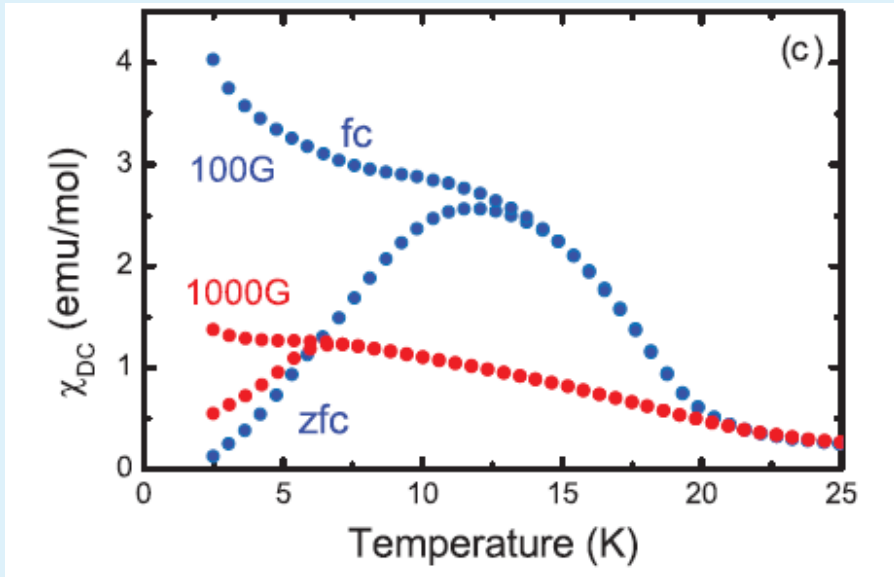
NMR

Phonon trapping in Ni10

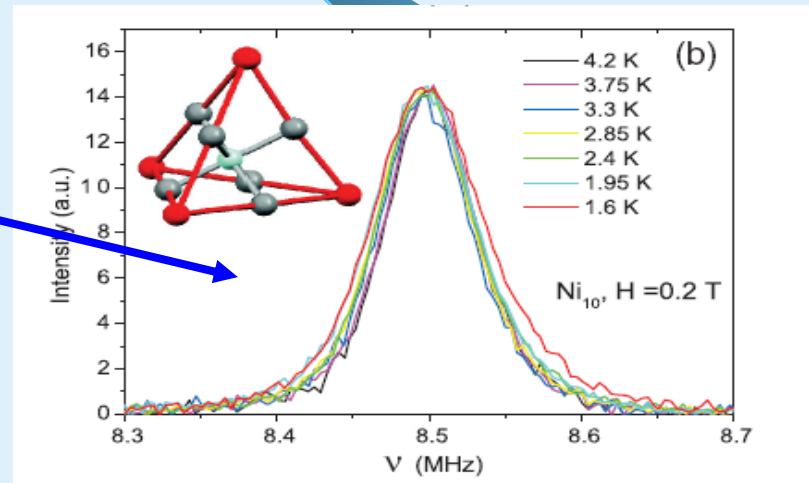


Nonequilibrium Dynamics in Ni10 powders

From SQUID : slowing down of M,
i.e. **non equilibrium** situation

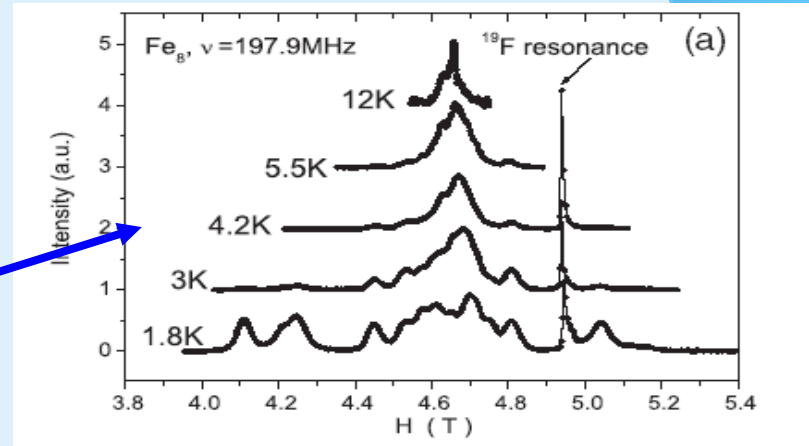


From NMR : narrow line
(FWHM ~ 100 KHz) i.e.
no local field due to “giant” S



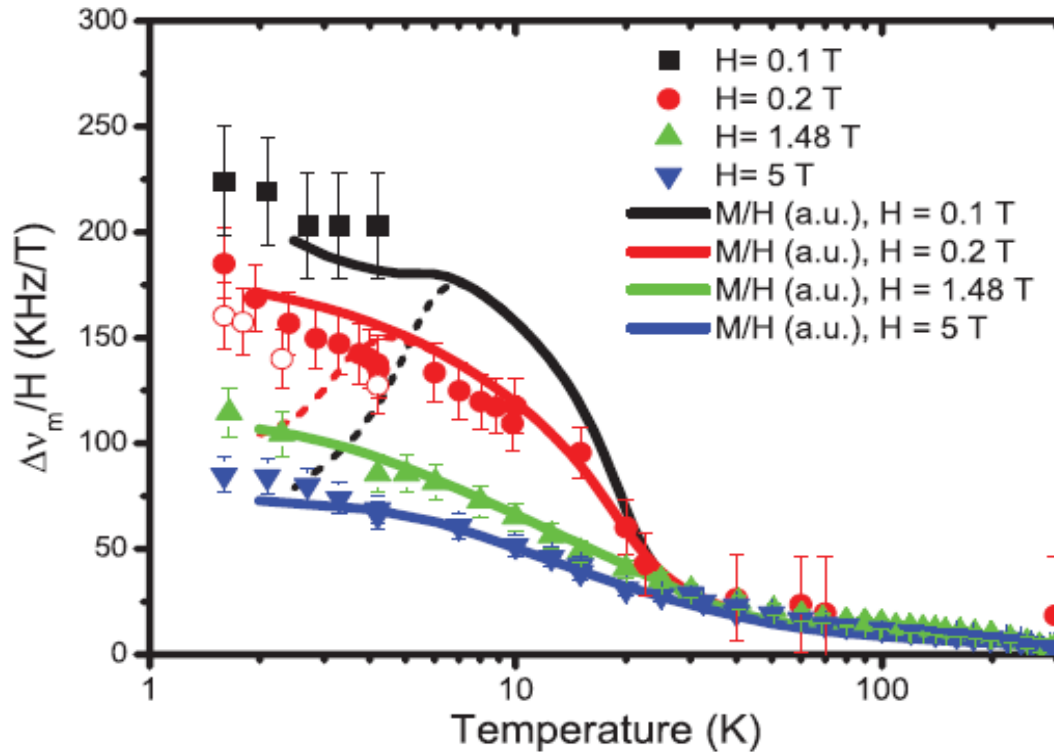
Ni10

For comparison : Fe8



Solution : resonant phonon trapping

Phonons are no more a heat bath but the joint dynamics of spin+phonons dominates
 (phonons populations n_{ph} are not fixed solely by thermostat temperature)



Points : NMR
 Lines : SQUID

$$\Delta \nu_{\text{tot}}^2 = \Delta \nu_d^2 + \Delta \nu_m^2$$

$$\Delta \nu_m^2 = \sum_R \sum_{i \in R} (\langle \nu_{R,i} - \nu_0 \rangle_{\Delta t})^2 / N$$

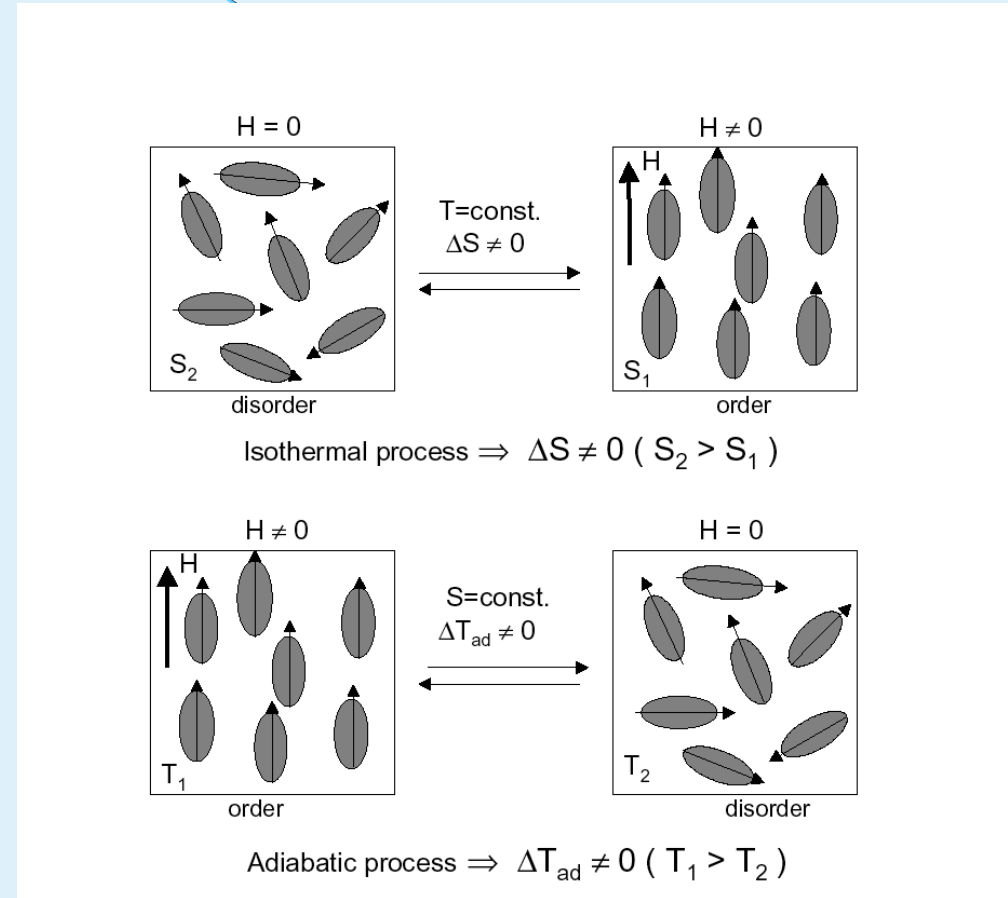
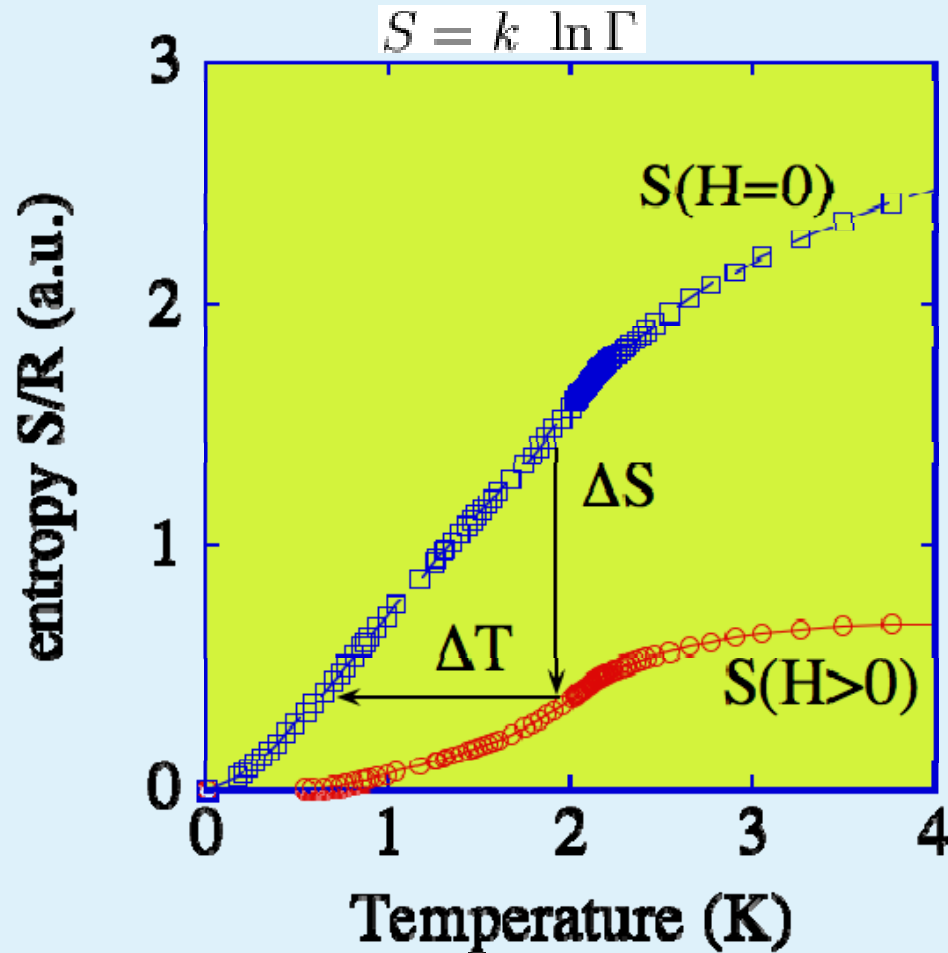
$$\sum_{i \in R} (\langle \nu_{R,i} - \nu_0 \rangle_{\Delta t})^2 \simeq \gamma^2 \sum_{i \in R} \left[\sum_{j \in R} \frac{A(\theta_{i,j})}{r_{i,j}^3} \langle m_{z,j} \rangle_{\Delta t} \right]^2$$

- (i) The dependence of $\langle m_{z,j} \rangle_{\Delta t}$ on j is weak and can be neglected
- (ii) The average molecular magnetization over Δt is nearly homogeneous

→

$$\Delta \nu_m^2 = \gamma^2 \sum_R [\langle \mu_z \rangle_{\Delta t}]^2 A / N = BM^2$$

Magnetocaloric effect: entropy of a magnetic system



The MagnetoCaloric Effect (MCE) is the adiabatic temperature change of a material upon application of a magnetic field



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Entropy and MCE for Magnetic nanoparticles

classical case

$$Z = \left[4\pi \frac{kT}{mH} \sinh\left(\frac{mH}{kT}\right) \right]^N,$$

$$\begin{aligned} S_C &= - \frac{\partial(kT \ln Z)}{\partial T} \\ &= Nk \left[\ln(4\pi) + \ln\left(\sinh\left(\frac{mH}{kT}\right) / \left(\frac{mH}{kT}\right)\right) \right. \\ &\quad \left. + 1 - \frac{mH}{kT} \coth\left(\frac{mH}{kT}\right) \right]. \end{aligned} \quad (5)$$

$$\Delta S_C \approx \frac{-Nm^2H^2}{6kT^2} = \frac{-mM_0H^2}{6kT^2}.$$

quantum case:

$$Z = \sum_{m=-J}^J e^{-m\mu_B H / kT}$$

$$S = k_B \ln(ZJ + 1)$$

$$\Delta S_Q = - \frac{Ng^2\mu_B^2 J(J+1)H^2}{6kT^2}.$$

McMichael et al.

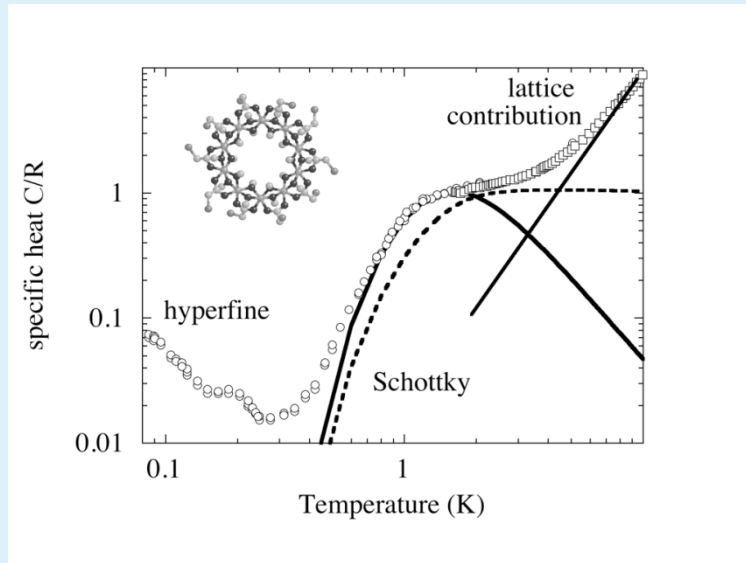
Journal of Magnetism and Magnetic Materials 111 (1992) 29–33

Scripta Materialia 46 (2002) 89–94

Determination of MCE from experiments



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$$\Delta S = \frac{Q_{rev}}{T}$$

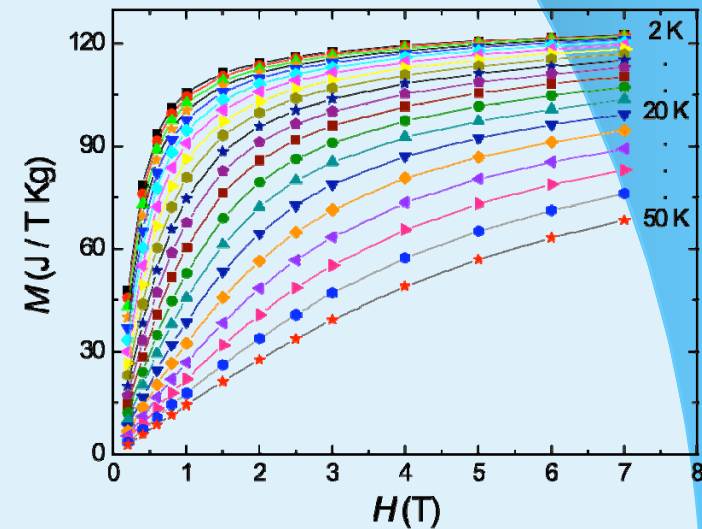
$$\int_A^B \left(\frac{\delta Q}{T} \right)_{rev}$$

from specific heat data:

$$S(T)_H = \int_0^T \frac{C(T)_H}{T} dT.$$

from magnetization data:

$$\Delta S_{m2}(T)_{\Delta H} = \int_{H_2}^{H_f} \left(\frac{\partial M(T, H)}{\partial T} \right)_H dH.$$





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MCE - a comparison

| | $\otimes \Sigma$ ($\mathcal{G}/K\gamma K$) | T(K) | ΔH (T) |
|----------------|--|-----------|--------------------|
| inter-metallic | ~ 3 | $< 10K$ | $3T \rightarrow 0$ |
| Mn12 | ~ 3 | $\sim 3K$ | $7T \rightarrow 0$ |
| Mn10 | 12 | 2K | $3T \rightarrow 0$ |
| Fe14 | 4 | 6K | $7T \rightarrow 0$ |
| PBA | 1 | 200K | $3T \rightarrow 0$ |
| Mn32 | 15 | 18 | $3T \rightarrow 0$ |
| Gd2 | 40 | 2K | $7T \rightarrow 0$ |

Recent theoretical study(2013) on MCE



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- By explicitly considering Carnot refrigeration cycles, we theoretically show that the best molecules for magnetic refrigeration between $T = 10\text{K}$ and the sub-Kelvin region are **those made of strongly ferromagnetically coupled magnetic ions**, contrarily to the established belief. (E. Garlatti et al, APPLIED PHYSICS LETTERS 103, 202410 (2013))

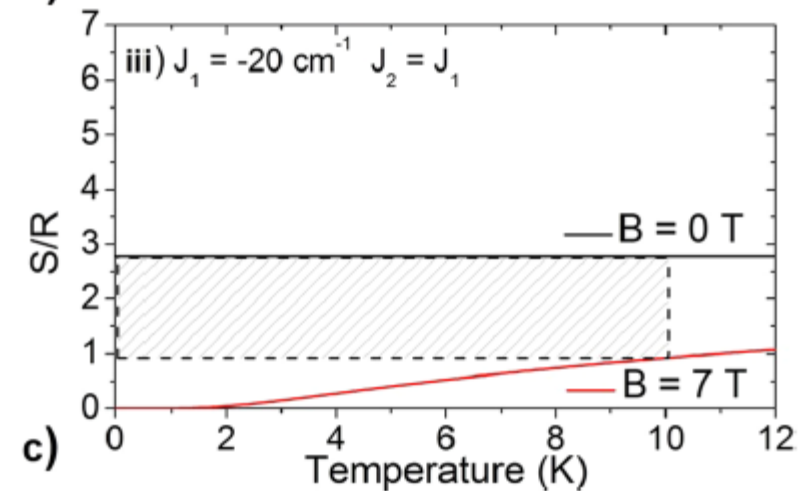
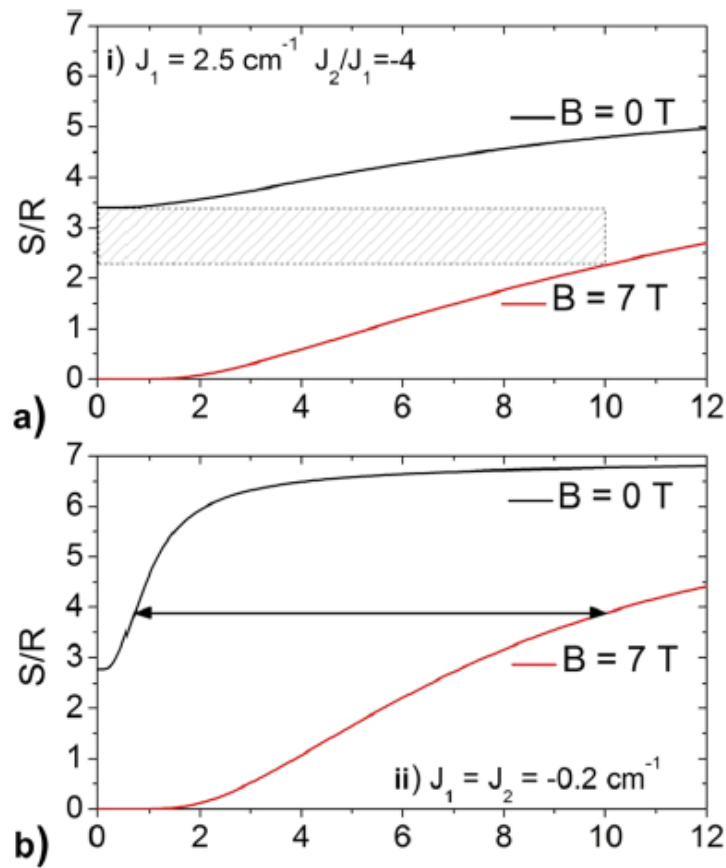
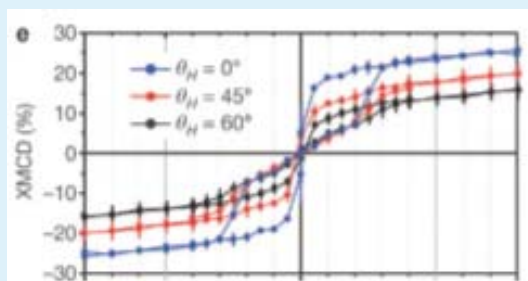
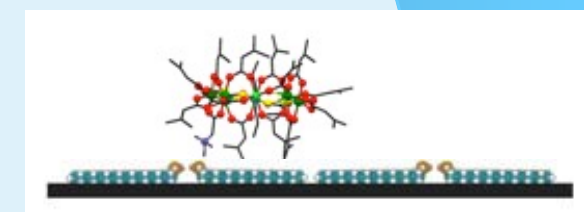
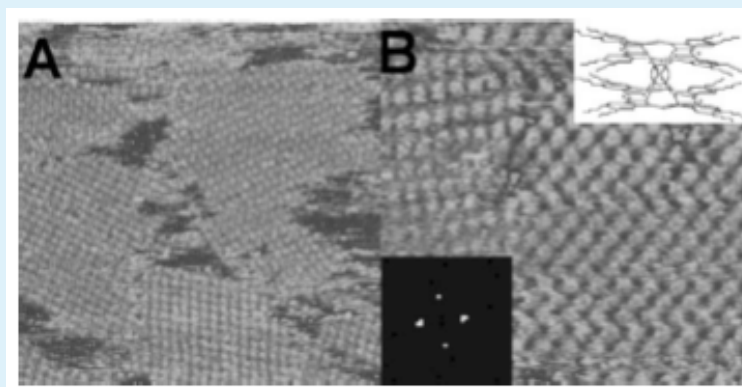
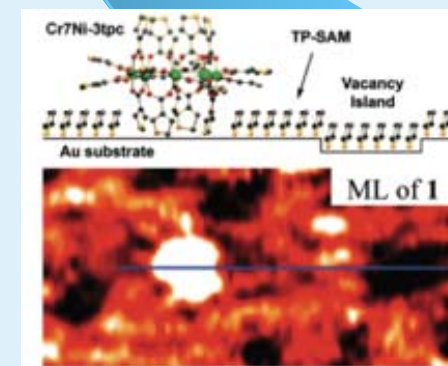
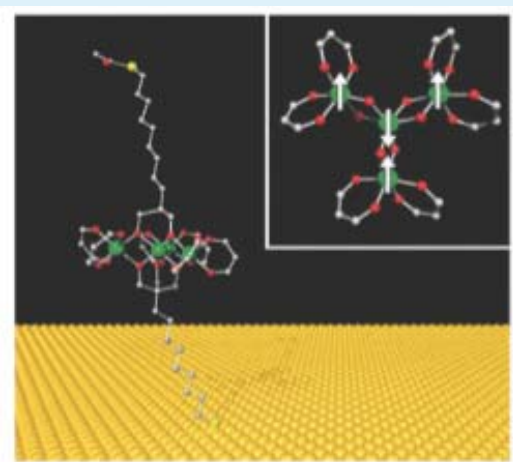
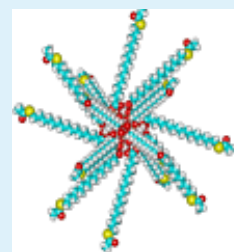
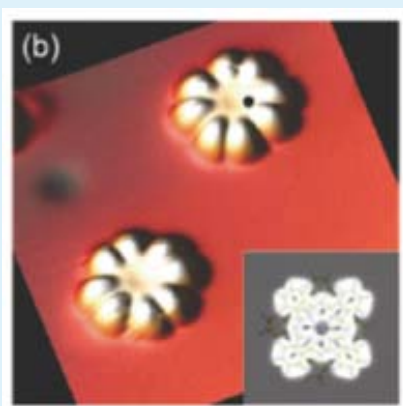
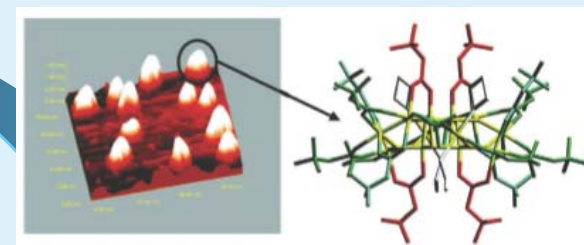
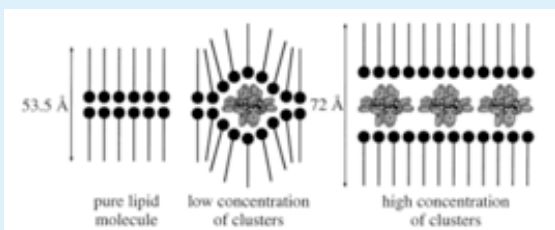


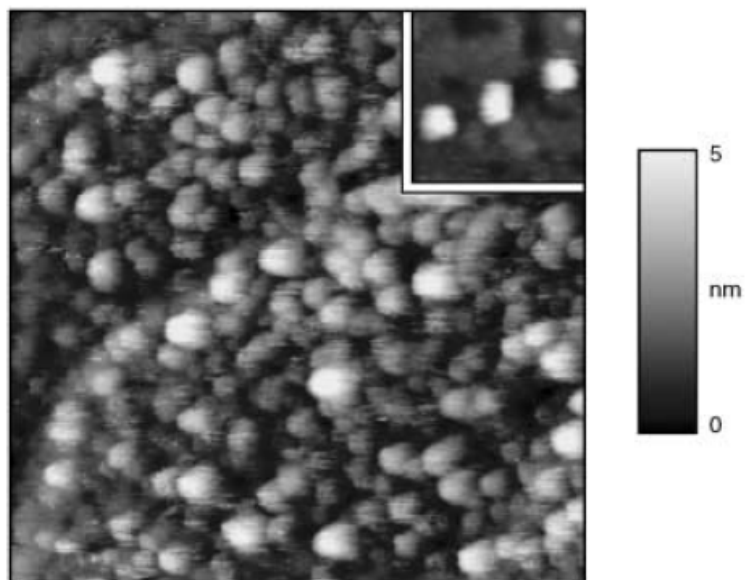
FIG. 4. $S(T)$ curves for cases (i) (panel (a)), (ii) (panel (b)) and (iii) (panel (c)) with $B = 0 \text{ T}$ and $B = 7 \text{ T}$. The shaded areas in panel (a) and (c) represent the best Carnot cycles with $T_{\text{cold}} = 1 \text{ mK}$ and $T_{\text{hot}} = 10 \text{ K}$. The horizontal arrow in panel (b) shows that for case (ii) it is not possible to build a closed Carnot cycle able to reach $T_{\text{cold}} = 1 \text{ mK}$ from $T_{\text{hot}} = 10 \text{ K}$.

Magnetic Molecules on surfaces

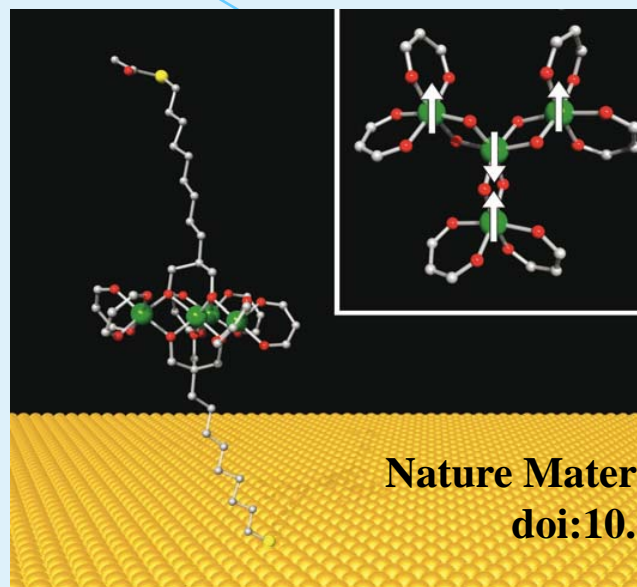
Single molecule read and write



Sunset of Mn12 & sunrise of Fe4

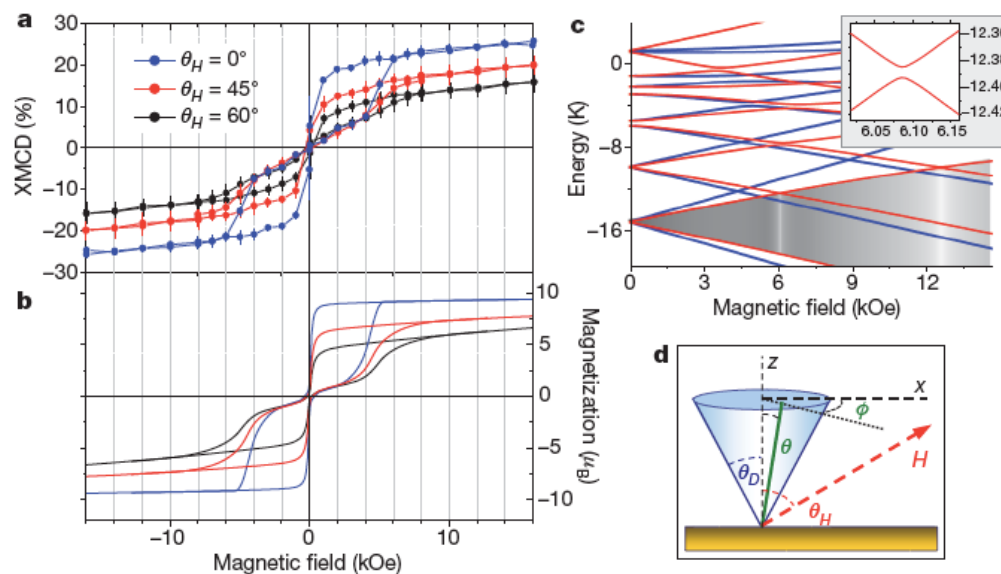


Angew. Chem. Int. Ed. 2003, 42, 1645–1648



Nature Materials 8, 194 - 197 (2009)
doi:10.1038/nmat2374

doi:10.1038/nature09478





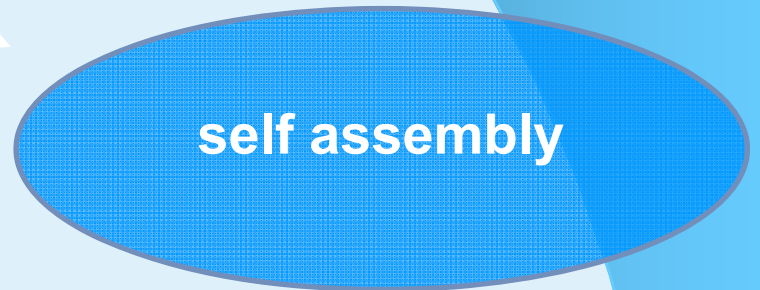
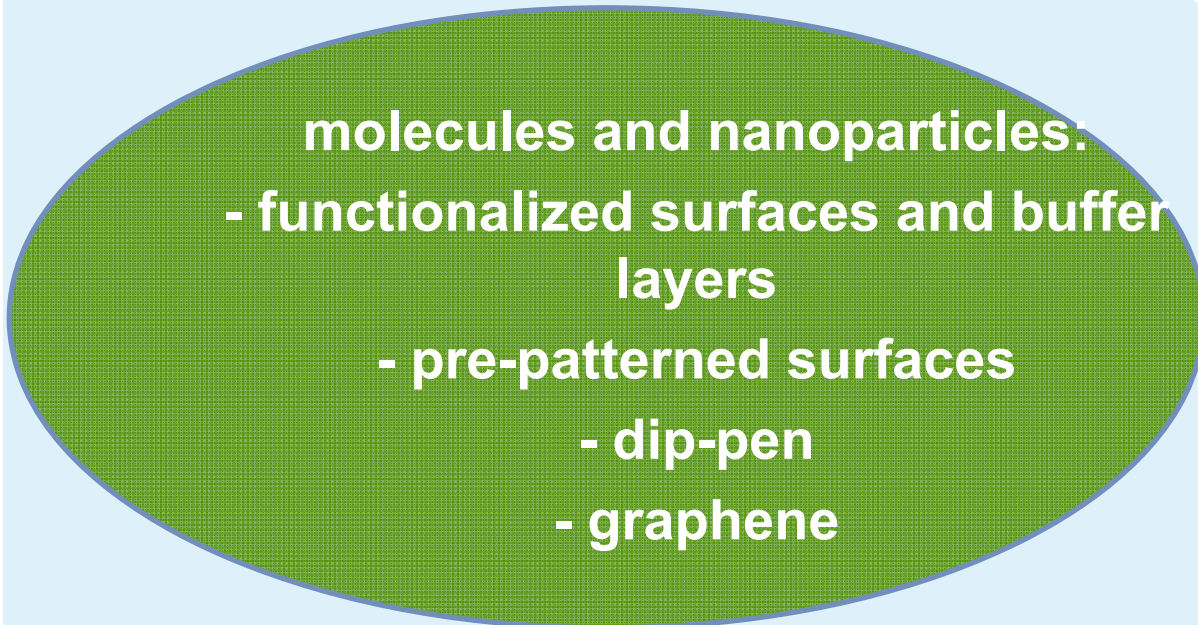
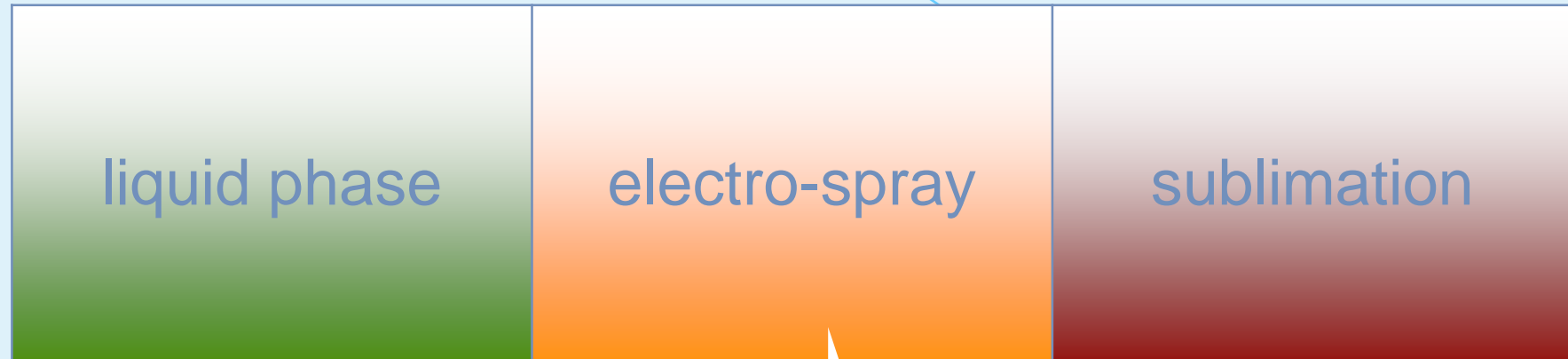
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Methods of deposition

air

high vacuum

ultra-high vacuum

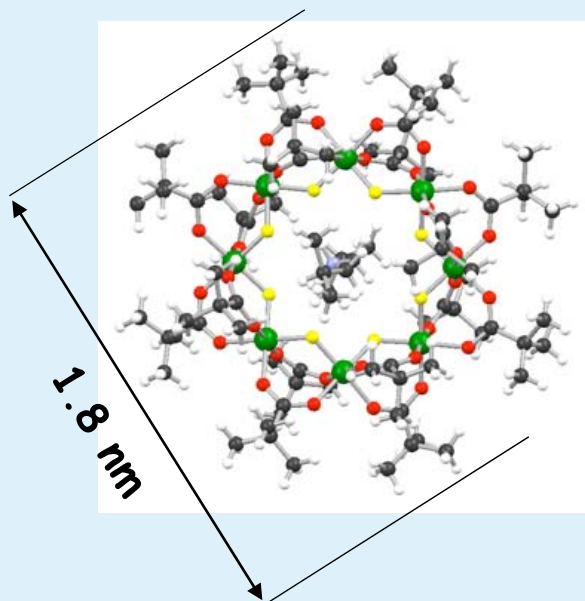


Integrity checks (also magnetic properties)

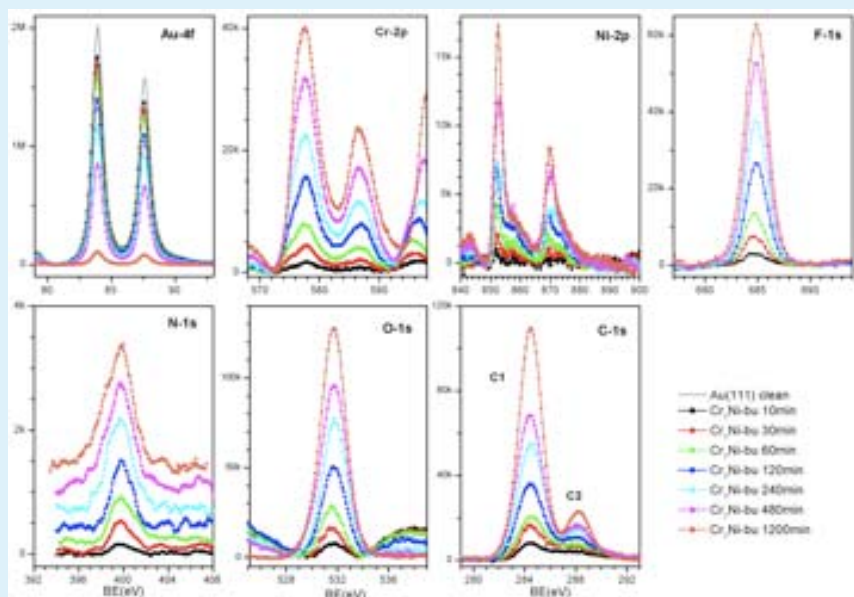
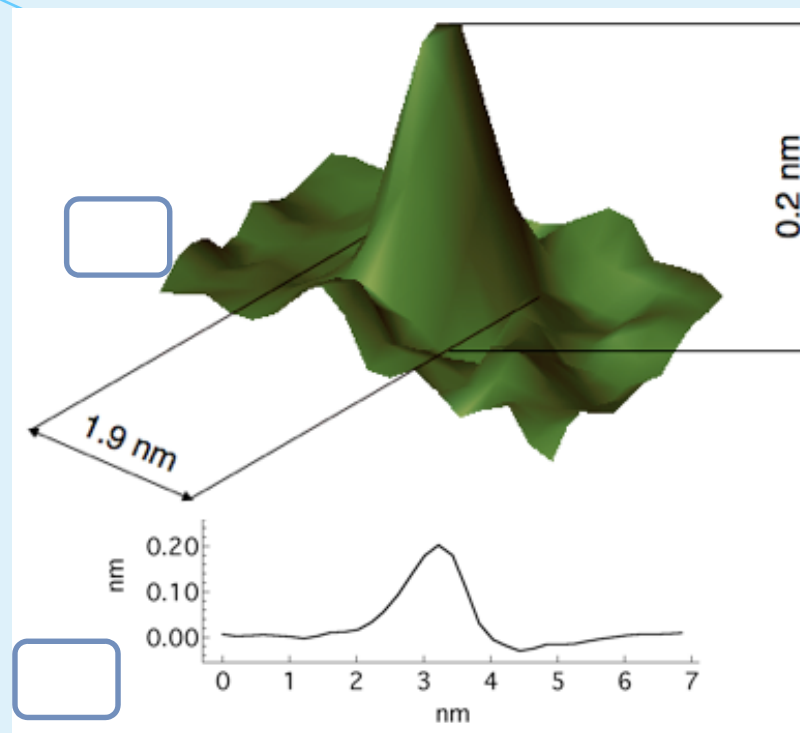


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surface



STM: lateral size as expected



| Derivative | Cr-2p/Ni-2p | F-1s/Cr-2p | N-1s/ 7Cr-2p | S-2p/ 7Cr-2p | O-1s/ 7Cr-2p | C-1s/7Cr-2p |
|--------------|---------------|-----------------|-----------------|-----------------|--------------|------------------|
| | [7.0] | [1.14] | [1] | [1] | [32] | |
| Cr7Ni-bu | 7.2 ± 0.5 | 1.17 ± 0.05 | 1.10 ± 0.15 | - | 29 ± 5 | 90 ± 15 [88] |
| Cr7Ni-thiobu | 6.8 ± 0.5 | 1.13 ± 0.05 | 0.90 ± 0.15 | 1.00 ± 0.15 | 30 ± 5 | 95 ± 15 [86] |

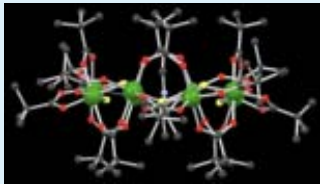
XPS: stoichiometric elemental ratios are respected

Self-assembly!

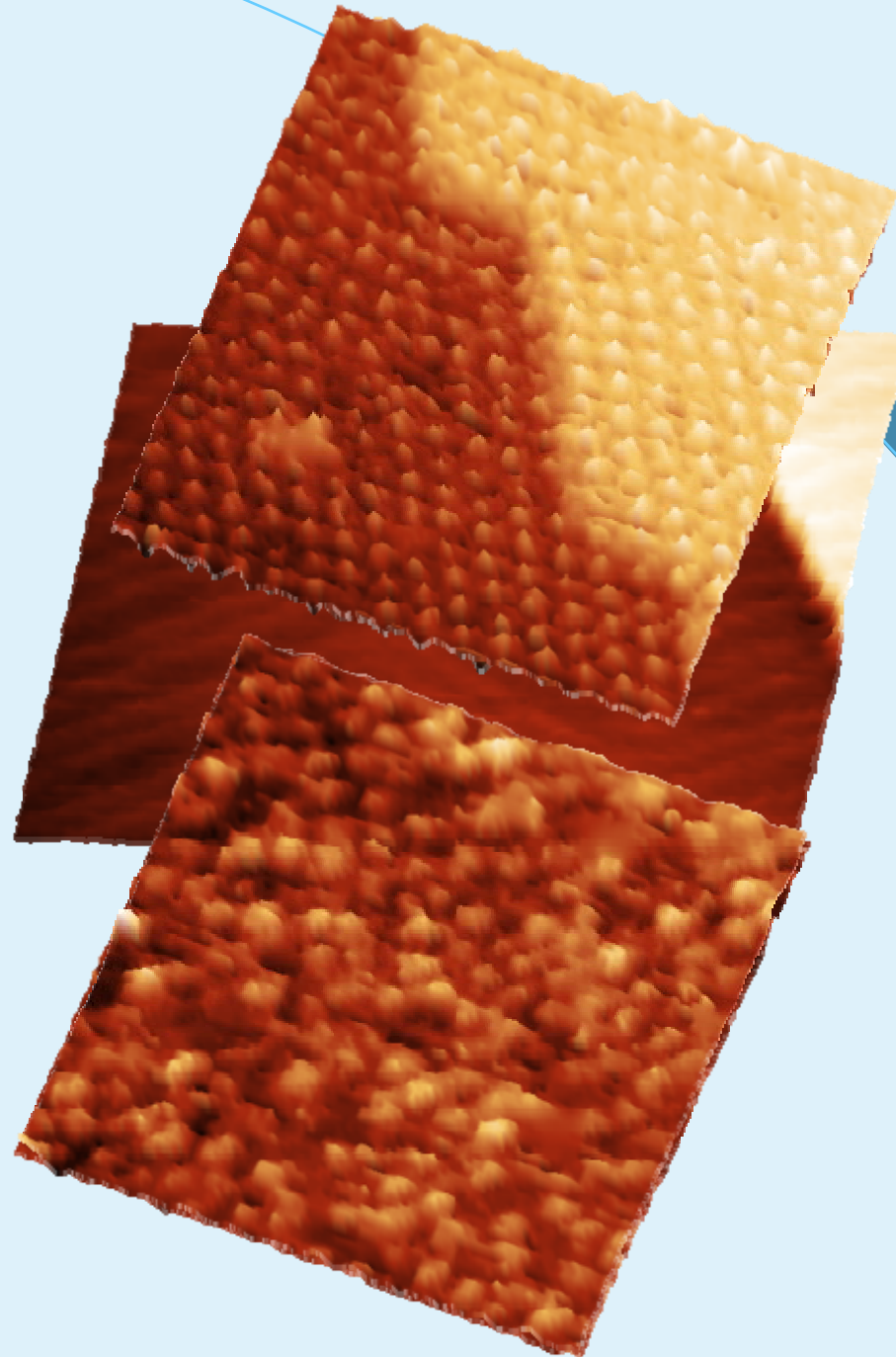
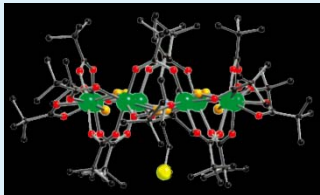


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Cr₇Ni-bu



Cr₇Ni-thiobu



monolayer

Recently addressing Fe₄ molecules



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Here, we probe electrical transport through individual Fe₄ SMMs using a scanning tunnelling microscope at 0.5 K. Correlation of topographic and spectroscopic information permits identification of the spin excitation fingerprint of intact Fe₄ molecules. Building from this, we find that the exchange coupling strength within the molecule's magnetic core is significantly enhanced.

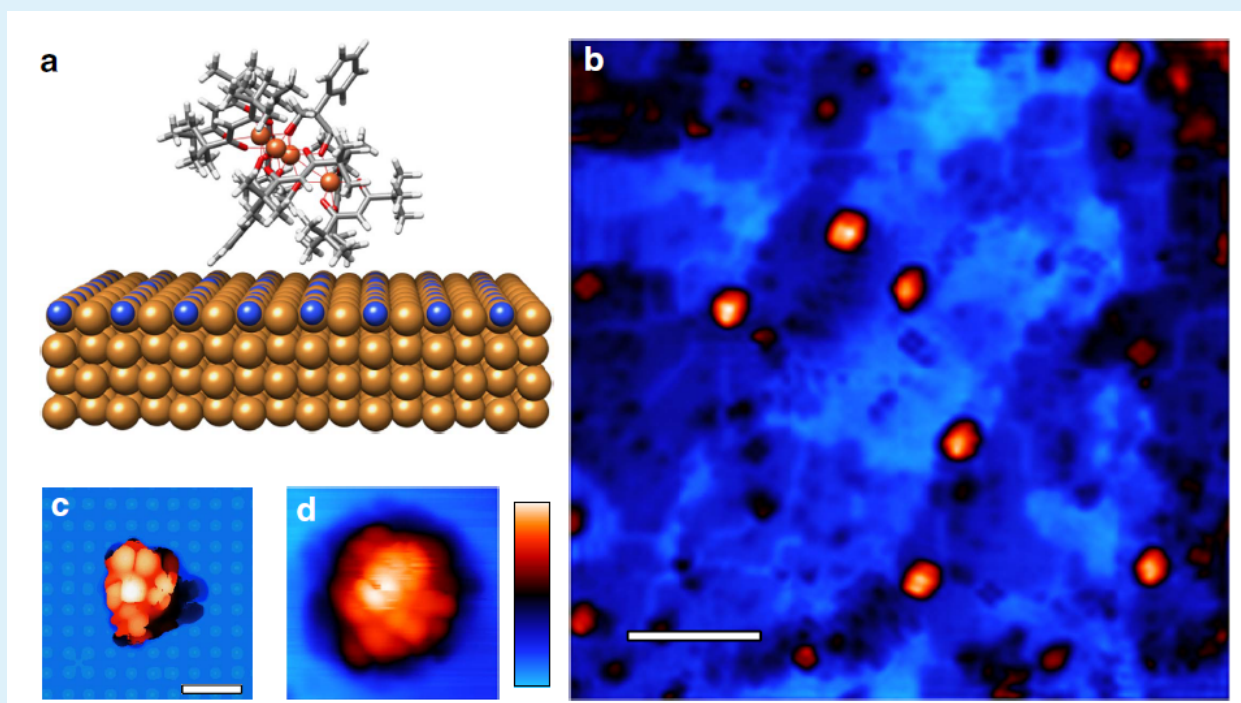
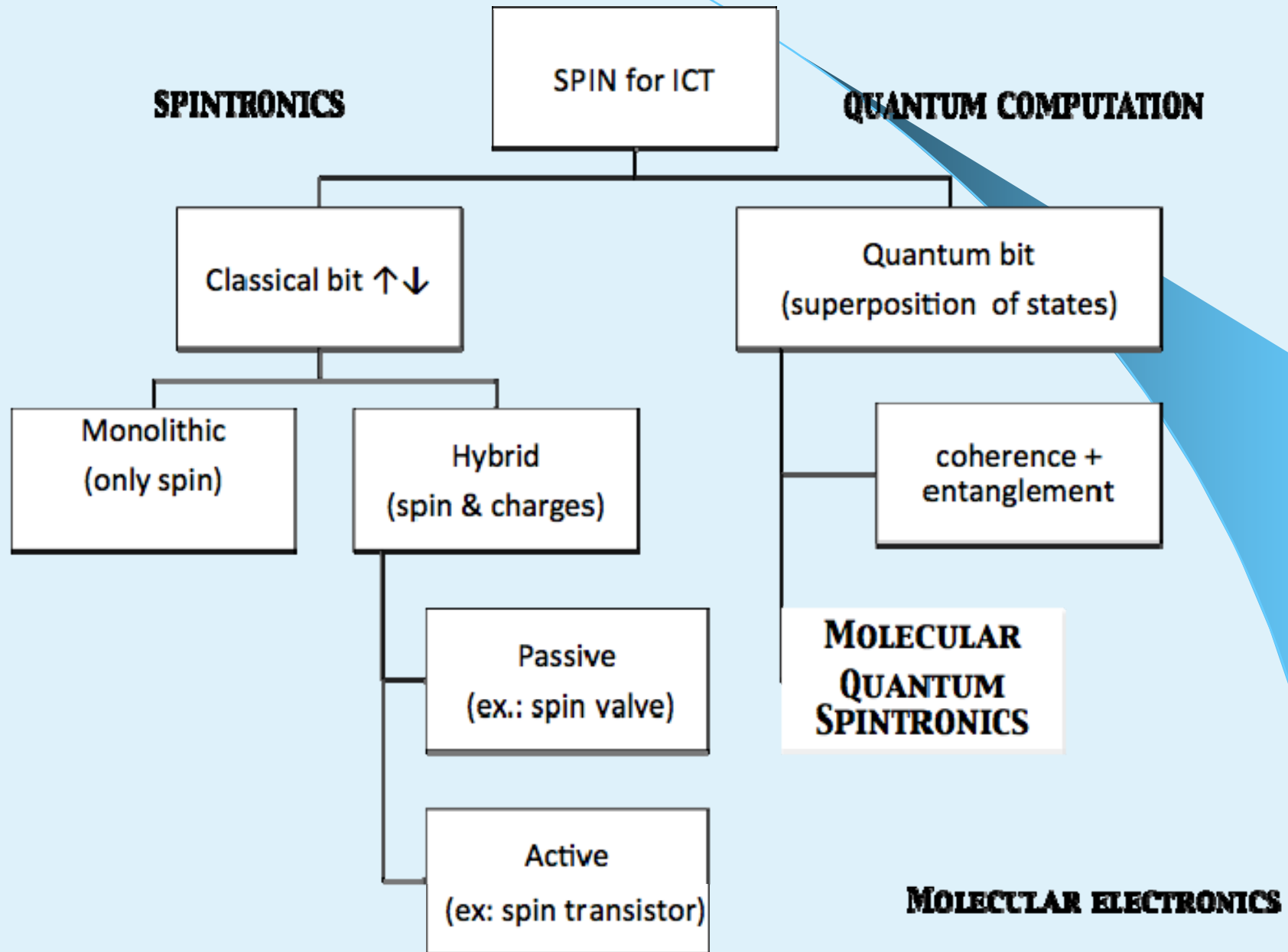


Figure 1 | Fe₄ molecule adsorbed on the Cu₂N surface. (a) [Fe₄(L)₂(dpm)₆] resting on the Cu₂N surface.

Molecular spintronics and quantum computation



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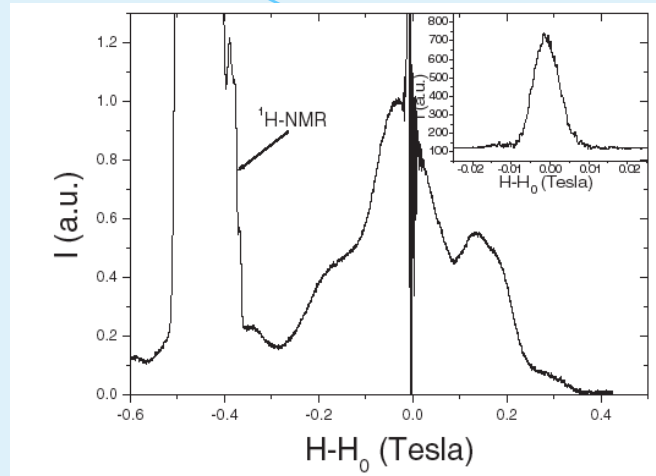
Quantum bits

$$|\psi\rangle = \alpha |\uparrow\rangle + \beta |\downarrow\rangle$$

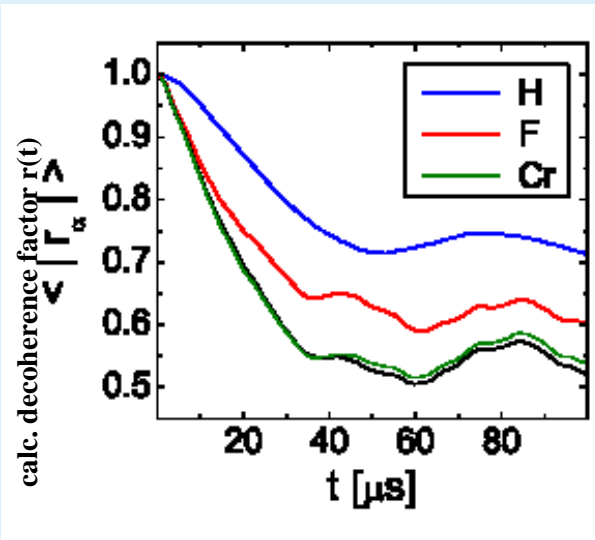
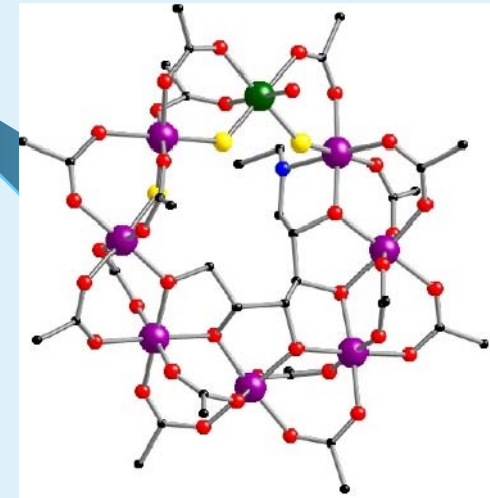


Quantum coherence in antiferromagnetic rings

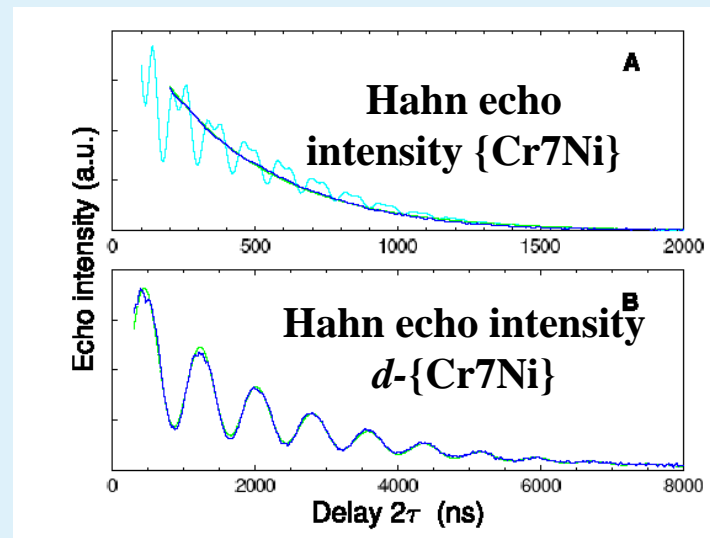
Cr7Ni



Micotti et al. PRL 97, 267204 (2006)



F. Troiani, V. Bellini, and M. Affronte
Physical Review B 77, 054428 (2008).



glued Cr7Ni in which
fluoride groups are replaced by alkoxides
G.Timco et al. Angew. Chem.2008, 47, 9681

Ardavan et al. PRL 98, 057201 (2007)

Entanglement as a genuine quantum phenomenon



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separate objects with well defined states.



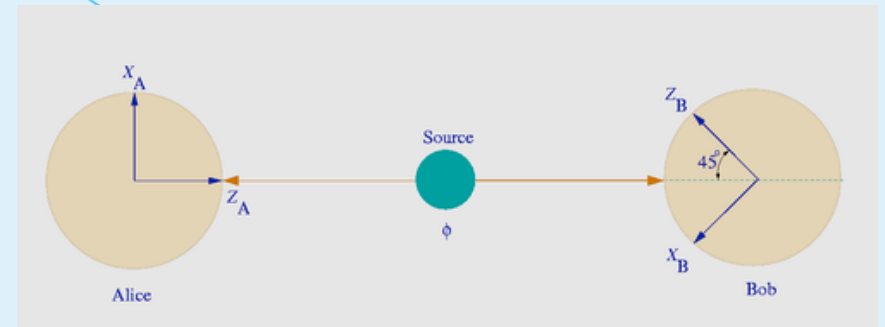
weak (initial) coupling.



the states of each subsystem can no longer be described independently from one to another!



the state of the global system cannot be factorized



example of separable state:

$$|\Psi\rangle = |\uparrow_A\rangle |\downarrow_B\rangle$$

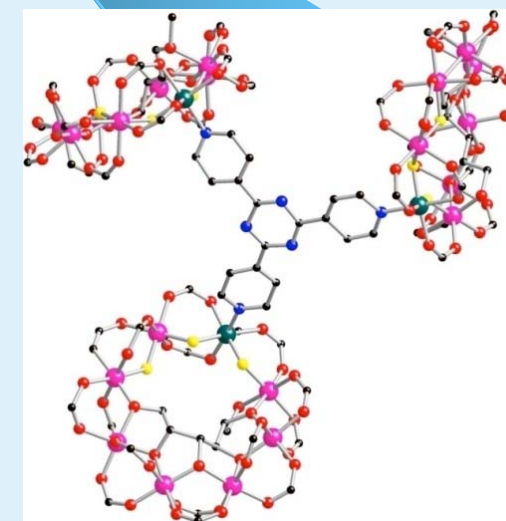
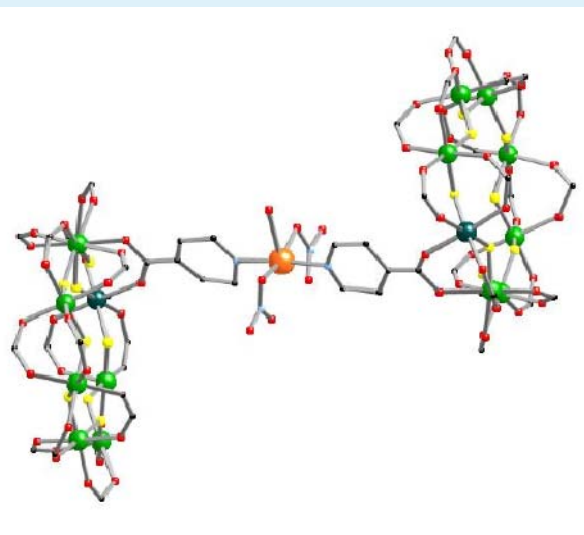
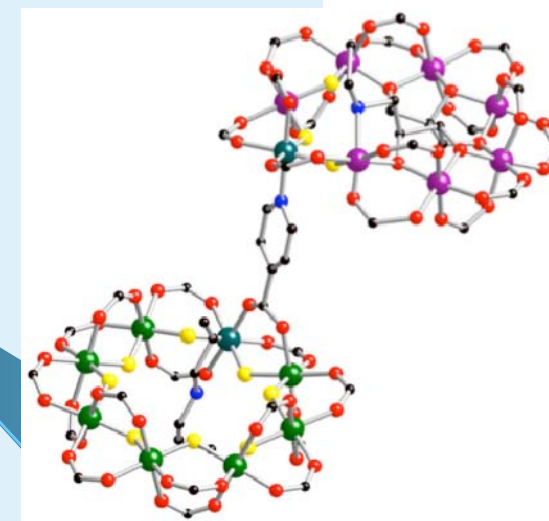
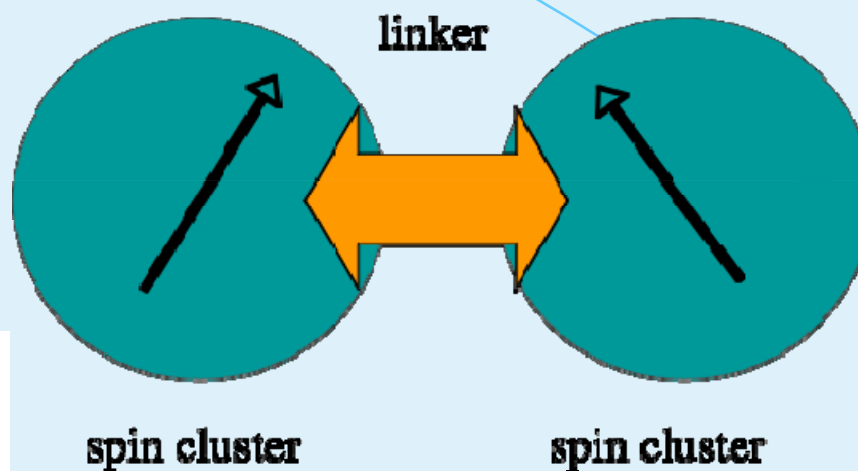
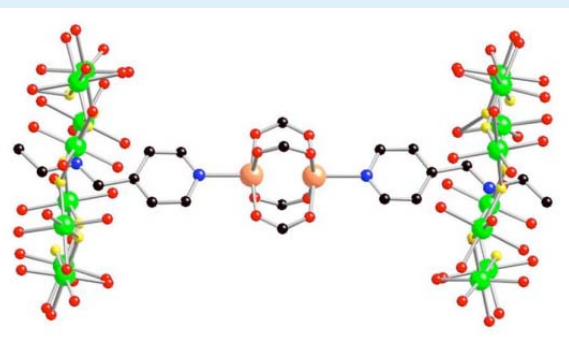
example of entangled state:

Bell (or Einstein, Podolsky, Rosen) state

$$|\Psi\rangle = \frac{1}{\sqrt{2}} (|\uparrow_A\rangle |\downarrow_B\rangle + |\downarrow_A\rangle |\uparrow_B\rangle)$$

A measurement of the second qubit always gives result depending on the state of the first

Rules of "this" game



**To entangle the spins of
different molecular units**

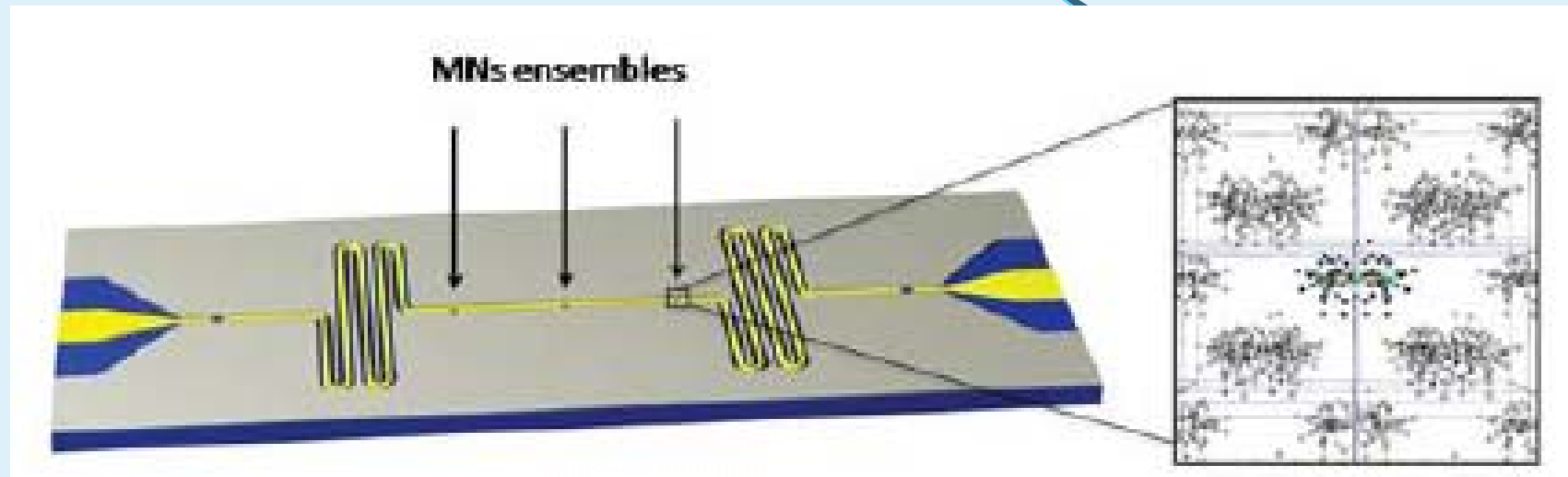
Molecular spin clusters for Quantum Computation



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| molecule | references | Identification of qubit & scalability | Reliable state & preparation | Decoherence time | Control of coupling | Read out |
|----------------------------------|--|---|------------------------------|--------------------------|---------------------|----------|
| Cr₇Ni | Phys. Rev. Lett. 2007, 98, 057201 | S=1/2 Crystals assembly surface | by cooling in magnetic field | 15 μ s @ 1K | yes | ESR |
| V₁₅ | Nature, 2008, 455, 208 | S=3/2 in solution | by cooling in magnetic field | 0.4 μ s @ 4K | | ESR |
| Cu₂ | unpublished | S=1/2 | by cooling in magnetic field | 1 μ s @ 1K | | ESR |
| Nit-Radicals | unpublished | S=1/2 on surface | | 3 μ s @ 70K | | FSR |
| (malonyl) radicals | J. Mater. Chem. 2009, 19, 8789-8794 | S=1/2 - nuclear I | Pseudo-pure state | μ s @ 1K + higher T. | yes | ENDOR |
| POM polyoxometallate | unpublished | S \geq 1/2 Crystals | by cooling in magnetic field | 1 μ s @ 1K | | FSR |
| Fe₄ | Phys. Rev. Lett. 2008, 101, 147201. | S=5 multiplet | by cooling in magnetic field | 0.64 μ s @ 2K | | FSR |
| Fe₈ | PR. 2009, 106, 087403 Nature 474, 76 (2011) | S=10 multiplet | by cooling in magnetic field | 0.7 μ s @ 1K | yes | FSR |
| Mn₁₂ | Nature, 2000, 403, 719. | S=10 multiplet not scalable | by cooling in magnetic field | | | - |
| Er³⁺ ions | Nature Nanotech 2009, 2, 49. | J=15/2 Impurities in crystalline matrix CaWO ₄ | by cooling in magnetic field | μ s @ 2K | ? | FSR |
| Tb₂ | PR. 107, 117203 (2011) | 2x J=6 | | | yes | |
| SMM linked by diketonates | Chem -Eur J, 2009, 15, 11288 | | | ? | yes | - |

Cavity-assisted Quantum Information Processing



superconducting resonators with Molecular Nanomagnets

In progress.

YBCO resonator already realized



Pavia, 07/06/16

The end

Any questions ??

